

PROGRESS IN
MATHEMATICS

Volume 9

Algebra and Geometry

PROGRESS IN MATHEMATICS

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Preface

This volume contains five review articles, two in the Algebra part and three in the Geometry part, surveying the fields of categories and class field theory, in the Algebra part, and of Finsler spaces, structures on differentiable manifolds, and packing, covering, etc., in the Geometry part. The literature covered is primarily that published in 1964-1967.

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