Ratio and Proportion
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Research and Teaching in Mathematics Teachers’ Education (Pre- and In-Service Mathematics Teachers of Elementary and Middle School Classes)

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SENSE PUBLISHERS
ROTTERDAM/BOSTON/TAIPEI
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