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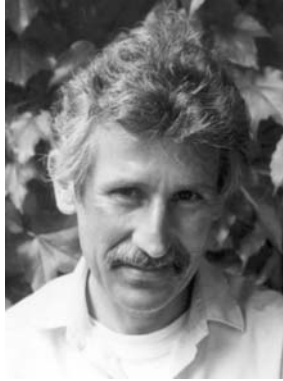


Photo by George Bergman.

Marc Yor, one of the most prominent members of the French probabilistic school, is turning 60. For the last 33 years, he contributed to the Séminaire by his own articles and his counselling of other authors; his methods and style permeate throughout the volumes of this series. He was a tireless member of the Rédaction during a quarter of a century, from Volume XIV to XXXIX, careful to maintain the highest quality, from broad mathematical ideas to minutest details. We wish we were able to keep up with the high standards he has set! Since Volume XL, he is no longer an official rédacteur, but keeps helping us with the editorial work and the refereeing.

Marc, nous te souhaitons un joyeux anniversaire, et nous sommes heureux de te dédier ce volume.

Catherine Donati-Martin, Michel Émery,
Alain Rouault, Christophe Stricker

Preface

Nine volumes ago, in Séminaire de Probabilités XXXIII, a series of advanced courses was started; nine such courses have appeared since. Two of them are due to Antoine Lejay, including his *Introduction to rough paths* in volume XXXVII. This unrepentant recidivist now strikes again, with *Yet another introduction to rough paths*, which sheds a more algebraic light on the same matter.

The various contributions which constitute the rest of the volume exemplify the rôle the Séminaire intends to play on the probabilistic stage: junior authors go side by side with older contributors, with a predominance from French or francophile ones; short notes mix with real research articles; and the themes are well in the traditional spirit of the Séminaire, ranging over the broad spectrum of interest of the readership of the Séminaire.

*Catherine Donati-Martin, Michel Émery,
Alain Rouault, Christophe Stricker*

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