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# Hypercomplex Analysis

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# Preface

This volume contains some papers written by the participants to the Session “Quaternionic and Clifford Analysis” of the 6th ISAAC Conference (held in Ankara, Turkey, in August 2007) and some invited contributions. The contents cover several different aspects of the hypercomplex analysis. All contributed papers represent the most recent achievements in the area as well as “state-of-the-art” expositions.

The Editors are grateful to the contributors to this volume, as their works show how the topic of hypercomplex analysis is lively and fertile, and to the referees, for their painstaking and careful work. The Editors also thank professor M.W. Wong, President of the ISAAC, for his support which made this volume possible.

October 2008,

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