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Herbert Hoijtink · Irene Klugkist · Paul A. Boelen  
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# Bayesian Evaluation of Informative Hypotheses

 Springer

*Editors*

Herbert Hoijtink  
Department of Methods and Statistics  
Faculty of Social Sciences  
University of Utrecht  
P.O. Box 80140  
3508 TC Utrecht  
The Netherlands  
h.hoijtink@uu.nl

Irene Klugkist  
Department of Methods and Statistics  
Faculty of Social Sciences  
University of Utrecht  
P.O. Box 80140  
3508 TC Utrecht  
The Netherlands  
i.klugkist@uu.nl

Paul A. Boelen  
Department of Clinical  
and Health Psychology  
Faculty of Social Sciences  
University of Utrecht  
P.O. Box 80140  
3508 TC Utrecht  
The Netherlands  
p.a.boelen@uu.nl

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## Preface

This book provides an overview of the developments in the area of Bayesian evaluation of informative hypotheses that took place since the publication of the first paper on this topic in 2001 [Hoijtink, H. Confirmatory latent class analysis, model selection using Bayes factors and (pseudo) likelihood ratio statistics. *Multivariate Behavioral Research*, **36**, 563–588]. The current state of affairs was presented and discussed by the authors of this book during a workshop in Utrecht in June 2007. Here we would like to thank all authors for their participation, ideas, and contributions. We would also like to thank Sophie van der Zee for her editorial efforts during the construction of this book. Another word of thanks is due to John Kimmel of Springer for his confidence in the editors and authors. Finally, we would like to thank the Netherlands Organization for Scientific Research (NWO) whose VICI grant (453-05-002) awarded to the first author enabled the organization of the workshop, the writing of this book, and continuation of the research with respect to Bayesian evaluation of informative hypotheses.

Utrecht,  
May 2008

*Herbert Hoijtink*  
*Irene Klugkist*  
*Paul A. Boelen*



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## List of Contributors

### **Veerabhadran**

#### **Baladandayuthapani**

Department of Biostatistics  
The University of Texas  
M.D. Anderson Cancer Center  
1515 Holcombe Blvd.  
Houston, 77030 TX, USA  
veera@mdanderson.org

### **Paul A. Boelen**

Department of Clinical and Health  
Psychology  
Utrecht University  
P.O. Box 80140  
3508 TC, Utrecht, the Netherlands  
p.a.boelen@uu.nl

### **Jan Boom**

Department of Developmental  
Psychology  
Utrecht University  
P.O. Box 80140  
3508 TC, Utrecht, the Netherlands  
j.boom@uu.nl

### **Ming-Hui Chen**

Department of Statistics  
University of Connecticut  
215 Glenbrook Road  
U-4120, Storrs, CT 06269, USA  
mhchen@stat.uconn.edu

### **Herbert Hoijtink**

Department of Methodology and  
Statistics  
Utrecht University  
P.O. Box 80140  
3508 TC, Utrecht, the Netherlands  
h.hoijtink@uu.nl

### **Marcel van den Hout**

Department of Clinical and Health  
Psychology  
Utrecht University  
P.O. Box 80140  
3508 TC, Utrecht, the Netherlands  
m.vandenhout@uu.nl

### **Rafaele Huntjens**

Department of Experimental  
Psychopathology  
Groningen University  
Grote Kruisstraat 2/1  
9712 TS, Groningen, the Netherlands  
r.j.c.huntjens@rug.nl

### **Geoffrey J. Iverson**

Department of Cognitive Sciences  
University of California at Irvine  
3151 Social Science Plaza  
Irvine, CA 92697, USA  
giverson@uci.edu

**Valen E. Johnson**

Department of Biostatistics  
The University of Texas  
M.D. Anderson Cancer Center  
1515 Holcombe Blvd.  
Houston, 77030 TX, USA  
vejohanson@mdanderson.org

**George Karabatsos**

College of Education  
University of Illinois-Chicago  
1040 W. Harrison Street  
Chicago, IL 60607, USA  
georgek@uic.edu

**Bernet Sekasanvu Kato**

Twin Research and Genetic  
Epidemiology Unit  
St. Thomas' Hospital Campus  
King's College London  
Westminster Bridge Road  
London, SE1 7EH, United Kingdom  
bernet.kato@kcl.ac.uk

**SungDuk Kim**

Division of Epidemiology  
Statistics and Prevention Research  
National Institute of Child Health  
and Human Development NIH  
Rockville, MD 20852, USA  
kims2@mail.nih.gov

**Irene Klugkist**

Department of Methodology and  
Statistics  
Utrecht University  
P.O. Box 80140  
3508 TC, Utrecht, the Netherlands  
i.klugkist@uu.nl

**Annemarie Kolk**

Clinical Psychology  
University of Amsterdam  
Roeterstraat 15  
1018 WB, Amsterdam  
the Netherlands  
a.m.m.kolk@uva.nl

**Rebecca Kuiper**

Department of Methodology and  
Statistics  
Utrecht University  
P.O. Box 80140  
3508 TC, Utrecht, the Netherlands  
r.m.kuiper@uu.nl

**Olav Laudy**

Department of Methodology and  
Statistics  
Utrecht University  
P.O. Box 80140  
3508 TC, Utrecht, the Netherlands  
o.laudy@uu.nl

**Michael Lee**

Department of Cognitive Sciences  
University of California at Irvine  
3151 Social Science Plaza  
Irvine, CA 92697, USA  
mdlee@uci.edu

**Guimei Liu**

Department of Mathematics  
University of Puerto Rico at Rio  
Piedras Campus  
P.O. Box 23355  
San Juan, 00931-3355, Puerto Rico  
liugm@zucc.edu.cn

**Tom Lodewyckx**

Department of Quantitative and  
Personality Psychology  
University of Leuven  
Tiensestraat 102  
3000 Leuven, Belgium  
tom.lodewyckx@student.kuleuven.be

**Joris Mulder**

Department of Methodology and  
Statistics  
Utrecht University  
P.O. Box 80140  
3508 TC, Utrecht, the Netherlands  
j.mulder3@uu.nl

**Jay I. Myung**

Department of Psychology  
Ohio State University  
1835 Neil Avenue  
Columbus, OH, 43210, USA  
myung.1@osu.edu

**Carel F.W. Peeters**

Department of Methodology and  
Statistics  
Utrecht University  
P.O. Box 80140  
3508 TC, Utrecht, the Netherlands  
c.f.w.peeters@uu.nl

**Luis Raúl Pericchi Guerra**

Department of Mathematics  
University of Puerto Rico at Rio  
Piedras Campus  
P.O. Box 23355  
San Juan 00931-3355, Puerto Rico  
lrpericchi@uprrp.edu and  
luarpr@gmail.com

**Albert Reijntjes**

Department of Pedagogical and  
Educational Sciences  
Utrecht University  
P.O. Box 80140  
3508 TC, Utrecht, the Netherlands  
a.h.a.reijntjes@uu.nl

**Marleen Rijkeboer**

Department of Clinical and Health  
Psychology  
Utrecht University  
P.O. Box 80140  
3508 TC, Utrecht, the Netherlands  
m.m.rijkeboer@uu.nl

**Jan-Willem Romeijn**

Department of Theoretical  
Philosophy  
Groningen University  
Oude Boteringstraat 52  
9712 GL, Groningen, the Netherlands  
j.w.romeijn@rug.nl

**David Rossel**

Bioinformatics and Biostatistics Unit  
Institute for Research in  
Biomedicine of Barcelona  
Josep Samitier 1-5  
08028 Barcelona, Spain  
rosselldavid@gmail.com

**Rens van de Schoot**

Department of Methodology and  
Statistics  
Utrecht University  
P.O. Box 80140  
3508 TC, Utrecht, the Netherlands  
a.g.j.vandeschoot@uu.nl

**David Torres Nunez**

Department of Mathematics  
University of Puerto Rico at Rio  
Piedras Campus  
P.O. Box 23355  
San Juan 00931-3355, Puerto Rico  
david.torres.math@gmail.com

**Eric-Jan Wagenmakers**

Department of Psychology  
University of Amsterdam  
Roetersstraat 15  
1018 WB, Amsterdam  
the Netherlands  
ej.wagenmakers@gmail.com

**Sonja van Well**

Clinical Psychology  
University of Amsterdam  
Roeterstraat 15  
1018 WB Amsterdam  
the Netherlands  
s.m.vanwell@uva.nl

**Floryt van Wesel**

Department of Methodology and  
Statistics  
Utrecht University  
P.O. Box 80140  
3508 TC, Utrecht, the Netherlands  
f.vanwesel@uu.nl