

Index of Notations

Structures of Spaces

- \mathcal{U} : arbitrary real-generated structure on a set, page 1
- \mathcal{C} : convergence structure on a set, page 15
- \mathcal{M} : metric structure on a set, page 10
- \mathcal{N} : proximity structure on a set, page 16
- \mathcal{T} : topological structure on a set, page 15
- \mathcal{U} : uniform structure on a set, page 6

Categories

- \mathcal{A} and \mathcal{B} : arbitrary real-generated categories, page 1
- \mathcal{C} : metrizable convergence spaces and continuous functions, page 2
- \mathcal{D} : topological spaces with the weak topology, page 101
- \mathcal{E} : uniform spaces and uniformly continuous maps, page 3
- \mathcal{F} : metrizable topological fields and continuous homomorphisms, page 111
- \mathcal{G} : metrizable topological abelian groups, page 105
- \mathcal{H} : clopen-paracompact metrizable topological spaces, page 72
- \mathcal{K} : quasi uniform spaces, page 3

- \mathfrak{L} : metrizable topological rings, page 111
- \mathcal{M} : metric spaces and isometries, page 2
- \mathcal{N} : metrizable proximity spaces and p-continuous maps, page 2
- \mathfrak{T} : metrizable topological spaces and continuous functions, page 2
- \mathcal{U} : metrizable uniform spaces, page 2
- \mathcal{V} : metrizable general topological vector spaces, page 141

Subsets of the real numbers

- $\frac{1}{2}D = \{0, \frac{1}{2}\}$, page 135
- $D = \{0, 1\}$, page 8
- $D_m = \{1/n_1 + \dots + 1/n_s : \text{for } 1 \leq i \leq s \leq m, n_i \text{ is a whole number}\} \cup \{0\}$, page 33
- $E = \{1/3^n : n \text{ is an integer}\} \cup \{0\}$, page 113
- $G = \text{an arbitrary additive subgroup of the real numbers, page 58}$
- $H = \{1/n : n \text{ is a whole number}\} \cup \{0\}$, page 33
- $I = [0, 1]$, page 8
- $J_m = \{I - D_m\} \cup \{0\}$ where m is a whole number, page 33
- $\mathbb{M} = \text{the computable real numbers, page 181}$
- $\mathbb{N} = \{1, 2, 3, \dots\}$, page 19
- $O = \{0\}$, page 44

\mathbb{P} = the irrational numbers, page 32

\mathbb{P}^+ = $\{\mathbb{P} \cap [0, \infty)\} \cup \{0\}$, page 32

\mathbb{Q} = the rational numbers, page 32

\mathbb{Q}^+ = $\mathbb{Q} \cap [0, \infty)$, page 32

\mathbb{R} = the real numbers, page 1

\mathbb{R}^+ = $\mathbb{R} \cap [0, \infty)$, page 33

S and T stand for arbitrary subsets of \mathbb{R} , page 2

W = $\{1/3^n : n \text{ is a whole number}\} \cup \{0\}$, page 36

X_m = $\{1/2^{n_1} + \dots + 1/2^{n_s} : \text{for } 1 \leq i \leq s \leq m, n_i \text{ is a whole number}\} \cup \{0\}$, page 91

\mathbb{Z} = $\{0, \pm 1, \pm 2, \dots\}$, page 56

\mathbb{Z}^+ = $\{0, 1, 2, \dots\}$, page 56

Families of subsets of the real numbers

\mathcal{H} : subsets of the positive reals which include 0 , page 5

\mathcal{J} : non empty subsets of the real numbers, page 2

\mathcal{O} : neighborhoods of 0 in \mathbb{R}^+ , page 41

\mathcal{S} : arbitrary non empty family of subsets, page 2

\mathcal{W} : positive parts of additive subgroups of \mathbb{R} , page 58

\mathcal{X} : closed subsets of the positive reals which include 0 , page 46

\mathcal{Y} : semimodules in \mathbb{R}^+ , page 56

\mathcal{Z} : closed subgroups of \mathbb{R} , page 59

Properties of structure generating functionsFunctions of two variables (page 93 and page 105)

1. $d(x,y) \geq 0$ for all x and y , $d(x,x) = 0$ for all x ,
2. if $d(x,y) = 0$ then $x = y$,
3. $d(x,y) = d(y,x)$ for all x and y ,
4. $d(x,y) \leq d(x,z) + d(z,y)$ for all $x, y,$ and z ,
5. $d(x,y) \leq \max\{d(x,z), d(z,y)\}$ for all $x, y,$ and z ,
6. $d(x+a, y+a) = d(x,y)$ for all $x, y,$ and a .

$$\mathcal{P}_1 = \{1, 2, 3, 5\}$$

$$\mathcal{P}_{10} = \{1, 3, 5\}$$

$$\mathcal{P}_2 = \{1, 2, 3, 4\}$$

$$\mathcal{P}_{20} = \{1, 3, 4\}$$

$$\mathcal{P}_3 = \{1, 2, 3\}$$

$$\mathcal{P}_{30} = \{1, 3\}$$

$$\mathcal{P}_4 = \{1, 2\}$$

$$\mathcal{P}_{40} = \{1\}$$

$$\mathcal{P}_5 = \{1, 2, 4\}$$

$$\mathcal{P}_{50} = \{1, 4\}$$

$$\mathcal{P}_6 = \{1, 2, 3, 4, 6\}$$

Functions of one variable (page 109 and page 141)

1. $f(x) = 0$ if and only if $x = 0$,
2. $f(x) = f(-x)$ for all x ,
3. $f(x+y) \leq f(x) + f(y)$ for all x and y ,
4. $f(x+y) \leq \max\{f(x), f(y)\}$ for all x and y ,
5. $f(x \cdot y) \leq \min\{f(x), f(y)\}$ for all x and y ,
6. $f(x \cdot y) \leq f(x) \cdot f(y)$ for all x and y ,
7. $f(x \cdot y) = f(x) \cdot f(y)$ for all x and y ,
8. if $a \rightarrow 0$ in \mathbb{K} and $x \in V$ then $f(ax) \rightarrow 0$ in \mathbb{R} ,
9. if $a \in \mathbb{K}$ and $|a| \leq 1$ then $f(ax) \leq f(x)$ for all x .

$$\mathcal{P}_{21} = \{1, 2, 3, 5\}$$

$$\mathcal{P}_{22} = \{1, 2, 3, 6\}$$

$$\mathcal{P}_{23} = \{1, 2, 4, 5\}$$

$$\mathcal{P}_{24} = \{1, 2, 4, 6\}$$

$$\mathcal{P}_{31} = \{1, 2, 3, 7\}$$

$$\mathcal{P}_{32} = \{1, 2, 4, 7\}$$

$$\mathcal{P}_{41} = \{1, 2, 3, 8, 9\}$$

References

- [1] R. Arens and J. Dugundji, "A remark on the concept of compactness", *Portugaliae Math.* 9 (1950), 141-143.
- [2] S. Banach, "Sur les opérations dans les ensembles abstraits et leurs applications aux équations intégrales", *Fund. Math.* 3 (1922), 133-181.
- [3] B. Banaschewski, "Über nulldimensionale Räume", *Math. Nachr.* 13 (1955), 129-140.
- [4] E. Beckenstein, "On regular non-archimedean Banach algebras", *Arch. Math.* 19 (1968), 423-427.
- [5] R. Bennett, "Countable dense homogeneous spaces", *Fund. Math.* 74 (1972), 189-194.
- [6] R.H. Bing, "Extending a metric", *Duke Math. J.* 14 (1947), 511-519.
- [7] R.H. Bing, "Metriization of topological spaces", *Canad. J. Math.* 3 (1951), 175-186.
- [8] W. Blum, "Über kommutative nichtarchimedische Banach algebren", *Arch. Math.* 24 (1973), S. 493-498.
- [9] N. Bourbaki, Commutative Algebra, Addison-Wesley, Reading, Massachusetts, 1972.
- [10] N. Bourbaki, General Topology Part I, Addison-Wesley, Reading, Massachusetts, 1966.

- [11] N. Bourbaki, General Topology Part II, Addison-Wesley, Reading, Massachusetts, 1966.
- [12] J.R. Boyd, "Axioms that define semi-metric, Moore, and metric spaces", Proc. Amer. Math. Soc. 13 (1962), 482-484.
- [13] K.A. Broughan, "A metric characterizing Čech dimension zero", Proc. Amer. Math. Soc. 39 (1973), 437-440.
- [14] K.A. Broughan, "Metriization of spaces having Čech dimension zero", Bull. Austral. Math. Soc. 9 (1973), 161-168.
- [15] K.A. Broughan and M. Schroder, "Variations on a metric theme", Math. Chronicle 3 (1974), 71-80.
- [16] M. Brown, "Semi-metric spaces", Summer Institute on Set Theoretic Topology, Madison, Amer. Math. Soc. (1955), 64-66.
- [17] R. Cacciopoli, "Un teorema generale sull'esistenza di elementi uniti in una trasformazione funzionale", Rend. Accad. Naz. Lincei 11 (1930), 794-799.
- [18] P.J. Collins, "On uniform connection properties", Amer. Math. Monthly 78 (1971), 372-374.
- [19] W.W. Comfort, "A survey of cardinal invariants", Gen. Top. App. 1 (1971), 163-199.

- [20] C.H. Dowker, "Local dimension of normal spaces",
Quart. Jour. of Math. Oxford 6 (1955), 101-120.
- [21] J. Dugundji, Topology, Allyn and Bacon, Boston, 1966.
- [22] R. Engelking, Outline of General Topology, North
Holland, Amsterdam, 1968.
- [23] H.C. Enos, "Coarse uniformities on the rationals",
Proc. Amer. Math. Soc. 34 (1972), 623-626.
- [24] B. Fitzpatrick, Jr., "A note on countable dense
homogeneity", Fund. Math. 75 (1972), 33-34.
- [25] P. Fletcher and W.F. Lindgren, "Transitive
quasi-uniformities", J. Math. Anal. and App. 39
(1972), 397-405.
- [26] M.K. Fort, Jr., "Homogeneity of infinite products of
manifolds with boundary", Pacific J. Math. 12 (1962),
879-884.
- [27] J. de Groot, "On a metric that characterizes dimension",
Canad. J. Math. 9 (1957), 511-514.
- [28] E. Hille and R.S. Phillips, Functional analysis and
semi-groups, Amer. Math. Soc. Colloquium Publications,
Vol. 31, revised edition, Providence, R.I. (1957).
- [29] O. Hölder, "Die Axiome der Quantität und die Lehre
vom Mass", Leipzig Ber., Math.-Phys. Cl. 53 (1901),
1-64.

- [30] J. Horváth, Topological Vector Spaces and Distributions
Volume I, Addison-Wesley, Reading, Massachusetts, 1966.
- [31] I. Kaplansky, "Topological methods in valuation theory",
Duke Math. J. 14 (1948), 527-541.
- [32] N. Kimura, "On a sum theorem in dimension theory",
Proc. Japan Acad. 43 (1967), 98-101.
- [33] K. Kuratowski, "Quelques problèmes concernant les
espaces métriques non-séparables", Fund. Math. 25
(1935), 534-545.
- [34] S. Lang, Algebra, Addison-Wesley, Reading, Mass., 1965.
- [35] S. Lefschetz, Algebraic Topology, Amer. Math. Soc.
Colloquium Pub., Vol. 27, New York, 1942.
- [36] N. Levine, "On uniformities generated by equivalence
relations", Rend. Circ. Mat. Palermo (2) 18 (1969),
62-70.
- [37] N. Levine, "Well chained uniformities", Kyunpook
Math. J. 11 (1971), 143-149.
- [38] K. Mahler, Introduction to p-adic numbers and their
functions, Cambridge University Press, London, 1973.
- [39] M.R. Mather, "Paracompactness and partitions of unity",
preprint (1964).
- [40] E. Michael, "A note on paracompact spaces", Proc. Amer.
Math. Soc. 4 (1953), 831-838.

- [41] K. Morita, "Normal families and dimension theory for metric spaces", *Math. Ann.* 128 (1954), 350-362.
- [42] K. Morita, "On the dimension of normal spaces II", *Journ. Math. Soc. Japan* 2 (1950), 16-33.
- [43] K. Nagami, "Paracompactness and strong screenability", *Nagoya Math. J.* 8 (1955), 83-88.
- [44] L. Narici, "On nonarchimedean Banach algebras", *Arch. Math.* 19 (1968), 428-435.
- [45] L.J. Norman, "A sufficient condition for quasi-metrizability of a topological space", *Portugaliae Math.* 26 (1967), 207-211.
- [46] G. Peano, "Intégration par séries des équations différentielles linéaires", *Math. Ann.* 32 (1888), 450-456.
- [47] A.R. Pears, "On quasi-order spaces, normality and paracompactness", *Proc. Lond. Math. Soc.* 23 (1971), 428-444.
- [48] E. Picard, "Mémoire sur la théorie des équations aux dérivées partielles et la méthode des approximations successives", *J. Math.* (4) 6 (1890), 145-210.
- [49] J. Pollard, "On extending homeomorphisms on zero-dimensional spaces", *Fund. Math.* 67 (1970), 39-48.

- [50] V.I. Ponomarev, "Projective spectra and continuous mappings of paracompacta", *Mat. Sb.* 60 (102) (1963), 89-119; *Amer. Math. Soc. Transl. Ser. 2* 39 (1964), 133-164.
- [51] M. van der Put, "Algèbres de fonctions continues p-adiques", *Nederl. Akad. Wetensch. Proc. Ser. A* 71 (1968), 401-420.
- [52] M.O. Rabin, "Computable algebra, general theory and theory of computable fields", *Trans. Amer. Math. Soc.* 95 (1960), 341-360.
- [53] I.L. Reilly, "On quasiuniform spaces and quasipseudometrics", *Math. Chronicle* 1 Pt II (1970), 71-76.
- [54] A.P. Robertson and Wendy Robertson, "A note on the completion of a uniform space", *Jour. Lond. Math. Soc.* 33 (1958), 181-185.
- [55] H. Rogers, Theory of Recursive Functions and Effective Computability, McGraw-Hill, New York, 1967.
- [56] P. Roy, "Failure of the equivalence of dimension concepts for metric spaces", *Bull. Amer. Math. Soc.* 68 (1962), 609-613.
- [57] P. Roy, "Nonequality of dimensions for metric spaces", *Trans. Amer. Math. Soc.* 134 (1968), 117-132.
- [58] N. Schilkret, "Non-Archimedean Banach algebras", *Duke Math. J.* 37 (1970), 315-322.

- [59] W. Sierpinski, Introduction to General Topology,
University of Toronto Press, Toronto, 1934.
- [60] M. Sion and G. Zelmer, "On quasi-metrizability", *Canad.
J. Math.* 19 (1967), 1243-1249.
- [61] Yu. M. Smirnov, "On strongly paracompact spaces", *Izv.
Akad. Nauk. SSSR ser. mat.* 20 (1956), 253-274 (Russian).
- [62] L.A. Steen, "Conjectures and counterexamples in
metrization theory", *Amer. Math. Mon.* 79 (1972),
113-132.
- [63] R.A. Stoltenberg, "On quasi-metric spaces", *Duke Math.
J.* 36 (1969), 65-71.
- [64] A.H. Stone, "Paracompactness and product spaces", *Bull.
Amer. Math. Soc.* 54 (1948), 977-982.
- [65] W.J. Thron, Topological Structures, Holt, Rinehart
and Winston, New York, 1966.
- [66] H.E. Vaughn, "On the class of metrics defining a
metrizable space", *Bull. Amer. Math. Soc.* 44 (1938),
557-561.