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PREFACE

This volume contains articles based on talks given at the Seminar on Functional Analysis and Function Theory held at Kristiansand, Norway, June 9 - 14 1975.

Although the papers herein covers a broad area of mathematical research, most of them are in some way connected with algebras and spaces of analytic functions in one or several complex variables. Hopefully this report will be of interest to mathematicians working within these and related areas.

We wish to thank all the participants and contributors for their cooperation. And we gratefully acknowledge the generous financial support from the Norwegian Research Council (NAVF) and from Agder Distriktshøgskole. We also wish to express our gratitude to Professor Erik Alfsen, University of Oslo for his steady encouragement during the preparation of the seminar. We would also like to give special thanks to our secretary Ingrid Skram for her assistance during the seminar and her efficient typing of the manuscripts.

Otto B. Bekken

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SEMINAR IN FUNCTIONAL ANALYSIS AND FUNCTION THEORY
JUNE 9-14, 1975 IN KRISTIANSAND S., NORWAY

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