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## PREFACE

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Le présent volume contient le texte des exposés que les conférenciers ont bien voulu nous faire parvenir. Toutefois, la liste des articles publiés ne correspond pas exactement avec celle des conférences présentées durant le Colloque. C'est le cas, en particulier, lorsque les exposés concernaient des travaux déjà publiés ou dont la publication était prévue par ailleurs.

Outre les participants à cette rencontre, nous tenons à remercier l'U.E.R. de Marseille-Luminy et le Centre International de Rencontres Mathématiques qui ont rendu possible la tenue de ce Colloque, ainsi que le secrétariat du département de Mathématiques qui a assuré une partie de la frappe des textes dactylographiés.

Jacques CARMONA

Michèle VERGNE

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