

# Bibliography

## *Ancient and Medieval Mathematical Works Referenced by Title*

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*Commentary on Euclid's Data*, Marinus: Greek text edited by Menge (1896, 234–257), English translation by Taisbak (2003, 241–249).

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*Elements*, Euclid: Greek text edited with Latin translation by Heiberg (1969–1977), English translation with commentary by Heath (1956), French translation and commentary by Vitrac (1990–2001).

*Measurements*, Heron: Greek text edited with German translation by Schöne (1903), Greek text reedited with French translation and commentary by Acerbi and Vitrac (2014)

### *Medieval Manuscripts*

#### *Greek*

**a:** Florence, Biblioteca Medicea Laurenziana, Plut. 28.1. 14th century.

**b:** Bologna, Biblioteca Comunale dell'Archiginnasio di Bologna, A.18–19. 11th century.

**P:** Vatican, Biblioteca Apostolica Vaticana, gr. 190. Early 9th century.<sup>13</sup>

**Vat:** Vatican, Biblioteca Apostolica Vaticana, gr. 204. 9th century.

#### *Arabic*

**A:** Istanbul, Topkapı Palace Museum, Ahmet III 3464. Early 7th century AH (early 13th century CE).

**E:** Madrid, Escorial Library Ms. árabe 907. 7th century AH (13th century CE).

**Ia:** Istanbul, Topkapı Palace Museum, Ahmet III 3453. Late 7th century AH (late 13th century CE).

**Ih:** Istanbul, Hacı Selim Ağa Library 743. Late 7th century AH (Late 13th century CE).

**Is:** Istanbul, Süleymaniye Library, Aya Sofya 2758. Early 8th century AH (Early 14th century CE).

**K:** Private collection, sold by H.P. Kraus. Late 7th century AH (late 13th century CE).

**L:** London, British Library, Or. 13127. 548 AH (1153 CE).

**M:** Tehran, Majlis Shūrā 6851. 859 AH (1455 CE).<sup>14</sup>

<sup>13</sup> This manuscript used to be dated to the 10th century, but Mogenet and Tihon (1985, 23) argue that we should change this to the early 9th century (Vitrac 2012, 73, n. 12).

<sup>14</sup> De Young (2015) refers to this manuscript as 2060, which number does appear on the cover. The number 6851, however, also appears on the cover in two places and is listed in the online database.

**Tb:** Tabriz, National Library, 3484. Late 7th–early 8th century AH (late 13th–early 14th century CE).

**Th:** Tehran, Madrasa-yi ‘Ālī-yi Shahīd Muṭahharī Library (formally Sipahsālār), 4727. Late 7th century AH (late 13th century CE).

**Tm:** Tehran, Malik Library, 3586. 345 AH (954 CE).

**W:** Warsaw, Jagiellonska Library, (formally Berlin, Preussische Staatsbibliothek) Ms. or. fol. 258. 12th century AH (17th century CE).

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