

Lecture Notes in Mathematics

1840

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Boris Tsirelson Wendelin Werner

Lectures on Probability Theory and Statistics

Ecole d'Eté de Probabilités
de Saint-Flour XXXII - 2002

Editor: Jean Picard



Springer

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Cover picture: Blaise Pascal (1623-1662)

Cataloging-in-Publication Data applied for

Bibliographic information published by Die Deutsche Bibliothek

Die Deutsche Bibliothek lists this publication in the Deutsche Nationalbibliografie;
detailed bibliographic data is available in the Internet at <http://dnb.ddb.de>

Mathematics Subject Classification (2001):
60-01, 60Gxx, 60J65, 60K35, 82B20, 82B27, 82B41

ISSN 0075-8434 Lecture Notes in Mathematics
ISSN 0721-5363 Ecole d'Été des Probabilités de St. Flour
ISBN 3-540-21316-3 Springer-Verlag Berlin Heidelberg New York

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Printed in Germany

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Typesetting: Camera-ready \TeX output by the authors

SPIN: 10994733 41/3142/du - 543210 - Printed on acid-free paper

Preface

Three series of lectures were given at the 32nd Probability Summer School in Saint-Flour (July 7–24, 2002), by Professors Pitman, Tsirelson and Werner. In order to keep the size of the volume not too large, we have decided to split the publication of these courses into two parts. This volume contains the courses of Professors Tsirelson and Werner. The course of Professor Pitman, entitled “Combinatorial stochastic processes”, is not yet ready. We thank the authors warmly for their important contribution.

76 participants have attended this school. 33 of them have given a short lecture. The lists of participants and of short lectures are enclosed at the end of the volume.

Finally, we give the numbers of volumes of Springer *Lecture Notes* where previous schools were published.

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