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A. J. Mabbett

**M**  
MACMILLAN

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To Sandra, Richard and Claire — thank you for all your patience

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# Preface

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I have written this book specifically for those students studying an introductory course in mathematics; a course which is related to economics, business studies or accountancy. The need for such a workbook as this has become increasingly apparent in recent years with a substantial number of students having only a very elementary grounding in mathematics. Many such students lack that initial confidence of tackling such 'applied' questions as are commonly found in introductory economics. The aim of this book is to get such students started on the road to problem solving.

I should like to thank those students who have inspired me to put all my verbal explanations onto paper. Without their constant encouragement, I would have never started such a project as this. My thanks also go to them for trying out many of the problems. I am not conscious of having made any direct use of other people's examples; however, over the years it is only too easy to collect problems from different sources only to forget their origin; and I apologise if this has happened inadvertently. I should like to thank my colleagues for their constant advice and encouragement. Lastly, my gratitude to my family for their patience while Dad disappeared to write 'that dreaded book'.

*Bromsgrove, 1986*

A. J. M.