

References

In addition to the references appearing in the text, we have included a number of textbooks and monographs for general reference. One category is books on finite element methods and includes (Aubin 1980), (Axelsson & Barker 1984), (Becker, Carey & Oden 1981), (Braess 2001), (Ciarlet 1976), (Ciarlet 1991), (Fairweather 1978), (Fried 1979), (Hughes 2000), (Oden & Reddy 1976), (Schwab 1998), (Szabó & Babuška 1991), and (Schultz 1972). Another category is books on partial differential equations and includes (Ciarlet 1988), (Gilbarg & Trudinger 1983), (Lions & Magenes 1972), (Showalter 1977), (Sobolev 1964), (Taylor 1996), (Wendland 1979) and (Wloka 1987).

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“ $i.x.j$ ” refers to an exercise, and

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