IUTAM Symposium on Mechanical and Electromagnetic Waves in Structured Media

SOLID MECHANICS AND ITS APPLICATIONS Volume 91

Series Editor: G.M.L. GLADWELL Department of Civil Engineering University of Waterloo Waterloo, Ontario, Canada N2L 3GI

Aims and Scope of the Series

The fundamental questions arising in mechanics are: *Why?*, *How?*, and *How much?* The aim of this series is to provide lucid accounts written by authoritative researchers giving vision and insight in answering these questions on the subject of mechanics as it relates to solids.

The scope of the series covers the entire spectrum of solid mechanics. Thus it includes the foundation of mechanics; variational formulations; computational mechanics; statics, kinematics and dynamics of rigid and elastic bodies: vibrations of solids and structures; dynamical systems and chaos; the theories of elasticity, plasticity and viscoelasticity; composite materials; rods, beams, shells and membranes; structural control and stability; soils, rocks and geomechanics; fracture; tribology; experimental mechanics; biomechanics and machine design.

The median level of presentation is the first year graduate student. Some texts are monographs defining the current state of the field; others are accessible to final year undergraduates; but essentially the emphasis is on readability and clarity.

IUTAM Symposium on

Mechanical and Electromagnetic Waves in Structured Media

Proceedings of the IUTAM Symposium held in Sydney, NSW, Australia, 18–22 January 1999

Edited by

ROSS C. McPHEDRAN University of Sydney, Sydney, Australia

LINDSAY C. BOTTEN

University of Technology, Sydney, Australia

and

NICOLAE A. NICOROVICI

University of Sydney, Sydney, Australia

KLUWER ACADEMIC PUBLISHERS New York, BOSTON, DORDRECHT, LONDON, MOSCOW

eBook ISBN: 0-306-46955-3 Print ISBN: 0-792-37038-4

©2002 Kluwer Academic Publishers New York, Boston, Dordrecht, London, Moscow

All rights reserved

No part of this eBook may be reproduced or transmitted in any form or by any means, electronic, mechanical, recording, or otherwise, without written consent from the Publisher

Created in the United States of America

Visit Kluwer Online at: and Kluwer's eBookstore at: http://www.kluweronline.com http://www.ebooks.kluweronline.com Organizing Committee

L. C. Botten, Chairman, University of Technology, Sydney N. F. Cramer, University of Sydney C. M. de Sterke, University of Sydney E. Morris, University of Sydney N. A. Nicorovici, University of Sydney A. Reuben, University of Technology, Sydney

Scientific Committee

R. C. McPhedran, Chairman, University of Sydney, Australia A. Priou, University of Paris X, France
A. Jordan, Naval Research Laboratory, Washington, USA
V. I. Erofeyev, Russian Academy of Sciences, Nizhny Novgorod, Russia
M. A. Hayes, University College, Dublin, Ireland
R. K. T. Hsieh, Royal Institute of Technology, Sweden
A. B. Movchan, University of Liverpool, UK
N. Phan-Thien, University of Sydney, Australia
G. W. Milton, University of Utah, USA
A. Thess, Technical University, Dresden, Germany

Contents

Preface

Contributing Authors	xiii
Part I OVERVIEW	
1 Electric and Elastic Properties of Linear and Non-Linear Composites G. W. Milton	3
 2 Advances in the Rayleigh Multipole Method for Problems in Photonics and Phononics <i>R. C. McPhedran, N. A. Nicorovici, L. C. Botten, and A. B. Movchan</i> 	15
Part II ASPECTS OF ELECTROMAGNETIC WAVES	
3 Random Scattering and the Detection Capability of the Magnetotelluric Method Benjamin S. White, Werner Kohler, and Leonard J. Srnka	31
4 Phase Singularities in Beams <i>G. F. Brand</i>	43
5 Nonlinear Pulse Propagation in Fibre Gratings B. J. Eggleton, C. Martijn de Sterke, and R. E. Slusher	57

xi

Part III ASPECTS OF MECHANICAL WAVES

viii	
Radiation From a Transducer into an Elastic Half-Space G. W. Owen and I. D. Abrahams	73
7 Energy Flux in Elasticity and Electromagnetism Philippe Boulanger and Michael Hayes	89
8 On Oscillation of Layered Structures with Imperfect Interfaces A. Movchan, S. Sorokin, and Ö. Selsil	101
 9 Free Vibration of Elastic Solids: Effect of Boundary Perturbation on Fun- damental frequencies N. V. Movchan 	111
10 Diffusing Acoustic Wave Transport and Spectroscopy J. H. Page, M. L. Cowan, Ping Sheng, and D. A. Weitz	121
Part IV COMPOSITES	
11 Charged Dust Structures in Plasmas N. F. Cramer and S. V. Vladimirov	135
12 Longitudinal Magneto–Elastic Waves in Solids with Microstructure V. Erofeyev, V. Kazhaev, and S. Kovalev	149
13 Transport Properties of a Fibre–Layer Composite Material V. V. Mityushev and T. N. Zhorovina	159
 14 Laplace Transform Methods and the Rayleigh Identity for an Array of Elliptical Cylinders A. J. Reuben, J. G. Yardley, and R. C. McPhedran 	169
Part V HOMOGENIZATION	
Symmetry Breaking in Annular Domains for a Ginzburg–Landau Super- conductivity Model	189
Leonid Berlyand and Karl Voss	
16Diffraction by Perfectly Conducting Capacitive Grids: Photonic Band Structures and Circuit ModelsL. C. Botten, R. C. McPhedran, and N. A. Nicorovici	201

17 Photonic Crystal Optics and Homogenization of 2D Periodic Composites <i>P. Halevi, A.A. Krokhin, and J. Arriaga</i>	219	
18 Asymptotics of Photonic Band Structures for Doubly–Periodic Arrays C. G. Poulton, R. C. McPhedran, N. A. Nicorovici, L. C. Botten, and A. B. Move	227 han	
Part VI PHOTONIC BAND GAP MATERIALS AND LOCALIZATION		
19 Electromagnetic Modelling of Dielectric and Metallic Photonic Crystals D. Maystre, G. Tayeb, P. Vincent, S. Enoch, and G. Guida	241	
 20 Band Gap Engineering in Metallic PBG Materials at Microwave Frequencies Using Composite Material and Defect Lattice F. Gadot, E. Akmansoy, T. Brillat, A. de Lustrac, and JM. Lourtioz 	257	
21 Photonic Bands and Scattering for Stacks of Lossy, Dispersive Cylinders N. A. Nicorovici, R. C. McPhedran, L. C. Botten, A. A. Asatryan, P. A. Robinson, C. M. de Sterke	269 and	
22 Surface Plasmons and Zero Order Metal Gratings J. R. Sambles, T. W. Preist, WC. Tan, and N. P. Wanstall	285	
 23 General Characteristics of Localization in Stratified Media with Random Loss and Gain L. C. Botten, C. M. de Sterke, R. C. McPhedran, N. A. Nicorovici, A. A. Asatryan, P. A. Robinson 	297 and	
24 Light Amplification and Attenuation in Stratified Structures with Complex Refractive Index Sergei A. Bulgakov and Manuel Nieto-Vesperinas	311	

Author Index

321

Contents

ix

Preface

The IUTAM Symposium on Mechanical and Electromagnetic Waves in Structured Media took place at the University of Sydney from January 18-22, 1999. It brought together leading researchers from eleven countries for a week-long meeting, with the aim of providing cross-links between the communities studying related problems involving elastic and electromagnetic waves in structured materials. After the meeting, participants were invited to submit articles based on their presentations, which were refereed and assembled to constitute these Proceedings.

The topics covered here represent areas at the forefront of research into elastic and electromagnetic waves. They include effect of nonlinearity, diffusion and multiple scattering on waves, as well as asymptotic and numerical techniques. Composite materials are discussed in depth, with example systems ranging from dusty plasmas to a magneto-elastic microstructured system. Also included are studies of homogenisation, that field which seeks to determine equivalent homogeneous systems which can give equivalent wave properties to structured materials, and inverse problems, in which waves are used as a probe to infer structural details concerning scattering systems. There are also strong groups of papers on the localization of waves by random systems, and photonic and phononic band gap materials. These are being developed by analogue with semiconductors for electrons, and hold out the promise of enabling designers to control the propagation of waves through materials in novel ways.

We would like to thank the other members of the Scientific Committee (A. Priou, A. Jordan, V.I. Erofyev, M.A. Hayes, R.K.T. Hsieh, A.B. Movchan, G.W. Milton, N. Phan-Thien and A. Thess) and of the Organizing Committee (N.F. Cramer, C.M. de Sterke, S. Mackinlay, E. Morris, and A.Reuben) for their help in selecting participants, arranging the venues and functions, and supporting participants. The Symposium ran efficiently and in a friendly atmosphere, and the scientific interchanges were excellent, and this can be attributed in large part to the work of those mentioned.

We would also like to record our appreciation of those who provided the sponsorship which enabled the event to occur, and which helped the travel of researchers from all round the world to Sydney. Our sponsors were: IUTAM, the University of Sydney and the University of Technology Sydney.

Finally, we would like to note that the Symposium was the last scientific event which our colleague, Sergei Bulgakov, was able to attend. Unbeknownst to us, he was fighting a terminal illness, but came to the Symposium, and interacted fully in its program. As a small token of our respect for the ability, dedication and courage of Sergei, we have included in this volume a brief tribute to him, as well as his last paper.

ROSS MCPHEDRAN, LINDSAY BOTTEN AND NICOLAE NICOROVICI

Symposium Sponsors

International Union of Theoretical and Applied Mechanics University of Sydney University of Technology, Sydney

Contributing Authors

Prof. I. D. Abrahams

Department of Mathematics University of Manchester, UK gowen@gwowen.freeserve.co.uk

Dr. E. Akmansoy

Institut d'Optique Théorique et Appliquée Université Paris XI, URA 14 du CNRS Bât 503, 91405 Orsay, FRANCE

Dr. J. Arriaga

Instituto de Física Universidad Autónoma de Puebla Apartado Postal J-48 72570, Puebla, MÉXICO arriaga@sirio.ifuap.buap.mx

Dr. A. A. Asatryan

School of Physics University of Sydney NSW 2006, AUSTRALIA ara@physics.usyd.edu.au

Prof. L. Berlyand

Department of Mathematics The Pennsylvania State University University Park, PA 16801, USA berlyand@math.psu.edu

Prof. L. C. Botten

School of Mathematical Sciences University of Technology, Sydney NSW 2007, AUSTRALIA lindsay @ it.uts.edu.au

Prof. P. Boulanger

Université Libre de Bruxelles 1050 Bruxelles, BELGIUM phboul@@ulb.ac.be

Dr. G. F. Brand

School of Physics University of Sydney NSW 2006, AUSTRALIA brand@physics.usyd.edu.au

Dr. T. Brillat

Groupe d'Electromagnétisme Appliqué IUT de Ville d'Avray Université Paris X 92410 Ville d'Avray, FRANCE

Dr. S. A. Bulgakov

School of Physics University of Sydney NSW 2006, AUSTRALIA (Deceased) **Dr. M. L. Cowan** Dept. of Physics and Astronomy University of Manitoba Winnipeg, Manitoba CANADA, R3T 2N2

Dr. N. F. Cramer

Theoretical Physics Department School of Physics The University of Sydney NSW 2006, AUSTRALIA cramer@physics.usyd.edu.au

Dr. B. J. Eggleton

Bell Laboratories Lucent Technologies Murray Hill 07974 New Jersey, USA

Dr. S. Enoch

Institut Fresnel Faculté des Sciences et Techniques de St Jérôme, case 262 Avenue Escadrille Normandie-Niemen 13397 Marseille Cedex 20, FRANCE enoch@loe.u-3mrs.fr

Prof. V. Erofeyev

Mechanical Engineering Research Institute Russian Academy of Sciences IMASh RAN, ul. Belinskogo, 85 Nizhny Novgorod 603024 RUSSIA wvs@dynamo.nnov.ru

Dr. F. Gadot

Institut d'Electronique Fondamentale Université Paris XI, URA 22 du CNRS Bât 220, 91405 Orsay, FRANCE Frederique.gadot@ief.u-psud.fr

Dr. G. Guida

Institut Fresnel Faculté des Sciences et Techniques de St Jérôme, case 262 Avenue Escadrille Normandie-Niemen 13397 Marseille Cedex 20, FRANCE

Prof. P. Halevi

Instituto de Astrofísica, Optica y Electrónica, Apartado Postal 51 72000, Puebla MÉXICO halevi@inaoep.mx

Prof. M. A. Hayes

University College Dublin Dublin 4, IRELAND Michael.Hayes@@ucd.ie

Dr. V. Kazhaev

Mechanical Engineering Research Institute Russian Academy of Sciences IMASh RAN, ul. Belinskogo, 85 Nizhny Novgorod 603024 RUSSIA

Prof. W. Kohler

Department of Mathematics Virginia Tech Blacksburg, VA 24061, USA kohler@math.vt.edu

Dr. S. Kovalev

Mechanical Engineering Research Institute Russian Academy of Sciences IMASh RAN, ul. Belinskogo, 85 Nizhny Novgorod 603024 RUSSIA kov_serg@yahoo.com

xiv

Prof. A. A. Krokhin

Institute de Física Universidad Autónoma de Puebla, Apartado Postal J-48 72570, Pueblo, MÉXICO

Prof. J.-M. Lourtioz

Institut d'Electronique Fondamentale Université Paris XI, URA 22 du CNRS Bât 220, 91405 Orsay, FRANCE

Prof. A. de Lustrac

Institut d'Electronique Fondamentale Université Paris XI, URA 22 du CNRS Bât 220, 91405 Orsay, FRANCE

Prof. D. Maystre

Institut Fresnel Faculté des Sciences et Techniques de St Jérôme, case 262 Avenue Escadrille Normandie-Niemen 13397 Marseille Cedex 20, FRANCE maystre@loe.u-3mrs.fr

Prof. R. C. McPhedran

School of Physics University of Sydney NSW 2006, AUSTRALIA r.mcphedran@physics.usyd.edu.au

Prof. G. W. Milton

Department of Mathematics University of Utah Salt Lake City, UT 84112, USA milton@utah.edu.au

Prof. V. V. Mityushev

Department of Mathematics Pedagogical College ul. Arciszewskiego 22B 76-200, Slupsk, POLAND mityu@wsp.slupsk.pl

Prof. A. B. Movchan

Department of Mathematical Sciences University of Liverpool Liverpool L69 3BX, UK abm@liv.ac.uk

Dr. N. V. Movchan

Department of Mathematical Sciences University of Liverpool M&O Building Liverpool L69 3BX, UK nvm@liv.ac.uk

Dr. N. A. Nicorovici

School of Physics University of Sydney NSW 2006, AUSTRALIA nicolae@physics.usyd.edu.au

Prof. M. Nieto-Vesperinas

Instituto de Ciencia de Materiales C.S.I.C., Cantoblanco E-28049, Madrid, SPAIN mnieto@bach.icmm.csic.es

Prof. G. W. Owen Department of Mathematics

University of Manchester, UK gowen@gwowen.freeserve.co.uk

Prof. J. H. Page Dept. of Physics and Astronomy University of Manitoba Winnipeg, Manitoba CANADA, R3T 2N2 jhpage@cc.UManitoba.CA

Dr. C. G. Poulton School of Physics University of Sydney NSW 2006, AUSTRALIA C.Poulton@liv.ac.uk

Dr. T. W. Preist

Thin Film Photonics Group School of Physics University of Exeter Exeter EX4 4QL, UK

Dr. A. J. Reuben

Department of Applied Physics University of Technology, Sydney NSW 2007, AUSTRALIA

Prof. P. A. Robinson

School of Physics University of Sydney NSW 2006, AUSTRALIA robinson@physics.usyd.edu.au

Prof. J. R. Sambles

Thin Film Photonics Group School of Physics University of Exeter Exeter EX4 4QL, UK j.r.sambles @ exeter.ac.uk

Dr. Ö. Selsil

University of Liverpool Liverpool, L69 3BX, UK

Prof. Ping Sheng

Dept. of Physics Hong Kong Univ. of Science & Technology Clear Water Bay, Kowloon HONG KONG

Dr. R. E. Slusher

Bell Laboratories Lucent Technologies Murray Hill 07974 New Jersey, USA

Dr. S. Sorokin

Marine Technical University St. Petersburg, RUSSIA

Dr. L. J. Srnka

ExxonMobil Upstream Research Company P. O. Box 2189 Houston, TX 77252, USA len.j.srnka@exxon.sprint.com

Dr. C. M. de Sterke

School of Physics University of Sydney NSW 2006, AUSTRALIA m.desterke@physics.usyd.edu.au

Dr. W.-C. Tan

Thin Film Photonics Group School of Physics University of Exeter Exeter EX4 4QL, UK

Prof. G. Tayeb

Institut Fresnel Faculté des Sciences et Techniques de St Jérôme, case 262 Avenue Escadrille Normandie-Niemen 13397 Marseille Cedex 20, FRANCE tayeb@loe.u-3mrs.fr

Prof. P. Vincent Institut Fresnel Faculté des Sciences et Techniques

xvi

de St Jérôme, case 262 Avenue Escadrille Normandie-Niemen 13397 Marseille Cedex20, FRANCE

Dr. S. V. Vladimirov

Research Centre for Theoretical Astrophysics, School of Physics The University of Sydney NSW 2006, AUSTRALIA vladimi@physics.usyd.edu.au

Dr. K. Voss

Department of Mathematics The Pennsylvania State University University Park, PA 16801, USA voss@math.psu.edu

Dr. N. P. Wanstall

Thin Film Photonics Group School of Physics University of Exeter Exeter EX4 4QL, UK **Prof. D. A. Weitz** Dept. of Physics and Astronomy University of Pennsylvania Philadelphia, PA 19104-6396, USA

Dr. B. S. White

ExxonMobil Research and Engineering Company Route 22E, Annandale NJ 08801, USA bswhite@erenj.com

Dr. J. G. Yardley

Department of Theoretical Physics School of Physics University of Sydney NSW 2006, AUSTRALIA yardley@physics.usyd.edu.au

Dr. T. N. Zhorovina

Department of Mathematics Pedagogical College ul. Arciszewskiego 22B 76-200, Slupsk, POLAND