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A collection of informal reports and seminars

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Proceedings of the International Symposium at
McMaster University, Canada, April, 1968

Edited by M. Behara, K. Krickeberg, and J. Wolfowitz

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Preface

This volume contains the invited lectures presented at the First International Symposium on Probability and Information Theory which was held at McMaster University, Hamilton, Ontario, Canada, April 4th and 5th, 1968.

The purpose of the Symposium was to bring together for discussion workers in probability theory and information theory, and to provide relatively quick publication for their contributions.

We would like to thank Professor H.G. Thode, M.B.E., F.R.S.C., F.R.S., President of McMaster University, for his address of welcome, and Professor A.N. Bourns, F.R.S.C., Vice-President, Academic (Science) of McMaster, for acting as host to the participants in the International Symposium. We also thank Professor Husain, Chairman of the Mathematics Department, and Professor G. Bruns for their financial and overall support, without which this Symposium would never have taken place. We gratefully acknowledge major financial support from the National Research Council of Canada. Finally, we take great pleasure in thanking Professor I.Z. Chorneyko for his valuable help in organizing the Symposium.

M. Behara, K. Krickeberg, J. Wolfowitz

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