

# References

*This is an integrated list of the references cited in the chapters of the book. The numbers here are for enumeration purposes only and do not correlate with the reference numbers in each chapter.*

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