
References

1. J. Ackermann. *Robust Control*. Springer-Verlag, 1993.
2. B. D. O. Anderson and J. B. Moore. *Linear Optimal Control*. Prentice Hall, Englewood Cliffs, New Jersey, 1971.
3. A. A. Andronov, A. A. Vitt, and L. S. Pontryagin. Statistische Auffassung dynamischer Systeme. *Phys. Z. Sowjetunion*, 6:1–24, 1934.
4. P. Ara and M. Mathieu. *Local Multipliers of C^* -Algebras*. Springer-Verlag, 2003.
5. W. Arendt. Resolvent positive operators. *Proc. London Math. Soc.*, 54(3):321–349, 1987.
6. L. Arnold. *Stochastische Differentialgleichungen*. R. Oldenburg Verlag, 1973.
7. L. Arnold, H. Crauel, and V. Wihstutz. Stabilization of linear systems by noise. *SIAM J. Control Optim.*, 21:451–461, 1983.
8. V. I. Arnold. *Gewöhnliche Differentialgleichungen*. Springer, 2001.
9. T. Başar and P. Bernhard. *H^∞ -Optimal Control and Related Minimax Design Problems. A Dynamic Game Approach*. Birkhäuser, Boston, 2nd edition, 1995.
10. G. P. Barker, R. D. Hill, and R. D. Haertel. On the completely positive and positive-semidefinite-preserving cones. *Linear Algebra Appl.*, 56:221–229, 1984.
11. R. H. Bartels and G. W. Stewart. Solution of the matrix equation $AX + XB = C$: Algorithm 432. *Comm. ACM*, 15:820–826, 1972.
12. P. Benner and R. Byers. An exact line search method for solving generalized continuous-time algebraic Riccati equations. *IEEE Trans. Autom. Control*, 43(1):101–107, 1998.
13. A. Berman, M. Neumann, and R. J. Stern. *Nonnegative Matrices in Dynamic Systems*. John Wiley & Sons, New York, 1989.
14. A. Berman and R. J. Plemmons. *Nonnegative Matrices in the Mathematical Sciences*. Classics in Applied Mathematics. SIAM, 1994.
15. D. Bernstein and D. C. Hyland. Optimal projection equations for reduced-order modeling, estimation and control of linear systems with multiplicative noise. *J. Optim. Th. & Appl.*, 58:387–409, 1988.
16. D. S. Bernstein. Robust static and dynamic output-feedback stabilization: Deterministic and stochastic perspectives. *IEEE Trans. Autom. Control*, AC-32(12):1076–1084, 1987.
17. J.-M. Bismut. Linear-quadratic optimal stochastic control with random coefficients. *SIAM J. Control*, 14:419–444, 1976.

18. S. K. Biswas. Robust stabilization of linear systems in the presence of Gaussian perturbation of parameters. *Optim. Contr. Appl. Meth.*, 19:271–286, 1998.
19. S. Bittanti, A. J. Laub, and J. C. Willems. *The Riccati Equation*. Communication and Control Engineering Series. Springer-Verlag, Berlin, Heidelberg, New York, 1991.
20. J. L. Bogdanoff and S. J. Citron. Experiments with an inverted pendulum subject to random parametric excitation. *J. Acoustic Soc.*, 38(9):447–452, 1965.
21. S. Boyd, L. El Ghaoui, E. Feron, and V. Balakrishnan. *Linear Matrix Inequalities in Systems and Control Theory*, volume 15 of *Studies in Applied Mathematics*. SIAM, 1994.
22. R. W. Brockett. *Finite Dimensional Linear Systems*. John Wiley & Sons, New York, 1970.
23. L. Burlando. Monotonicity of spectral radius for positive operators on ordered Banach spaces. *Arch. Math.*, 56:49–57, 1991.
24. D. Carlson and R. Hill. Generalized controllability and inertia theory. *Linear Algebra Appl.*, 15:177–187, 1976.
25. B. M. Chen. *Robust and H_∞ control*. Communications and Control Engineering Series. Springer-Verlag, 2000.
26. S. Chen, X. Li, and X. Y. Zhou. Stochastic linear quadratic regulators with indefinite control weight costs. *SIAM J. Control Optim.*, 36(5):1685–1702, 1998.
27. S. J. Cho, S.-H. Kye, and S. G. Lee. Generalized Choi maps in three-dimensional matrix algebras. *Linear Algebra Appl.*, 171:212–224, 1992.
28. M.-D. Choi. Positive linear maps on C^* -algebras. *Canadian J. Math.*, 4:520–529, 1972.
29. M.-D. Choi. Completely positive linear maps on complex matrices. *Linear Algebra Appl.*, 10:285–290, 1975.
30. M.-D. Choi. Positive semidefinite biquadratic forms. *Linear Algebra Appl.*, 4:95–100, 1975.
31. A. N. Churilov. On the solution of a quadratic matrix equation. In E. L. Tonkov, editor, *Nonlinear oscillations and control theory. No.2.*, pages 24–33. Udmurt State University, Izhevsk, 1978.
32. D. J. Clements and H. K. Wimmer. Monotonicity of the optimal cost in the discrete-time regulator problem and Schur complements. *Automatica*, 37:1779–1786, 2001.
33. E. G. Collins, Jr. and A. S. Hodel. Efficient solutions of linearly coupled Lyapunov equations. *SIAM J. Matrix. Anal. Appl.*, 18(2):291–304, 1997.
34. W. A. Coppel. Matrix quadratic equations. *Bull. Austr. Math. Soc.*, 10:377–401, 1974.
35. R. F. Curtain, editor. *Stability of Stochastic Dynamical Systems*, volume 294 of *Lecture Notes in Mathematics*. Springer-Verlag, 1972.
36. R. F. Curtain and A. J. Pritchard. *Functional analysis in modern applied mathematics*, volume 132 of *Mathematics in Science and Engineering*. Academic Press, London, New York, 1977.
37. G. Da Prato. Direct solution of a Riccati equation arising in stochastic control theory. *Applied Mathematics and Optimization*, 11:191–208, 1984.
38. G. Da Prato and J. Zabczyk. *Stochastic Equations in Infinite Dimensions*, volume 45 of *Encyclopedia of Mathematics and Its Applications*. Cambridge University Press, 1992.

39. T. Damm. Generalized Riccati equations occurring in robust stochastic control. In V. Zakharov, editor, *Proceedings of the 11th IFAC Workshop, Saint Petersburg, Russia, 3-6 July 2000*. Pergamon Press, 2000.
40. T. Damm. State-feedback H^∞ -control of stochastic linear systems. In *Third NICONET Workshop on Numerical Software in Control Engineering*, pages 45–50, Louvain-la-Neuve, Belgium, 2001.
41. T. Damm. Minimal representations of inverted Sylvester and Lyapunov operators. *Linear Algebra Appl.*, 363:35–41, 2002.
42. T. Damm. State-feedback H^∞ -type control of linear systems with time-varying parameter uncertainty. *Linear Algebra Appl.*, 351–352:185–210, 2002.
43. T. Damm. A car-steering problem with random adhesion coefficient. *PAMM Proc. Appl. Math. Mech.*, 2:83–84, 2003.
44. T. Damm. Stability of linear systems and positive semigroups of symmetric matrices. In L. Benvenuti, A. D. Santis, and L. Farina, editors, *Positive Systems*, volume 294 of *Lecture Notes in Control and Information Sciences*, pages 207–214. Springer-Verlag, 2003.
45. T. Damm and D. Hinrichsen. Matrix (in)equalities for linear stochastic systems. In *Proceedings of MTNS-98*, Padova, Italy, 1998. Il Poligrafio.
46. T. Damm and D. Hinrichsen. On a rational matrix equation occurring in stochastic control. In *Proceedings of the 5th European Control Conference 1999, Karlsruhe*, pages DM–2, Karlsruhe, 1999.
47. T. Damm and D. Hinrichsen. On the parameter dependence of a class of rational matrix equations occurring in stochastic optimal control. In *Proceedings of MTNS-2000*, page IS19A, Perpignan, France, 2000.
48. T. Damm and D. Hinrichsen. Newton’s method for a rational matrix equation occurring in stochastic control. *Linear Algebra Appl.*, 332–334:81–109, 2001.
49. T. Damm and D. Hinrichsen. Newton’s method for concave operators with resolvent positive derivatives in ordered Banach spaces. *Linear Algebra Appl.*, 363:43–64, 2003.
50. B. N. Datta. Stability and inertia. *Linear Algebra Appl.*, 302–303:563–600, 1999.
51. J. de Pillis. Linear transformations which preserve Hermitian and positive semidefinite operators. *Pacific J. Math.*, 23(1):129–137, 1967.
52. C. E. de Souza and M. D. Fragoso. On the existence of maximal solutions for generalized algebraic Riccati equations arising in stochastic control. *Systems & Control Letters*, 14:233–239, 1990.
53. E. de Souza and S. Bhattacharyya. Controllability, observability and the solution of $AX - XB = C$. *Linear Algebra Appl.*, 39:167–188, 1981.
54. J. W. Demmel. *Applied Numerical Linear Algebra*. SIAM, Philadelphia, 1997.
55. J. Dieudonné. *Foundations of Modern Analysis*, volume 10-I of *Pure and Applied Mathematics*. Academic Press, New York, 1969.
56. D. Z. Djoković. Characterization of Hermitian and skew-Hermitian maps between matrix algebras. *Linear Algebra Appl.*, 12:165–170, 1975.
57. V. Drăgan, A. Halanay, and A. Stoica. An LMI solution to a disturbance attenuation problem with state feedback for stochastic systems. *Rev. Roum. Sci. Tech. Elektrotech. Energ.*, 41(4):513–519, 1996.
58. V. Drăgan, A. Halanay, and A. Stoica. A small gain theorem for linear stochastic systems. *Systems & Control Letters*, 30:243–251, 1997.

59. V. Drăgan, T. Morozan, and A. Halanay. Optimal stabilizing compensator for linear systems with state dependent noise. *Stochastic Analysis and Application*, 10:557–572, 1992.
60. F. Dullerud, G. E.; Paganini. *A course in robust control theory*, volume 36 of *Texts in Applied Mathematics*. Springer-Verlag, New York, 2000.
61. A. El Bouhtouri, D. Hinrichsen, and A. J. Pritchard. H^∞ type control for discrete-time stochastic systems. *Int. J. Robust & Nonlinear Control*, 9(13):923–948, 1999.
62. A. El Bouhtouri, D. Hinrichsen, and A. J. Pritchard. On the disturbance attenuation problem for a wide class of time invariant linear stochastic systems. *Stochastics and Stochastics Reports*, 65:255–297, 1999.
63. A. El Bouhtouri and A. J. Pritchard. A Riccati equation approach to maximizing the stability radius of a linear system by state feedback under structured stochastic Lipschitzian perturbations. *Systems & Control Letters*, 21:475–484, 1993.
64. L. El Ghaoui. State-feedback control of systems with multiplicative noise via linear matrix inequalities. *Systems & Control Letters*, 24(3):223–228, 1995.
65. L. Elsner. Monotonie und Randspektrum bei vollstetigen Operatoren. *Arch. Ration. Mech. Anal.*, 36:356–365, 1970.
66. L. Elsner. Quasimonotonie und Ungleichungen in halbgeordneten Räumen. *Linear Algebra Appl.*, 8:249–261, 1974.
67. M. Fiedler and V. Pták. On matrices with nonpositive off-diagonal elements and positive principal minors. *Czech. Math.*, 12:382–400, 1962.
68. A. Fischer, D. Hinrichsen, and N. K. Son. Stability radii of Metzler operators. *Vietnam J. Math*, 26:147–163, 1998.
69. M. D. Fragoso, O. L. V. Costa, and C. E. de Souza. A new approach to linearly perturbed Riccati equations in stochastic control. *Applied Mathematics and Optimization*, 37:99–126, 1998.
70. B. A. Francis. *A course in H_∞ control theory*. Number 88 in Lecture Notes in Control and Information Sciences. Springer-Verlag, Berlin-Heidelberg-New York, 1987.
71. G. Freiling and V. Ionescu. Monotonicity and convexity properties of matrix Riccati equations. *IMA J. Math. Control Inf.*, 18(1):61–72, 2001.
72. G. Freiling, G. Jank, and H. Abou-Kandil. Generalized Riccati difference and differential equations. *Linear Algebra Appl.*, 241-243:291–303, 1996.
73. A. Friedman. *Stochastic Differential Equations and Applications*. Number 28 in Probability and mathematical statistics. Academic Press, New York, 1975.
74. G. Frobenius. Über Matrizen aus positiven Elementen. *Sitzungsberichte der Königl. Preuss. Akad. Wiss*, pages 471–476, 1908.
75. P. Gahinet and P. Apkarian. A linear matrix inequality approach to H_∞ control. *Int. J. Robust & Nonlinear Control*, 4:421–448, 1994.
76. P. Gahinet and A. J. Laub. Numerically reliable computation of optimal performance in singular H_∞ control. *SIAM J. Control Optim.*, 35(5):1690–1710, 1997.
77. Z. Gajić and M. T. J. Qureshi. *Lyapunov Matrix Equation in System Stability and Control*, volume 195 of *Mathematics in Science and Engineering*. Academic Press, San Diego, California, 1995.
78. F. R. Gantmacher. *Matrizentheorie*. Springer, 1986.
79. Z. Y. Gao and N. U. Ahmed. Stabilizability of certain stochastic systems. *Int. J. Systems Sci.*, 17(8):1175–1185, 1986.

80. T. C. Gard. *Introduction to Stochastic Differential Equations*, volume 114 of *Monographs and Textbooks in Pure and Applied Mathematics*. Marcel Dekker, 1988.
81. I. I. Gikhman. On the theory of differential equations of stochastic processes. I, II. *Am. Math. Soc., Transl.*, II. Ser. 1:111–137, 139–161, 1955.
82. I. I. Gikhman and A. V. Skorokhod. *Stochastic Differential Equations*. Springer-Verlag, 1972.
83. S. K. Godunov. *Modern Aspects of Linear Algebra*, volume 175 of *Translations of Mathematical Monographs*. American Mathematical Society, Providence, Rhode Island, 1998.
84. I. Gohberg, P. Lancaster, and L. Rodman. On the Hermitian solutions of the symmetric algebraic Riccati equation. *SIAM J. Control Optim.*, 24:1323–1334, 1986.
85. G. H. Golub, S. Nash, and C. F. Van Loan. A Hessenberg-Schur method for the problem $AX + XB = C$. *IEEE Trans. Autom. Control*, AC-24:909–913, 1979.
86. G. H. Golub and C. F. van Loan. *Matrix Computations*, volume 3 of *Johns Hopkins Series in the Mathematical Sciences*. Johns Hopkins University Press, Baltimore, Maryland, 1990.
87. M. Green and D. J. N. Limebeer. *Linear Robust Control*. Prentice-Hall, Englewood Cliffs, New Jersey, 1995.
88. A. Greenbaum. *Iterative Methods for Solving Linear Systems*, volume 17 of *Frontiers in Applied Mathematics*. SIAM, Philadelphia, 1997.
89. R. Griesbaum. *Zur Stabilität dynamischer Systeme mit stochastischer Parametererregung*. PhD thesis, Fakultät für Maschinenbau, Universität Karlsruhe, 1999.
90. P. Gritzmann, V. Klee, and B.-S. Tam. Cross-positive matrices revisited. *Linear Algebra Appl.*, 223/224:285–305, 1995.
91. C.-H. Guo. Newton's method for discrete algebraic Riccati equations when the closed-loop matrix has eigenvalues on the unit circle. *SIAM J. Matrix. Anal. Appl.*, 20(2):279–294, 1998.
92. C.-H. Guo. Iterative solution of a matrix Riccati equation arising in stochastic control. Preprint, Department of Mathematics and Statistics, University of Regina, 2000.
93. C.-H. Guo. Nonsymmetric algebraic Riccati equations and Wiener-Hopf factorization of M -matrices. *SIAM J. Matrix. Anal. Appl.*, 23(1):225–242, 2001.
94. C.-H. Guo and P. Lancaster. Analysis and modification of Newton's method for algebraic Riccati equations. *Math. Comp.*, 67(223):1089–1105, 1998.
95. S. J. Hammarling. Numerical solution of the stable, non-negative definite Lyapunov equation. *IMA J. Numer. Anal.*, 2:303–323, 1982.
96. B. Hassibi, A. H. Sayed, and T. Kailath. *Indefinite-quadratic estimation and control: A unified approach to H^2 and H^∞ theories*, volume 15 of *Studies in Applied Mathematics*. SIAM, 1999.
97. U. G. Haussmann. Optimal stationary control with state and control dependent noise. *SIAM J. Control*, 9(2):713–739, 1971.
98. U. G. Haussmann. Stabilization of linear systems with multiplicative noise. In R. F. Curtain, editor, *Stability of Stochastic Dynamical Systems*, volume 294 of *Lecture Notes in Mathematics*, pages 125–130. Springer-Verlag, July 1972.
99. M. L. J. Hautus. Controllability and observability conditions of linear autonomous systems. *Indag. Math.*, 31:443–448, 1969.

100. M. L. J. Hautus. Operator substitution. *Linear Algebra Appl.*, 205-206:713–739, 1994.
101. U. Helmke and J. B. Moore. L^2 sensitivity minimization of linear system representations via gradient flows. *J. Math. Syst. Estim. Control*, 5(1):79–98, 1995.
102. G. A. Hewer. An iterative technique for the computation of the steady state gains for the discrete optimal regulator. *IEEE Trans. Autom. Control*, AC-16:382–384, 1971.
103. G. A. Hewer. Existence theorems for positive semidefinite and sign indefinite stabilizing solutions of H_∞ Riccati equations. *SIAM J. Control Optim.*, 31:16–29, 1993.
104. R. D. Hill. Linear transformations which preserve Hermitian matrices. *Linear Algebra Appl.*, 6:257–262, 1973.
105. R. D. Hill and S. R. Waters. On the cone of positive definite matrices. *Linear Algebra Appl.*, 90:81–88, 1987.
106. D. Hinrichsen and A. J. Pritchard. Stability radii with stochastic uncertainty and their optimization by output feedback. *SIAM J. Control Optim.*, 34:1972–1998, 1996.
107. D. Hinrichsen and A. J. Pritchard. Stochastic H_∞ . *SIAM J. Control Optim.*, 36(5):1504–1538, 1998.
108. D. Hinrichsen and A. J. Pritchard. *Mathematical Systems Theory*, chapter 1: Mathematical Models. Manuscript, Bremen, 2001.
109. D. Hinrichsen and N. K. Son. μ -analysis and robust stability of positive linear systems. *Appl. Math. Comput.*, 8(2):253–268, 1998.
110. M. Hochbruck and G. Starke. Preconditioned Krylov subspace methods for Lyapunov matrix equations. *SIAM J. Matrix. Anal. Appl.*, 16(1):156 – 171, 1994. see also: IPS Research Report 92–17, ETH Zürich, Switzerland (1992).
111. A. Hochhaus. *Existenz-, Konvergenz- und Vergleichssätze für verallgemeinerte Riccatische Matrix-Gleichungen*. PhD thesis, Fakultät für Naturwissenschaften, Universität Duisburg, 2002.
112. R. A. Horn and C. R. Johnson. *Matrix Analysis*. Cambridge University Press, Cambridge, Massachusetts, 1985.
113. R. A. Horn and C. R. Johnson. *Topics in Matrix Analysis*. Cambridge University Press, Cambridge, 1991.
114. M. S. Howe. The mean square stability of an inverted pendulum subject to random parametric excitation. *J. Sound Vibration*, 32(3):407–421, 1974.
115. N. Ikeda and S. Watanabe. *Stochastic Differential Equations and Diffusions Processes*. North Holland, 1981.
116. V. Ionescu, C. Oara, and M. Weiss. *Generalized Riccati Theory and Robust Control: A Popov Function Approach*. John Wiley & Sons, Chichester, 1999.
117. K. Ito. On a stochastic integral equation. *Proc. Japan Acad.*, 22(1–4):32–35, 1946.
118. K. Ito. On stochastic differential equations. *Mem. Am. Math. Soc.*, 4, 1951.
119. R. E. Kalman. Contributions to the theory of optimal control. *Bol. Soc. Matem. Mexico*, 5:102–119, 1960.
120. R. E. Kalman. Mathematical description of linear dynamical systems. *SIAM J. Control*, 1:152–192, 1963.
121. R. E. Kalman, P. L. Falb, and M. A. Arbib. *Topics in mathematical system theory*. McGraw-Hill, New York, 1969.

122. L. V. Kantorovich. Functional analysis and applied mathematics. *Usp. Mat. Nauk*, 3(6):89–185, 1948.
123. L. V. Kantorovich and G. P. Akilov. *Functional Analysis in Normed Spaces*. Pergamon Press, New York, 1964. Translated by D. E. Brown, edited by A. P. Robertson.
124. J. Kao and V. Wihstutz. Stabilization of companion form systems by mean square noise. *Stochastics Stochastics Rep.*, 49:1–25, 1994.
125. I. Karatzas and S. E. Shreve. *Brownian Motion and Stochastic Calculus*. 2nd ed., volume 113 of *Graduate Texts in Mathematics*. Springer-Verlag, New York, 1991.
126. I. Y. Kats and N. N. Krasovskij. On the stability of systems with random parameters. *J. Appl. Math. Mech.*, 24:1225–1246, 1961.
127. V. L. Kharitonov. Asymptotic stability of an equilibrium position of a family of systems of linear differential equations. *J. Diff. Eqns.*, 11:2086–2088, 1978.
128. V. L. Kharitonov. Distribution of the roots of the characteristic polynomial of an autonomous system. *Autom. Remote Control*, 42(5):589–593, 1981.
129. V. L. Kharitonov. Robust stability analysis of time delay systems: A survey. In *Commande et Structure des Systèmes*, pages 1–12, Nantes, 1998. Conference IFAC.
130. R. Z. Khasminskij. *Stochastic Stability of Differential Equations*. Sijthoff & Noordhoff, Alphen aan den Rijn, NL, 1980.
131. D. L. Kleinman. On an iterative technique for Riccati equation computations. *IEEE Trans. Autom. Control*, AC-13:114–115, 1968.
132. D. L. Kleinman. On the stability of linear stochastic systems. *IEEE Trans. Autom. Control*, AC-14:429–430, 1969.
133. D. L. Kleinman. Numerical solution of the state dependent noise problem. *IEEE Trans. Autom. Control*, AC-21:419–420, 1976.
134. P. E. Kloeden and E. Platen. *Numerical Solution of Stochastic Differential Equations*. Springer-Verlag, Berlin, 1995.
135. H.-W. Knobloch and H. Kwakernaak. *Lineare Kontrolltheorie*. Springer-Verlag, Berlin, 1985.
136. A. N. Kolmogorov. Über die analytischen Methoden in der Wahrscheinlichkeit-srechnung. *Mathematische Annalen*, 104:415–458, 1931.
137. M. A. Krasnosel'skii, G. M. Vainikko, P. P. Zabreiko, Y. B. Rutitskii, and V. Y. Stetsenko. *Approximate Solution of Operator Equations*. Wolters-Noordhoff, Groningen, 1972.
138. M. A. Krasnosel'skij. *Positive Solutions of Operator Equations*. P. Noordhoff Ltd., Groningen, The Netherlands, 1964.
139. M. A. Krasnosel'skij, J. A. Lifshits, and A. V. Sobolev. *Positive Linear Systems - The Method of Positive Operators*, volume 5 of *Sigma Series in Applied Mathematics*. Heldermann Verlag, Berlin, 1989.
140. M. G. Krein and M. A. Rutman. Linear operators leaving invariant a cone in a Banach space. *Amer. Math. Soc. Transl.*, 26:199–325, 1950.
141. N. V. Krylov. *Controlled Diffusion Processes*, volume 14 of *Applications of Mathematics*. Springer-Verlag, New York, 1980.
142. N. V. Krylov. *Introduction to the Theory of Diffusion Processes*, volume 142 of *Translations of Mathematical Monographs*. American Mathematical Society, 1995.
143. H. J. Kushner. *Stochastic stability and control*. Academic Press, New York, 1967.

144. H. Kwakernaak and R. Sivan. *Linear Optimal Control Systems*. John Wiley & Sons, New York, 1972.
145. P. Lancaster and L. Rodman. *Algebraic Riccati Equations*. Oxford, 1995.
146. C.-K. Li and H. J. Woerdeman. Special classes of positive and completely positive maps. *Linear Algebra Appl.*, 255:247–258, 1997.
147. G. Lindblad. On the generators of quantum dynamical semigroups. *Commun. Math. Phys.*, 1:219–224, 1976.
148. D. G. Luenberger. *Optimization by Vector Space Methods*. John Wiley & Sons, New York, 1969.
149. I. Marek. Frobenius theory of positive operators: Comparison theorems and applications. *SIAM J. Appl. Math.*, 19:607–628, 1970.
150. P. J. McLane. Optimal stochastic control of linear systems with state- and control-dependent disturbances. *IEEE Trans. Autom. Control*, AC-16(6):793–798, 1971.
151. V. Mehrmann. *The Autonomous Linear Quadratic Control Problem, Theory and Numerical Solution*. Number 163 in Lecture Notes in Control and Information Sciences. Springer-Verlag, Heidelberg, July 1991.
152. B. P. Molinari. The time invariant linear quadratic optimal control problem. *Automatica*, 13:347–357, 1977.
153. T. Morozan. Stabilization of some stochastic discrete-time control systems. *Stochastic Analysis and Application*, 1:89–116, 1983.
154. T. Morozan. Parametrized Riccati equations associated to input-output operators for time-varying stochastic differential equations with state-dependent noise. Technical Report 37, Institute of Mathematics of the Romanian Academy, 1995.
155. R. Nabben. A characterization of M-matrices. Preprint 95-002, SFB 343, Universität Bielefeld, 1995.
156. B. Oksendal. *Stochastic Differential Equations*. Springer-Verlag, 5th edition, 1998.
157. A. Ostrowski and H. Schneider. Some theorems on the inertia of general matrices. *J. Math. Anal. Appl.*, 4:72–84, 1962.
158. A. M. Ostrowski. Über die Determinanten mit überwiegender Hauptdiagonale. *Comm. Math. Helv.*, 10:69–96, 1937.
159. D. Ottl and C. Römmich. Schwingungen von Autorädern infolge mechanisch unrunder Reifen. *Automobiltechnische Zeitschrift*, 98(6):351–357, 1996.
160. D. V. Oulette. Schur complements and statistics. *Linear Algebra Appl.*, 36:187–295, 1981.
161. T. Penzl. Numerical solution of generalized Lyapunov equations. *Adv. Comput. Math.*, 8(1–2):33–48, 1998.
162. O. Perron. Zur Theorie der Übermatrizen. *Math. Ann.*, 64:248–263, 1907.
163. I. R. Petersen, V. A. Ugrinovskii, and A. V. Savkin. *Robust Control Design Using H^∞ -Methods*. Springer-Verlag, London, 2000.
164. Y. A. Phillis. Optimal stabilization of stochastic systems. *J. Math. Anal. Appl.*, 94:489–500, 1983.
165. H. Radjavi and P. Rosenthal. *Simultaneous triangularization*. Springer-Verlag, New York, 2000.
166. A. C. M. Ran and R. Vreugdenhil. Existence and comparison theorems for algebraic Riccati equations for continuous- and discrete-time systems. *Linear Algebra Appl.*, 99:63–83, 1988.

167. W. T. Reid. *Riccati Differential Equations*. Academic Press, New York, 1972.
168. M. Reurings. *Symmetric Matrix Equations*. PhD thesis, Vrije Universiteit Amsterdam, 2003.
169. S. Richter, L. D. Davis, and E. G. Collins, Jr. Efficient computation of the solutions to modified Lyapunov equations. *SIAM J. Matrix. Anal. Appl.*, 14(2):420–431, April 1993.
170. H. H. Rosenbrock. *State Space and Multivariable Theory*. Nelson-Wiley, 1970.
171. P. Sagirow. *Stochastic Methods in the Dynamics of Satellites*. Number 57 in Courses and lectures: International Centre for Mechanical Sciences. Springer-Verlag, Wien, New York, 1970.
172. A. A. Sagle and R. E. Walde. *Introduction to Lie Groups and Lie Algebras*, volume 51 of *Pure and Applied Mathematics*. Academic Press, New York–London, 1973.
173. J. C. Samuels and A. C. Eringen. On stochastic linear systems. *J. Math. Phys.*, 38:83–103, 1959.
174. N. R. Sandell. On Newton’s method for Riccati equation solution. *IEEE Trans. Autom. Control*, AC-19:254–255, 1974.
175. T. Sasagawa. LP-stabilization problem for linear stochastic control systems with multiplicative noise. *J. Optim. Th. & Appl.*, 61(3):451–471, 1989.
176. T. Sasagawa and J. L. Willems. Parametrization method for calculating exact stability bounds of stochastic linear systems with multiplicative noise. *Automatica*, 32(12):1741–1747, 1996.
177. H. H. Schaefer. *Topological Vector Spaces*. Springer-Verlag, Berlin, Heidelberg, New York, 1971.
178. C. W. Scherer. *The Riccati Inequality and State-Space H_∞ -Optimal Control*. PhD thesis, Mathematical Institute, University of Würzburg, 1990.
179. C. W. Scherer. The state feedback H_∞ -problem at optimality. *Automatica*, 30:293–305, 1994.
180. H. Schneider. Positive operators and an inertia theorem. *Numer. Math.*, 7:11–17, 1965.
181. H. Schneider and M. Vidyasagar. Cross-positive matrices. *SIAM J. Numer. Anal.*, 7(4):508–519, 1970.
182. M. A. Shayman. Geometry of the algebraic Riccati equation, Part I. *SIAM J. Control Optim.*, 21:375–394, 1983.
183. M. A. Shayman. Geometry of the algebraic Riccati equation, Part II. *SIAM J. Control Optim.*, 21:395–409, 1983.
184. E. D. Sontag. *Mathematical Control Theory, Deterministic Finite Dimensional Systems*. Springer-Verlag, New York, 2nd edition, 1998.
185. R. J. Stern and H. Wolkowitz. Exponential nonnegativity on the ice-cream cone. *SIAM J. Matrix. Anal. Appl.*, 12:755–778, 1994.
186. G. W. Stewart and J. Sun. *Matrix Perturbation Theory*. Computer Science and Scientific Computing. Academic Press, Boston, 1990.
187. W. F. Stinespring. Positive functions on C^* -algebras. *Proc. Amer. Math. Soc.*, 6:211–216, 1955.
188. R. L. Stratonovič. A new form of representing stochastic integrals and equations. *Vestnik Moskov. Univ.*, Ser. I 19(1):3–12, 1964.
189. W.-S. Tang. On positive linear maps between matrix algebras. *Linear Algebra Appl.*, 79:45–51, 1986.

190. G. Tessitore. Some remarks on the Riccati equation arising in an optimal control problem with state- and control- dependent noise. *SIAM J. Control Optim.*, 30(3):717–744, May 1992.
191. G. Tessitore. On the mean-square stabilizability of a linear stochastic differential equation. In J.-P. Zolesio, editor, *Boundary Control and Variation*, volume 163 of *Lect. Notes Pure Appl. Math.*, pages 383–400, New York, June 1994. 5th Working Conference held in Sophia Antipolis, France, Marcel Dekker.
192. H. L. Trentelman, A. A. Stoorvogel, and M. L. J. Hautus. *Control Theory for Linear Systems*. Springer-Verlag, London, 2001.
193. M. Turelli. Random environments and stochastic calculus. *Theor. Popul. Biol.*, 12:140–178, 1977.
194. V. A. Ugrinovskii. Robust H^∞ -control in the presence of stochastic uncertainty. *Internat. J. Control*, 71(2):219–237, 1998.
195. V. A. Ugrinovskii and I. R. Petersen. Absolute stabilization and minimax optimal control of uncertain systems with stochastic uncertainty. *SIAM J. Control Optim.*, 37(4):1089–1122, 1999.
196. J. S. Vandergraft. Newton’s method for convex operators in partially ordered spaces. *SIAM J. Numer. Anal.*, 4(3):406–432, 1967.
197. J. S. Vandergraft. Spectral properties of matrices which have invariant cones. *SIAM J. Appl. Math.*, 16(6):1208–1222, 1968.
198. R. S. Varga. *Matrix Iterative Analysis*. Prentice Hall, Englewood Cliffs, New Jersey, 1962.
199. R. S. Varga. On recurring theorems on diagonal dominance. *Linear Algebra Appl.*, 13:1–9, 1976.
200. W. J. Vetter. Vector structures and solutions of linear matrix equations. *Linear Algebra Appl.*, 10:181–188, 1975.
201. J. C. Willems. Least squares optimal control and the algebraic Riccati equation. *IEEE Trans. Autom. Control*, AC-16:621–634, 1971.
202. J. L. Willems. Moment stability of linear white noise and coloured noise systems. In B. e. a. Clarkson, editor, *Stoch. Probl. in Dyn., Symp. Univ. Southampton 1976*, pages 67–89, 1977.
203. J. L. Willems and D. Aeyels. Moment stability of linear stochastic systems with solvable Lie algebras. *IEEE Trans. Autom. Control*, AC-21:285, 1976.
204. J. L. Willems and J. C. Willems. Feedback stabilizability for stochastic systems with state and control depending noise. *Automatica*, 12:277–283, 1976.
205. J. L. Willems and J. C. Willems. Robust stabilization of uncertain systems. *SIAM J. Control Optim.*, 21:352–374, 1983.
206. H. K. Wimmer. Inertia theorems for matrices, controllability and linear vibration. *Linear Algebra Appl.*, 8:337–343, 1974.
207. H. K. Wimmer. On the algebraic Riccati equation. *Bull. Austral. Math. Soc.*, 14:457–461, 1976.
208. H. K. Wimmer. Monotonicity of maximal solutions of algebraic Riccati equations. *Systems & Control Letters*, 5:317–319, 1985.
209. H. K. Wimmer. Linear matrix equations, controllability and observability, and the rank of solutions. *SIAM J. Matrix. Anal. Appl.*, 9:570–578, 1988.
210. H. K. Wimmer. Geometry of the discrete-time algebraic Riccati equation. *J. Math. Syst. Estim. Control*, 2(1):123–132, 1992.
211. W. M. Wonham. Optimal stationary control of a linear system with state-dependent noise. *SIAM J. Control*, 5(3):486–500, 1967.

212. W. M. Wonham. On a matrix Riccati equation of stochastic control. *SIAM J. Control*, 6:681–697, 1968.
213. W. M. Wonham. Random differential equations in control theory. In A. T. Bharucha-Reid, editor, *Probab. Methods Appl. Math.*, volume 2, pages 131–212, New York - London, 1970. Academic Press.
214. W. M. Wonham. *Linear Multivariable Control: A Geometric Approach*. Springer-Verlag, Heidelberg, 2nd edition, 1979.
215. S. L. Woronowicz. Positive linear maps of low dimensional matrix algebras. *Rep. Math. Phys.*, 10:165–183, 1976.
216. V. A. Yakubovich. A frequency theorem in control theory. *Siberian Mathematical Journal*, 14:265–289, 1973.
217. W.-Y. Yan, J. B. Moore, and U. Helmke. Recursive algorithms for solving a class of nonlinear matrix equations with applications to certain sensitivity optimization problems. *SIAM J. Control Optim.*, 32:1559–1576, 1994.
218. J. Yong and X. Y. Zhou. *Stochastic Controls*, volume 43 of *Applications of Mathematics*. Springer, New York, 1999.
219. G. Zames. Feedback and optimal sensitivity: Model reference transformations, multiplicative seminorms, and approximate inverses. *IEEE Trans. Autom. Control*, AC-26:301–320, 1981.
220. K. Zhou, J. C. Doyle, and K. Glover. *Robust and Optimal Control*. Prentice Hall, New Jersey, 1995.
221. K. Zhou and P. P. Khargonekar. An algebraic Riccati equation approach to H^∞ optimization. *Systems & Control Letters*, 11(2):85–91, 1988.

Index

- Bounded Real Lemma, 50
- bounded uncertainty, 19, 56
- completely positive operator, 73, 89, 94, 117
- concavity, 104
- constraint (definite/indefinite), 56, 124
- controllability, 24, 151
- convex cone, 61
- detectability, 29, 65, 94
 - anti-, 30
- disturbance attenuation, 33, 35, 38, 50, 158, 171, 176
- duality transformation, 132
- expectation, 1
- extremal, 62
- Frobenius inner product, 62, 181
- Gâteaux differentiability, 104
- H^∞ -control, 48, 51, 56
- Hermitian-preserving, 71
- inertia, 181
- Itô
 - formula, 6
 - integral, 3
 - process, 4
- Kronecker product, 69
- Loewner ordering, 181
- LQ-control, 43, 146, 159
- Lyapunov
 - function, 21, 27
 - operator, 13, 23, 63, 75, 85
- M-matrix, 63, 119
- Newton's method, 106, 162
 - double steps, 113, 169
 - modified, 110
- observability, 24
- order interval, 61
- ordering, 61
- perturbation operator, 48
- positive operator, 13, 62
- regular splitting, 67
- regular system, 53, 133
- regularization, 177
- resolvent positive operator, 62
- Riccati
 - equation, 55, 145, 155
 - dual, 131, 170
 - non-symmetric, 118
 - standard, 120, 130, 164
 - inequality, 27, 53
 - coupled pair, 59
 - dual, 171
 - operator, 48, 134
 - dual, 138, 155, 167, 175
- Schur-complement, 54, 181

- spectral
 - abscissa, 63
 - radius, 63
- stability, 10
 - mean-square, 12, 13
 - second moment, 12
 - stochastic, 11
- stabilizability, 22
- stabilizing
 - matrix, 136, 164
 - solution, 107, 131, 145, 162
- stable
 - equation, 11
 - equilibrium, 10
 - internally/externally, 47
 - matrix, 63
 - operator, 66, 106
- Stein operator, 63, 76, 85
- stochastic
 - differential equation, 5
 - process, 1
- Stratonovich
 - integral, 4
 - interpretation, 4, 7, 10, 17, 18, 21, 27
- Sylvester operator, 98
- white noise, 2
- Wiener process, 2
- Z-matrix, 63

Notation

Sets, matrices and linear operators

\mathbb{N}	natural numbers $\{0, 1, 2, \dots\}$
\mathbb{R}, \mathbb{C}	field of real, complex numbers
\mathbb{K}	\mathbb{R} or \mathbb{C}
$\operatorname{Re} z$	real part of a complex number z
$\operatorname{Im} z$	imaginary part of a complex number z
i	imaginary unit or index, depending on context
$\mathbb{K}^{m \times n}$	vector space of matrices with m rows and n columns
\mathbb{K}^m	equal to $\mathbb{K}^{m \times 1}$
\bar{A}	complex conjugate of a matrix (or a number) A
A^T	transpose of a matrix A over \mathbb{K}
A^*	conjugate transpose of a matrix A over \mathbb{K}
\mathcal{H}^n	ordered Hilbert space of $n \times n$ Hermitian matrices over \mathbb{K}
\mathcal{H}_+^n	cone of positive semidefinite matrices in \mathcal{H}^n
\mathcal{H}_-^n	equal to $-\mathcal{H}_+^n$
$\mathcal{B}, \mathcal{B}_i$	basis of \mathcal{H}^n (see Section 3.4)
$>, \geq, <, \leq$	order relations in \mathbb{R} , or in ordered vector spaces
I_m	$m \times m$ unit matrix
I	unit matrix, whose dimension is clear by context
$e_i^{(m)}$	i -th unit vector in \mathbb{K}^m
$E_{ij}^{(mn)}$	equal to $e_i^{(m)}(e_j^{(n)})^T$
$(I_{pq} \otimes T)(E^{(mn)})$	see equation (3.2)
Ker	kernel of a matrix or an operator
im	image of a matrix or an operator
rk	rank of a matrix or an operator
$\sigma(T)$	spectrum of an operator or a matrix T
$\rho(T)$	spectral radius of T , equal to $\max\{ \lambda \mid \lambda \in \sigma(T)\}$
$\beta(T)$	spectral bound of T , equal to $\max\{\operatorname{Re}(\lambda) \mid \lambda \in \sigma(T)\}$
trace	trace of a matrix
$\langle X, Y \rangle$	equal to trace XY for $X, Y \in \mathcal{H}^n$
\det	determinant
In	inertia (see appendix)
$\mathcal{S}(M/Q)$	Schur-complement (see appendix)
vec	rearranges $m \times n$ -matrix in mn -vector (see Def. 3.3.1)
\otimes	Kronecker product (see Def. 3.3.1)
\mathcal{L}_A	Lyapunov operator $\mathcal{L}_A : X \mapsto A^*X + XA$
Π_{A_0}	the operator $\Pi_{A_0} : X \mapsto \sum_{j=1}^N A_0^{j*} X A_0^j$, for given A_0^1, \dots, A_0^N .
\mathcal{S}_A	Stein operator $\mathcal{S}_A : X \mapsto A^*XA - X$
$\mathcal{S}_{A,B}$	Sylvester operator $\mathcal{S}_{A,B} : X \mapsto AX - XB$
\mathbb{L}	perturbation operator (see Section 2.2)

Stochastic analysis (see Section 1.1)

$(\Omega, \mathcal{F}, \mu)$	probability space
$L^2(\Omega, \mathbb{K}^k)$	Hilbert space of square integrable k -dimensional random variables
w	(normed) Wiener process
\mathcal{E}	expectation
$(\mathcal{F}_t)_{t \in \mathbb{R}_+}$	increasing sequence of σ -algebras
L_w^2	L^2 -space of non-anticipating processes (with respect to \mathcal{F}_t)
C_w	almost surely continuous processes in L_w^2

Banach spaces and nonlinear operators

int, cl	topological interior, closure of a set
$\mathcal{B}(x_0, \varepsilon)$	ball with center x_0 and radius ε
X^*	dual space of a Banach space X
$\langle x, v \rangle$	duality product of $x \in X$ and $v \in X^*$, equal to $v(x)$
$T^* : X^* \rightarrow X^*$	adjoint of a linear operator $T : X \rightarrow X$
C^*	dual cone of a cone in a Banach space (see Section 3.1)
$[x, y],]x, y[$	closed, open order interval, respectively (see Section 3.1)
$f : X \rightarrow X$	nonlinear mapping on a Banach space X
$\text{dom } f$	domain of f
f'_x	derivative of f at x (see Section 4.1)
$\mathcal{R} : \mathcal{H}^n \rightarrow \mathcal{H}^n$	Riccati operator (see Section 5.1)
$\mathcal{G} : \mathcal{H}^n \rightarrow \mathcal{H}^n$	dual Riccati operator (see Section 5.1.6)
$\text{dom}_+, \text{dom}_\pm$	target sets (see Sections 5.1.1 and 5.1.2)