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P.S. Bullen P.Y. Lee J.L. Mawhin
P. Muldowney W.F. Pfeffer (Eds.)

New Integrals

Proceedings of the Henstock Conference
held in Coleraine, Northern Ireland, August 9–12, 1988



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Editors

Peter S. Bullen
Department of Mathematics, University of British Columbia
Vancouver, British Columbia
Canada V6T 1Y4

Peng Yee Lee
Department of Mathematics, National University of Singapore
Singapore 0511, Republic of Singapore

Jean L. Mawhin
Département de Mathématiques, Université Catholique de Louvain
2 chemin du Cyclotron, 1348 Louvain-La-Neuve, Belgium

Patrick Muldowney
Magee College, University of Ulster
Londonderry BT48 7JL, Northern Ireland

Washek F. Pfeffer
Department of Mathematics, University of California
Davis, CA 95616, USA

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PREFACE

The Twelfth Summer Symposium in Real Analysis, August 9-12 1988, was held at the Coleraine campus of the University of Ulster. The theme of the conference was new integrals and related subjects, with particular reference to the generalised Riemann integral of R. Henstock and J. Kurzweil. This volume contains a brief introduction to the theme by R. Henstock, and a survey article by S. Foglio.

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P. M.

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