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We try to give closest numbers; ± may be an additional position indication. C stands for Corollary, D for Definition, E for Exercise or Example, L. for Lemma, P. for Proposition, R. for Remark, S. for Section, T. for Theorem. We try to put definitions first.

Ferran Sunyer i Balaguer (1912–1967) was a self-taught Catalan mathematician who, in spite of a serious physical disability, was very active in research in classical mathematical analysis, an area in which he acquired international recognition. His heirs created the Fundació Ferran Sunyer i Balaguer inside the Institut d'Estudis Catalans to honor the memory of Ferran Sunyer i Balaguer and to promote mathematical research.
Each year, the Fundació Ferran Sunyer i Balaguer and the Institut d'Estudis Catalans award an international research prize for a mathematical monograph of expository nature. The prize-winning monographs are published in this series. Details about the prize and the Fundació Ferran Sunyer i Balaguer can be found at

`http://www.crm.es/FSBPrize/ffsb.htm`

This book has been awarded the Ferran Sunyer i Balaguer 2004 prize.

The members of the scientific commitee of the 2004 prize were:

Hyman Bass
University of Michigan

Antonio Córdoba
Universidad Autónoma de Madrid

Paul Malliavin
Université de Paris VI

Joseph Oesterlé
Université de Paris VI

Oriol Serra
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