

Lecture Notes in Mathematics

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The Structure
of Nuclear Fréchet Spaces



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To Andrzej

"We have the greatest freedom when we are bound
together with those we love"

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