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Dynamical Systems V

Bifurcation Theory
and Catastrophe Theory

With 130 Figures



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N.D. Kazarinoff

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