

# Lecture Notes in Statistics

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# Lecture Notes in Statistics

Edited by D. Brillinger, S. Fienberg, J. Gani,  
J. Hartigan, and K. Krickeberg

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## Time Series Analysis of Irregularly Observed Data

Proceedings of a Symposium  
held at Texas A & M University, College Station, Texas  
February 10–13, 1983

Edited by Emanuel Parzen

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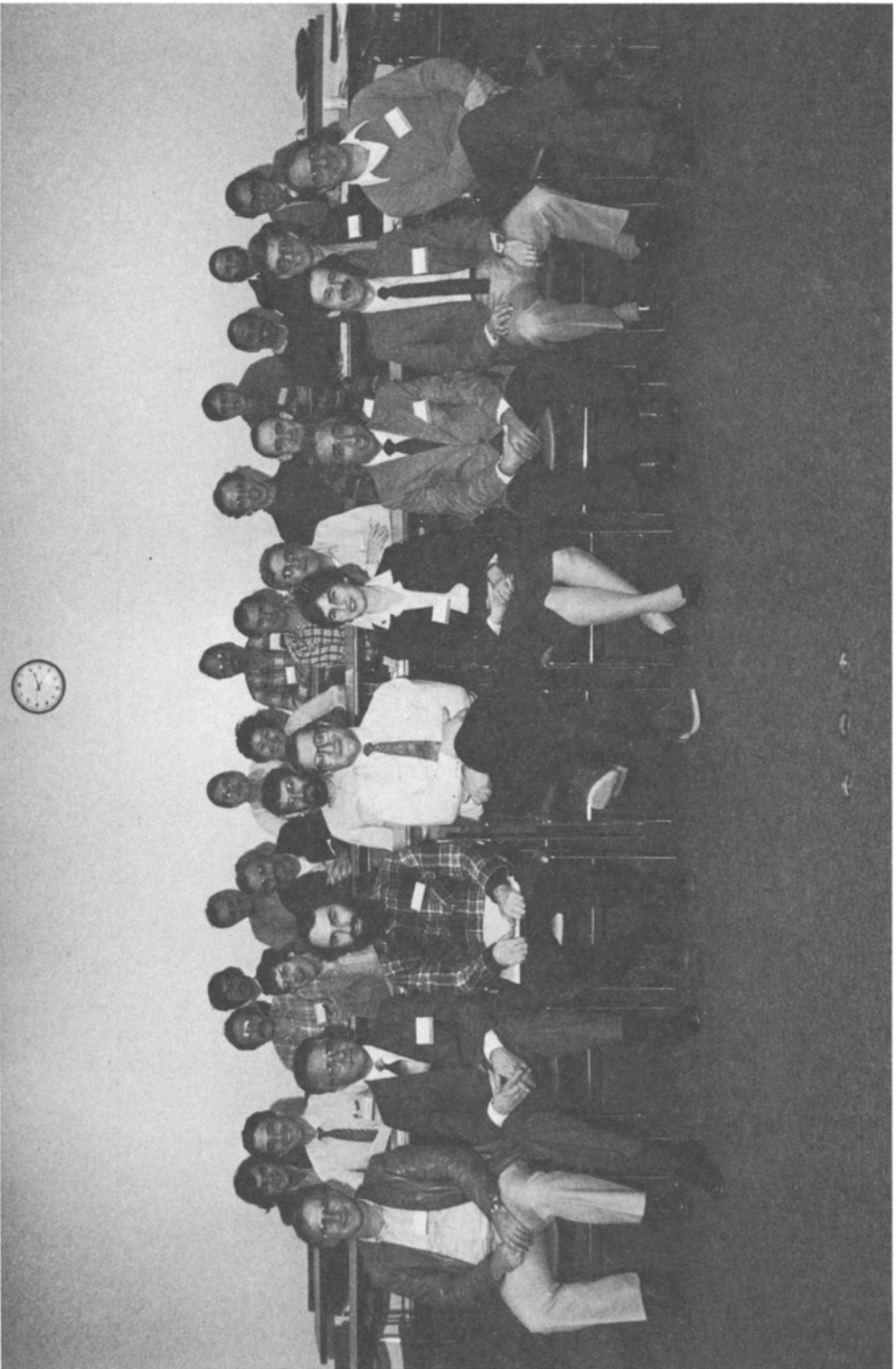
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## PREFACE

With the support of the Office of Naval Research Program on Statistics and Probability (Dr. Edward J. Wegman, Director), The Department of Statistics at Texas A&M University hosted a Symposium on Time Series Analysis of Irregularly Observed Data during the period February 10-13, 1983. The symposium aimed to provide a review of the state of the art, define outstanding problems for research by theoreticians, transmit to practitioners recently developed algorithms, and stimulate interaction between statisticians and researchers in subject matter fields. Attendance was limited to actively involved researchers.

This volume contains refereed versions of the papers presented at the Symposium. We would like to express our appreciation to the many colleagues and staff members whose cheerful help made the Symposium a successful happening which was enjoyed socially and intellectually by all participants. I would like to especially thank Dr. Donald W. Marquardt whose interest led me to undertake to organize this Symposium.

This volume is dedicated to the world wide community of researchers who develop and apply methods of statistical analysis of time series.



Picture Caption

Participants in Symposium on Time Series Analysis of Irregularly Observed Data at Texas A&M University, College Station, Texas, February 10-13, 1983

First Row: Henry L. Gray, D. W. Marquardt, P. M. Robinson, Emanuel Parzen, Julia Abrahams, E. Masry, H. L. Weinert, R. H. Shumway.

Second Row: W. T. M. Dunsmuir, A. C. Harvey, V. Solo, O. M. Ferreiro, R. B. Miller, A. D. Thrall

Third Row: H. Joseph Newton, C. Ansley, Eugene L. Sobel, Mildred Francis, W. Weber, David F. Findley, M. Hinich, William A. Coberly

Fourth Row: G. Kitagawa, Will Gersch, Jeff Hart, R. H. Jones, Roy Mendelssohn, D. Brillinger

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## CONTENTS

	Page
Parzen, Emanuel. Introduction . . . . .	1
Ansley, Craig and Kohn, Robert. On the estimation of ARIMA Models with missing values. . . . .	9
Brillinger, David R. Statistical inference for irregularly observed processes. . . . .	38
Dunsmuir, William. Large sample properties of estimation in time series observed at unequally spaced times. . . . .	58
Dunsmuir, William. Time series regression with periodically correlated errors and missing data. . . . .	78
Harvey, A. C. and McKenzie, C. R. Missing observations in dynamic econometric models: a partial synthesis . . . . .	108
Hinich, Melvin J. and Weber, Warren E. A Hilbert transform method for estimating distributed lag models with randomly missed or distorted observations. . . . .	134
Jones, Richard H. Fitting multivariate models to unequally spaced data . . . . .	158
Kitagawa, Genshiro. State space modeling of nonstationary time series and smoothing of unequally spaced data. . . . .	189
Marquardt, Donald W. and Acuff, Sherry K. Direct quadratic spectrum estimation with irregularly spaced data. . . . .	211
Masry, Elias. Spectral and probability density estimation from irregularly observed data. . . . .	224
Miller, Robert B. and Ferreiro, Osvaldo M. A strategy to complete a time series with missing observations. . . . .	251
Robinson, P. M. Multiple time series analysis of irregularly spaced data . . . . .	276
Shumway, R. H. Some applications of the EM algorithm to analyzing incomplete time series data . . . . .	290
Solo, Victor. Some aspects of continuous-discrete time series modelling . . . . .	325
Thrall, Anthony D. and Burton, C. Shepherd. Inferring the attainment of national ambient air quality standards using missing value time series techniques. . . . .	346
Weinert, Howard L. The complementary model in continuous/ discrete smoothing. . . . .	353