

A

Mandelbrot–van Ness Representation: Some Related Calculations

Now we calculate the constant that appeared in the Mandelbrot–van Ness representation of fBm (see Section 1.3, Theorem 1.3.1).

Lemma A.0.1. *The following equalities hold:*

$$C_H^{(2)} := \left(\int_{\mathbb{R}_+} ((1+s)^\alpha - s^\alpha)^2 ds + \frac{1}{2H} \right)^{-1} = \frac{(2H \sin \pi H \Gamma(2H))^{1/2}}{\Gamma(1+\alpha)}.$$

Proof. Recall that the constant $C_H^{(2)}$ is chosen to normalize the fBm

$$\overline{B}_t^H = C_H^{(2)} \int_{\mathbb{R}} k_H(t, u) dW_u = C_H^{(2)} \Gamma(1+\alpha) \int_{\mathbb{R}} (I_-^\alpha \mathbf{1}_{(0,t)})(x) dW_x$$

(see Lemma 1.1.3). Therefore, the first equality is evident, since

$$\begin{aligned} \int_{\mathbb{R}} (k_H(t, u))^2 du &= \int_{-\infty}^0 ((t-x)^\alpha - (-x)^\alpha)^2 dx + \int_0^t (t-x)^{2\alpha} dx \\ &= t^{2H} \left(\int_0^\infty ((1+s)^\alpha - s^\alpha)^2 ds + \frac{1}{2H} \right). \end{aligned}$$

We obtain the second equality if we note that

$$\int_{\mathbb{R}} (I_-^\alpha \mathbf{1}_{(0,t)})(x)^2 dx = \frac{1}{2\pi} \int_{\mathbb{R}} \left(\widehat{\mathcal{F}}(I_-^\alpha \mathbf{1}_{(0,t)})(x) \right)^2 dx$$

and according to Theorem 1.1.5

$$\begin{aligned} \widehat{\mathcal{F}}(I_-^\alpha \mathbf{1}_{(0,t)})(x)(\lambda) &= \widehat{\mathbf{1}_{(0,t)}}(\lambda) |\lambda|^{-\alpha} \exp \left\{ \frac{\alpha\pi i}{2} \operatorname{sign} \lambda \right\} \\ &= \frac{e^{it\lambda} - 1}{i\lambda} |\lambda|^{-\alpha} \exp \left\{ \frac{\alpha\pi i}{2} \operatorname{sign} \lambda \right\}. \end{aligned}$$

Therefore,

$$\begin{aligned}
 \int_{\mathbb{R}} (I_{-}^{\alpha} \mathbf{1}_{(0,t)})(x)^2 dx &= \frac{1}{2\pi} \int_{\mathbb{R}} |e^{it\lambda} - 1|^2 |\lambda|^{-2\alpha-2} d\lambda \\
 &= \frac{1}{2\pi} \int_{\mathbb{R}} (1 - \cos t\lambda)^2 |\lambda|^{-2\alpha-2} d\lambda + \frac{1}{2\pi} \int_{\mathbb{R}} \sin^2 t\lambda |\lambda|^{-2\alpha-2} d\lambda \\
 &= \frac{1}{\pi} \int_0^{\infty} \frac{(1 - \cos t\lambda)^2}{\lambda^{2\alpha+2}} d\lambda + \frac{1}{\pi} \int_0^{\infty} \frac{\sin^2 t\lambda}{\lambda^{2\alpha+2}} d\lambda \\
 &= t^{2H} \left(\frac{1}{\pi} \int_0^{\infty} \frac{(1 - \cos \lambda)^2}{\lambda^{2\alpha+2}} d\lambda + \frac{1}{\pi} \int_0^{\infty} \frac{\sin^2 \lambda}{\lambda^{2\alpha+2}} d\lambda \right) = \frac{t^{2H}}{2H \sin \pi H \Gamma(2H)},
 \end{aligned}$$

whence the proof follows. \square

B

Approximation of Beta Integrals and Estimation of Kernels

These results were obtained by E.Valkeila (KMOV05).

Lemma B.0.1. *Assume that $-1 < \delta < 0$, $\beta > -1$ and $n \geq 2$. Then for $\beta \geq 0$*

$$|I(\delta, \beta) - I_n(\delta, \beta)| \leq C_1(\delta, \beta)n^{-\alpha-1}, \quad (\text{B.0.1})$$

and with $-1 < \beta < 0$ we have

$$|I(\alpha, \beta) - I_n(\delta, \beta)| \leq C_2(\delta, \beta)n^{-\alpha-\beta-1} \quad (\text{B.0.2})$$

(for the value of the constants, see the proof).

Proof. We start the proof with

$$\begin{aligned} I(\delta, \beta) - I_n(\delta, \beta) &= \int_0^{\frac{1}{n}} s^\delta (1-s)^\beta ds - n^{-\delta-1} \\ &\quad + \sum_{k=1}^{n-2} \int_{\frac{k}{n}}^{\frac{k+1}{n}} \left(s^\delta (1-s)^\beta - \left(\frac{k+1}{n} \right)^\delta \left(1 - \frac{k}{n} \right)^\beta \right) ds \\ &\quad + \int_{1-\frac{1}{n}}^1 s^\delta (1-s)^\beta ds - n^{-\beta-1}. \end{aligned}$$

We work first with the integral on $(0, 1/n)$. We have

$$\begin{aligned} \int_0^{\frac{1}{n}} s^\delta (1-s)^\beta ds - n^{-\delta-1} &= \int_0^{\frac{1}{n}} (s^\delta - n^{-\delta}) ds \\ &\quad + \int_0^{\frac{1}{n}} s^\delta \left((1-s)^\beta - 1 \right) ds; \end{aligned} \quad (\text{B.0.3})$$

here

$$0 \leq \int_0^{\frac{1}{n}} (s^\delta - n^{-\delta}) ds = -\delta/(\delta+1)n^{-\delta-1},$$

if $\beta \geq 0$, then

$$\left| \int_0^{\frac{1}{n}} s^\delta \left((1-s)^\beta - 1 \right) ds \right| \leq \int_0^{\frac{1}{n}} s^\delta ds$$

and if $\beta < 0$ and $s \leq 1/n$, then $0 \leq (1-s)^\beta - 1 \leq 2^{-\beta} - 1$. Use these estimates in (B.0.3) to obtain

$$\left| \int_0^{\frac{1}{n}} s^\delta (1-s)^\beta ds - n^{-\delta-1} \right| \leq C_1(\delta, \beta) n^{-\delta-1}. \tag{B.0.4}$$

Next, we work with the integral on $(1 - 1/n, 1)$. We have

$$\begin{aligned} \int_{1-\frac{1}{n}}^1 s^\delta (1-s)^\beta ds - n^{-\beta-1} &= \int_{1-\frac{1}{n}}^1 \left((1-s)^\beta - n^{-\beta} \right) ds \\ &+ \int_{1-\frac{1}{n}}^1 (1-s)^\beta (s^\delta - 1) ds, \end{aligned}$$

and this gives

$$\left| \int_{1-\frac{1}{n}}^1 s^\delta (1-s)^\beta ds - n^{-\beta-1} \right| \leq \frac{|\beta|}{1+\beta} n^{-\beta-1} + 2^{-\delta} n^{-\beta-1}. \tag{B.0.5}$$

We continue with the middle term. We have

$$\begin{aligned} &\sum_{k=1}^{n-2} \left(\int_{\frac{k}{n}}^{\frac{k+1}{n}} s^\delta (1-s)^\beta ds - \left(\frac{k+1}{n} \right)^\delta \left(1 - \frac{k}{n} \right)^\beta \frac{1}{n} \right) \\ &= \sum_{k=1}^{n-2} \left(\int_{\frac{k}{n}}^{\frac{k+1}{n}} \left(s^\delta - \left(\frac{k+1}{n} \right)^\delta \right) (1-s)^\beta ds \right) \\ &+ \sum_{k=1}^{n-2} \left(\int_{\frac{k}{n}}^{\frac{k+1}{n}} \left(\frac{k+1}{n} \right)^\delta \left((1-s)^\beta - \left(1 - \frac{k}{n} \right)^\beta \right) ds \right). \end{aligned} \tag{B.0.6}$$

The first term on the right-hand side of (B.0.6) is always positive, when $\delta < 0$. We use the estimate

$$s^\delta - \left((k+1)/n \right)^\delta \leq (k/n)^\delta - \left((k+1)/n \right)^\delta.$$

If $\beta \geq 0$, then $(1-s)^\beta \leq 1$ and so for the first term on the right-hand side of (B.0.6) we obtain

$$0 \leq \sum_{k=1}^{n-2} \left(\int_{k/n}^{(k+1)/n} \left(s^\delta - \left((k+1)/n \right)^\delta \right) (1-s)^\beta ds \right)$$

$$\leq n^{-\delta-1} \sum_{k=1}^{n-2} \left(k^\delta - (k+1)^\delta \right) \leq n^{-\delta-1}. \tag{B.0.7}$$

If $\beta \leq 0$ then

$$\int_{k/n}^{(k+1)/n} \left(s^\delta - ((k+1)/n)^\delta \right) (1-s)^\beta ds \leq \frac{1}{1+\beta} n^{-\delta-\beta-1} \left(k^\delta - (k+1)^\delta \right) \left((n-k)^{\beta+1} - (n-(k+1))^{\beta+1} \right) \leq n^{-\delta-\beta-1} \left(k^\delta - (k+1)^\delta \right),$$

and this gives the estimate

$$0 \leq \sum_{k=1}^{n-2} \left(\int_{k/n}^{(k+1)/n} \left(s^\alpha - ((k+1)/n)^\alpha \right) (1-s)^\beta ds \right) \leq n^{-\alpha-\beta-1}. \tag{B.0.8}$$

Finally, the second part of the middle term is

$$J_n := \sum_{k=1}^{n-2} \left(\int_{k/n}^{(k+1)/n} ((k+1)/n)^\delta \left((1-s)^\beta - (1-k/n)^\beta \right) ds \right).$$

If $\beta \geq 0$, then with calculations similar to above

$$|J_n| \leq n^{-\delta-1}, \tag{B.0.9}$$

and if $\beta < 0$, then

$$|J_n| \leq -\frac{1}{\beta} 2^\beta n^{-\alpha-\beta-1}. \tag{B.0.10}$$

Combining the bounds (B.0.3)–(B.0.7) and (B.0.9) we get $C_1(\delta, \beta)$, and combining the bounds (B.0.3)–(B.0.6), (B.0.8) and (B.0.10) we get $C_2(\delta, \beta)$. \square

Lemma B.0.2. *Put*

$$H_n := \sum_{k=0}^{n-1} \left(\left(\frac{k+1}{n} \right)^{1/4-H} \left(1 - \frac{k}{n} \right)^{3/4-H} \left(\left(\frac{k+1}{n} \right)^{2H} - \left(\frac{k}{n} \right)^{2H} \right) - 2H \left(\frac{k+1}{n} \right)^{H-3/4} \left(1 - \frac{k}{n} \right)^{3/4-H} \frac{1}{n} \right).$$

Then

$$|H_n| \leq C n^{-\min(1, \frac{1}{4}+H)}. \tag{B.0.11}$$

Proof. The proof of Lemma B.0.2 is similar to Lemma B.0.1. \square

The proof of the following lemma is obvious.

Lemma B.0.3. *Consider the expression*

$$\bar{u}_n(H) := \frac{1}{n} \sum_{k=0}^{n-1} \left(\left(\frac{k+1}{n} \right)^{2H} - \left(\frac{k}{n} \right)^{2H} \right)^2.$$

Then

$$|\bar{u}_n(H)| \leq \frac{C}{n^2}. \quad (\text{B.0.12})$$

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