

# Lecture Notes in Mathematics

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Riemann Surfaces, Theta Functions,  
and Abelian Automorphisms Groups

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