

# CHAOS: a parallelization scheme for training convolutional neural networks on Intel Xeon Phi

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**Abstract** Deep learning is an important component of Big Data analytic tools and intelligent applications, such as self-driving cars, computer vision, speech recognition, or precision medicine. However, the training process is computationally intensive and often requires a large amount of time if performed sequentially. Modern parallel computing systems provide the capability to reduce the required training time of deep neural networks. In this paper, we present our parallelization scheme for training convolutional neural networks (CNN) named Controlled Hogwild with Arbitrary Order of Synchronization (CHAOS). Major features of CHAOS include the support for thread and vector parallelism, non-instant updates of weight parameters during back-propagation without a significant delay, and implicit synchronization in arbitrary order. CHAOS is tailored for parallel computing systems that are accelerated with the Intel Xeon Phi. We evaluate our parallelization approach empirically using measurement techniques and performance modeling for various numbers of threads and CNN architectures. Experimental results for the MNIST dataset of handwritten digits using the total number of threads on the Xeon Phi show speedups of up to

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103× compared to the execution on one thread of the Xeon Phi, 14× compared to the sequential execution on Intel Xeon E5, and 58× compared to the sequential execution on Intel Core i5.

**Keywords** Parallel programming · Deep learning · Convolutional neural networks · Intel Xeon Phi

## 1 Introduction

Traditionally engineers developed applications by specifying computer instructions that determined the application behavior. Nowadays engineers focus on developing and implementing sophisticated deep learning models that can learn to solve complex problems. Moreover, deep learning algorithms [28] can learn from their own experience rather than that of the engineer.

Many private and public organizations are collecting huge amounts of data that may contain useful information from which valuable knowledge may be derived. With the pervasiveness of the Internet of Things the amount of available data is getting much larger [20]. Deep learning is a useful tool for analyzing and learning from massive amounts of data (also known as Big Data) that may be unlabeled and unstructured [37,45,48]. Deep learning algorithms can be found in many modern applications [17,19,21,49,51,55,57,60], such as voice recognition, face recognition, autonomous cars, classification of liver diseases and breast cancer, computer vision, or social media.

A convolutional neural network (CNN) is a variant of a deep neural network (DNN) [14]. Inspired by the visual cortex of animals, CNNs are applied to state-of-the-art applications, including computer vision and speech recognition [15]. However, supervised training of CNNs is computationally demanding and time-consuming, and in many cases, several weeks are required to complete a training session. Often applications are tested with different parameters, and each test requires a full session of training.

Multi-core processors [56] and in particular many-core [5] processing architectures, such as the NVIDIA graphical processing unit (GPU) [38] or the Intel Xeon Phi [8] coprocessor, provide processing capabilities that may be used to significantly speed up the training of CNNs. While existing research [12,42,49,54,58] has addressed extensively the training of CNNs using GPUs, so far not much attention is given to the Intel Xeon Phi coprocessor. Besides the performance capabilities, the Xeon Phi deserves our attention because of programmability [39] and portability [23].

In this paper, we present our parallelization scheme for training convolutional neural networks, named Controlled Hogwild with Arbitrary Order of Synchronization (CHAOS). CHAOS is tailored for the Intel Xeon Phi coprocessor and exploits both the thread- and SIMD-level parallelism. The thread-level parallelism is used to distribute the work across the available threads, whereas SIMD parallelism is used to compute the partial derivatives and weight gradients in convolutional layer. Empirical evaluation of CHAOS is performed on an Intel Xeon Phi 7120 coprocessor. For experimentation, we use various number of threads, different CNNs architectures, and the MNIST dataset of handwritten digits [30]. Experimental evaluation results show

that using the total number of available threads on the Intel Xeon Phi we can achieve speedups of up to  $103\times$  compared to the execution on one thread of the Xeon Phi,  $14\times$  compared to the sequential execution on Intel Xeon E5, and  $58\times$  compared to the sequential execution on Intel Core i5. The error rates of the parallel execution are comparable to the sequential one. Furthermore, we use performance prediction to study the performance behavior of our parallel solution for training CNNs for numbers of cores that go beyond the generation of the Intel Xeon Phi that was used in this paper. The main contributions of this paper include:

- design and implementation of CHAOS parallelization scheme for training CNNs on the Intel Xeon Phi,
- performance modeling of our parallel solution for training CNNs on the Intel Xeon Phi,
- measurement-based empirical evaluation of CHAOS parallelization scheme,
- model-based performance evaluation for future architectures of the Intel Xeon Phi.

The rest of the paper is organized as follows. We discuss the related work in Sect. 2. Section 3 provides background information on CNNs and the Intel Xeon Phi many-core architecture. Section 4 discusses the design and implementation aspects of our parallelization scheme. The experimental evaluation of our approach is presented in Sect. 5. We summarize the paper in Sect. 6.

## 2 Related work

In comparison with related work that target GPUs, the work related to machine learning for Intel Xeon Phi is sparse. In this section, we describe machine learning approaches that target the Intel Xeon Phi coprocessor, and thereafter, we discuss CNN solutions for GPUs and contrast them to our CHAOS implementation.

### 2.1 Machine learning targeting Intel Xeon Phi

In this section, we discuss existing work for support vector machines (SVMs), restricted Boltzmann machines (RBMs), sparse auto encoders and the brain-state-in-a-box (BSB) model.

You et al. [59] present a library for parallel support vector machines, MIC-SVM, which facilitates the use of SVMs on many- and multi-core architectures including Intel Xeon Phi. Experiments performed on several known datasets showed up to  $84\times$  speedup on the Intel Xeon Phi compared to the sequential execution of LIBSVM [6]. In comparison with their work, we target deep learning.

Jin et al. [22] perform the training of sparse auto encoders and restricted Boltzmann machines on the Intel Xeon Phi 5110p. The authors reported a speedup factor of  $7-10\times$  times compared to the Xeon E5620 CPU and more than  $300\times$  times compared to the un-optimized version executed on one thread on the coprocessor. Their work targets unsupervised deep learning of restricted Boltzmann machines and sparse auto encoders, whereas we target supervised deep learning of CNNs.

The performance gain on Intel Xeon Phi 7110p for a model called brain-state-in-a-box (BSB) used for text recognition is studied by Ahmed et al. in [2]. The authors report about twofold speedup for the coprocessor compared to a CPU with 16 cores when parallelizing the algorithm. While both approaches target Intel Xeon Phi, our work addresses training of CNNs on the MNIST dataset.

## 2.2 Related work targeting CNNs

In this section, we will discuss CNNs solutions for GPUs in the context of computer vision (image classification). Work related to MNIST [30] dataset is of most interest, also NORB [31] and CIFAR 10 [25] is considered. Additionally, work done in speech recognition and document processing is briefly addressed. We conclude this section by contrasting the presented related work with our CHAOS parallelization scheme.

Work presented by Cireşan et al. [12] target a CNN implementation raising the bars for the CIFAR10 (19.51% error rate), NORB (2.53% error rate) and MNIST (0.35% error rate) datasets. The training was performed on GPUs (Nvidia GTX 480 and GTX 580) where the authors managed to decrease the training time severely—up to 60× compared to sequential execution on a CPU—and decrease the error rates to an, at the time, state-of-the-art accuracy level.

Later, Cireşan et al. [11] presented their multi-column deep neural network for classification of traffic signs. The results show that the model performed almost human-like (humans' error rate about 0.20%) on the MNIST dataset, achieving a best error rate of 0.23%. The authors trained the network on a GPU.

Vrtanoski et al. [54] use OpenCL for parallelization of the back-propagation algorithm for pattern recognition. They showed a significant cost reduction; a maximum speedup of 25.8× was achieved on an ATI 5870 GPU compared to a Xeon W3530 CPU when training the model on the MNIST dataset.

The ImageNet challenge aims to evaluate algorithms for large-scale object detection and image classification based on the ImageNet dataset. Krizhevsky et al. [26] joined the challenge and reduced the error rate of the test set to 15.3% from the second best 26.2% using a CNN with 5 convolutional layers. For the experiments, two GPUs (Nvidia GTX 580) were used only communicating in certain layers. The training lasted for 5 to 6 days.

In a later challenge, ILSVRC 2014, a team from Google entered the competition with GoogleNet, a 22-layer deep CNN and won the classification challenge with a 6.67% error rate. The training was carried out on CPUs. The authors state that the network could be trained on GPUs within a week, illuminating the limited amount of memory to be one of the major concerns [49].

Yadan et al. [58] used multiple GPUs to train CNNs on the ImageNet dataset using both data and model parallelism, i.e., either the input space is divided into mini-batches where each GPU train its own batch (data parallelism) or the GPUs train one sample together (model parallelism). There is no direct comparison with the training time on CPU; however, using 4 GPUs (Nvidia Titan) and model and data parallelism, the network was trained for 4.8 days.

Song et al. [47] constructed a CNN to recognize face expressions and developed a smartphone app in which the user can capture a picture and send it to a server hosting the network. The network predicts a face expression and sends the result back to the user. With the help of GPUs (Nvidia Titan), the network was trained in a couple of hours on the ImageNet dataset.

Scherer et al. [43] accelerated the large-scale neural networks with parallel GPUs. Experiments with the NORB dataset on an Nvidia GTX 285 GPU showed a maximal speedup of  $115\times$  compared to a CPU implementation (Core i7 940). After training the network for 360 epochs, an error rate of 8.6% was achieved.

Cireřan et al. [10] combined multiple CNNs to classify German traffic signs and achieved a 99.15% recognition rate (0.85 % error rate). The training was performed using an Intel Core i7 and 4 GPUs ( $2 \times$  GTX 480 and  $2 \times$  GTX 580).

More recently, Abadi et al. [1] presented TensorFlow, a system for expressing and executing machine learning algorithms including training deep neural network models.

Researchers have also found CNNs successful for speech tasks. Large vocabulary continuous speech recognition deals with translation of continuous speech for languages with large vocabularies. Sainath et al. [42] investigated the advantages of CNNs performing speech recognition tasks and compared the results with previous DNN approaches. Results indicated on a 12–14% relative improvement of word error rates compared to a DNN trained on GPUs.

Chellapilla et al. [7] investigated GPUs (Nvidia Geforce 7800 Ultra) for document processing on the MNIST dataset and achieved a  $4.11\times$  speedup compared to the sequential execution a Intel Pentium 4 CPU running at 2.5 GHz clock frequency.

In contrast to CHAOS, these studies target training of CNNs using GPUs, whereas our approach addresses training of CNNs on the MNIST dataset using the Intel Xeon Phi coprocessor. While there are several review papers (such as, [4, 46, 50]) and online articles (such as, [36]) that compare existing frameworks for parallelization of training CNN architectures, we focus on detailed analysis of our proposed parallelization approach using measurement techniques and performance modeling. We compare the performance improvement achieved with CHAOS parallelization scheme to the sequential version executed on Intel Xeon Phi, Intel Xeon E5 and Intel Core i5 processor.

### 3 Background

In this section, we first provide some background information related to the neural networks focusing on convolutional neural networks, and thereafter, we provide some information about the architecture of the Intel Xeon Phi.

#### 3.1 Neural networks

A convolutional neural network is a variant of a deep neural network, which introduces two additional layer types: *convolutional layers* and *pooling layers*. The mammal visual processing system is hierarchical (deep) in nature. Higher level features are abstractions of lower level ones. For example, to understand speech, waveforms are

translated through several layers until reaching a linguistic level. A similar analogy can be drawn for images, where edges and corners are lower-level abstractions translated into more spatial patterns on higher levels. Moreover, it is also known that the animal cortex consists of both simple and complex cells firing on certain visual inputs in their receptive fields. Simple cells detect edge-like patterns, whereas complex cells are locally invariant, spanning larger receptive fields. These are the very fundamental properties of the animal brain inspiring DNNs and CNNs.

In this section, we first describe the DNNs and the forward- and back-propagation and thereafter we introduce the CNNs.

### 3.1.1 Deep neural networks

The architecture of a DNN consists of multiple layers of neurons. Neurons are connected to each other through edges (weights). The network can simply be thought of as a weighted graph; a directed acyclic graph represents a feed-forward network. The depth and breadth of the network differ as may the layer types. Regardless of the depth, a network has at least one input and one output layer. A neuron has a set of incoming weights, which have corresponding outgoing edges attached to neurons in the previous layer. Also, a bias term is used at each layer as an intercept term. The goal of the learning process is to adjust the network weights and find a global minimum by reducing the overall error, i.e., the deviation between the predicted and the desired outcome of all the samples. The resulting weight parameters can thereafter be used to make predictions of unseen inputs [3].

### 3.1.2 Forward propagation

DNNs can make predictions by forward propagating an input through the network. Forward propagation proceeds by performing calculations at each layer until reaching the output layer, which contains a vector representing the prediction. For example, in image classification problems, the output layer contains the prediction score that indicates the likelihood that an image belongs to a category [3, 18].

The forward propagation starts from a given input layer, then at each layer the activation for a neuron is activated using the equation  $y_i^l = \sigma(x_i^l) + I_i^l$  where  $y_i^l$  is the output value of neuron  $i$  at layer  $l$ ,  $x_i^l$  is the input value of the same neuron, and  $\sigma$  (sigmoid) is the activation function.  $I_i^l$  is used for the input layer when there is no previous layer. The goal of the activation function is to return a normalized value (sigmoid return  $[0,1]$  and  $\tanh$  is used in cases where the desired return values are  $[-1,1]$ ). The input  $x_i^l$  can be calculated as  $x_i^l = \sum_j (w_{ji}^l y_j^{l-1})$  where  $w_{ji}^l$  denotes the weight between neuron  $i$  in the current layer  $l$ , and  $j$  in the previous layer, and  $y_j^{l-1}$  the output of the  $j$ th neuron at the previous layer. This process is repeated until reaching the output layer. At the output layer, it is common to apply a soft max function, or similar, to squash the output vector and hence derive the prediction.

### 3.1.3 Back-propagation

Back-propagation is the process of propagating errors, i.e., the loss calculated as the deviation between the predicted and the desired output, backward in the network, by adjusting the weights at each layer. The error and partial derivatives  $\delta_i^l$  are calculated at the output layer based on the predicted values from forward propagation and the labeled value (the correct value). At each layer, the relative error of each neuron is calculated and the weight parameters are updated based on how much the neuron participated in the faulty prediction. The equation:  $\frac{\delta E}{\delta y_i^l} = \sum w_{ij}^l \frac{\delta E}{\delta x_j^{l+1}}$  denotes that the partial derivative of neuron  $i$  at the current layer  $l$  is the sum of the derivatives of connected neurons at the next layer multiplied with the weights, assuming  $w^l$  denotes the weights between the maps. Additionally, a decay is commonly used to control the impact of the updates, which is omitted in the above calculations. More concretely, the algorithm can be thought of as updating the layer's weights based on "how much it was responsible for the errors in the output" [3, 18].

### 3.1.4 Convolutional neural networks

A convolutional neural network is a multilayer model constructed to learn various levels of representations where higher level representations are described based on the lower level ones [44]. It is a variant of deep neural network that introduces two new layer types: *convolutional* and *pooling* layers.

The convolutional layer consists of several feature maps where neurons in each map connect to a grid of neurons in maps in the previous layer through overlapping kernels. The kernels are tiled to cover the whole input space. The approach is inspired by the receptive fields of the mammal visual cortex. All neurons of a map extract the same features from a map in the previous layer as they share the same set of weights.

Pooling layers intervene convolutional layers and have shown to lead to faster convergence. Each neuron in a pooling layer outputs the (maximum/average) value of a partition of neurons in the previous layer and hence only activates if the underlying grid contains the sought feature. Besides from lowering the computational load, it also enables position invariance and down samples the input by a factor relative to the kernel size [29].

Figure 1 shows LeNet-5 that is an example of a convolutional neural network. Each layer of convolution and pooling (that is a specific method of subsampling used in LeNet) comprise several feature maps. Neurons in the feature map cover different subfields of the neurons from the previous layer. All neurons in a map share the same weight parameters; therefore, they extract the same features from different parts of the input from the previous layers.

CNNs are commonly constructed similarly to the LeNet-5, beginning with an input layer, followed by several convolutional/pooling combinations, ending with a fully connected layer and an output layer [29]. Recent networks are much deeper and/or wider, for instance, the GoogleNet [49] consists of 22 layers.

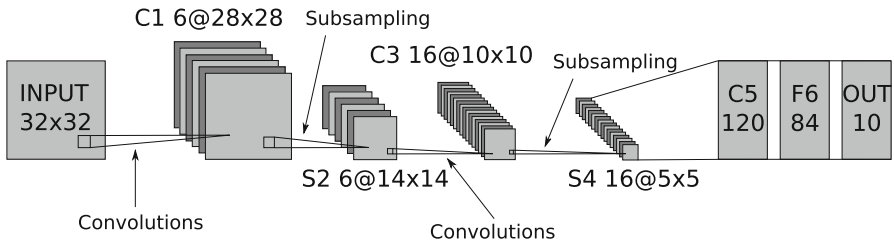


Fig. 1 LeNet-5 architecture

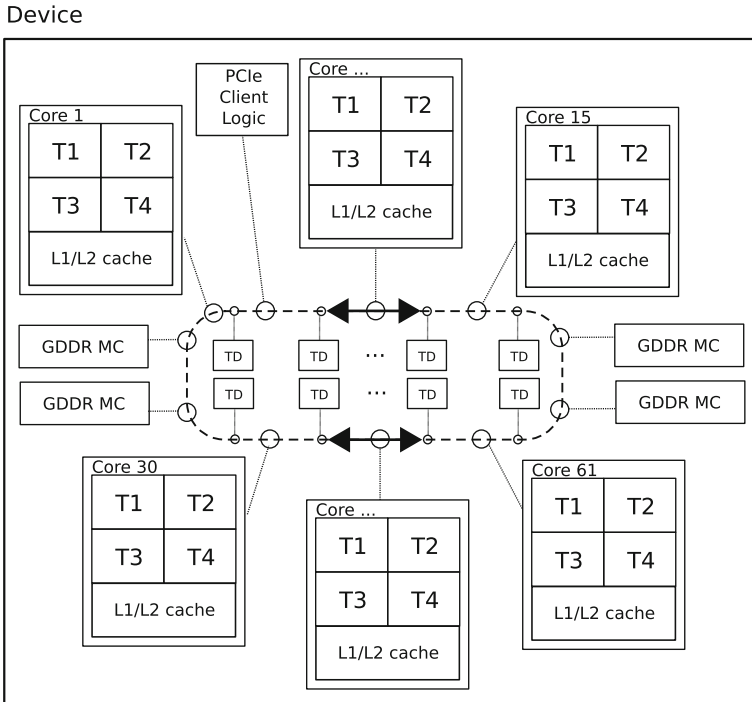


Fig. 2 An overview of our Emil system accelerated with the Intel Xeon Phi

Various implementations target the convolutional neural networks, such as *EbLearn* at New York University and *Caffe* at Berkeley. As a basis for our work, we selected a project developed by Cireşan [9]. This implementation targets the MNIST dataset of handwritten digits and has the possibility to dynamically configure the definition of layers, the activation function and the connection types using a configuration file.

### 3.2 Parallel systems accelerated with Intel®Xeon Phi™

Figure 2 depicts an overview of the Intel Xeon Phi (codenamed Knights Corner) architecture. It is a many-core shared-memory coprocessor, which runs a lightweight



Linux operating system that offers the possibility to communicate with it over *ssh*. The Xeon Phi offers two programming models:

1. *offload* parts of the applications running on the host are offloaded to the coprocessor
2. *native* the code is compiled specifically for running natively on the coprocessor. The code and all the required libraries should be transferred on the device. In this paper, we focus on the native mode.

The Intel Xeon Phi (type 7120P used in this paper) comprises 61 x86 cores, each core runs at 1.2 GHz base frequency, and up to 1.3GHz on max turbo frequency [8]. Each core can switch between four hardware threads in a round robin manner, which amounts to a total of 244 threads per coprocessor. Theoretically, the coprocessor can deliver up to one teraFLOP/s of double-precision performance or two teraFLOP/s of single-precision performance. Each core has its own L1 (32KB) and L2 (512KB) cache. The L2 cache is kept fully coherent by a global distributed tag directory (TD). The cores are connected through a bidirectional ring bus interconnect, which forms a unified shared L2 cache of 30.5MB. In addition to the cores, there are 16 memory channels that in theory offer a maximum memory bandwidth of 352GB/s. The GDDR memory controllers provide direct interface to the GDDR5 memory, and the PCIe Client Logic provides direct interface to the PCIe bus.

Efficient usage of the available vector processing units of the Intel Xeon Phi is essential to fully utilize the performance of the coprocessor [53]. Through the 512-bit wide SIMD registers, it can perform 16 (16 wide  $\times$  32 bit) single-precision or 8 (8 wide  $\times$  64 bit) double-precision operations per cycle.

The performance capabilities of the Intel Xeon Phi are discussed and investigated empirically by different researches within several domain applications [16,32–35,52].

## 4 Our parallelization scheme for training convolutional neural networks on Intel Xeon Phi

The parallelism can be either divided data-wise, i.e., threads process several inputs concurrently, or model-wise, i.e., several threads share the computational burden of one input. Whether one approach can be advantageous over the other mainly depends on the synchronization overhead of the weight vectors and how well it scales with the number of processing units.

In this section, we first discuss the design aspects of our parallelization scheme for training convolutional neural networks. Thereafter, we discuss the implementation aspects that allow full utilization of the Intel Xeon Phi coprocessor.

### 4.1 Design aspects

Online stochastic gradient descent has the advantage of instant updates of weights for each sample. However, the sequential nature of the algorithm yields impediments as the number of multi- and many-core platforms are emerging. We consider different existing parallelization strategies for stochastic gradient descent:

*Strategy A: Hybrid* uses both data and model parallelism, such that data parallelism is applied in convolutional layers, and the model parallelism is applied in fully connected layers [24].

*Strategy B: Averaged stochastic gradient* divides the input into batches and feeds each batch to a node. This strategy proceeds as follows: (1) initialize the weights of the learner by randomization; (2) split the training data into  $n$  equal chunks and send them to the learners; (3) each learner process the data and calculates the weight gradients for its batch; (4) send the calculated gradients back to the master; (5) the master computes and updates the new weights; and (6) the master sends the new weights to the nodes and a new iteration begins [13]. The convergence speed is slightly worse than for the sequential approach; however, the training time is heavily reduced.

*Strategy C: Delayed stochastic gradient* suggests updating the weight parameters in a round robin fashion by the workers. One solution is splitting the samples by the number of threads, and let each thread work on its own distinct chunk of samples, only sharing a common weight vector. Threads are only allowed to update the weight vector in a round robin fashion, and hence, each update will be delayed [27].

*Strategy D: HogWild!* is a stochastic gradient descent without locks. The approach is applicable for sparse optimization problems (threads/core updates do not conflict much) [41].

In this paper, we introduce Controlled Hogwild with Arbitrary Order of Synchronization (CHAOS), a parallelization scheme that can exploit both thread- and SIMD-level parallelism available on Intel Xeon Phi. CHAOS is a data-parallel controlled version of HogWild! with delayed updates, which combines parts of strategies A–D. The key aspects of CHAOS are:

- *Thread parallelism* The overview of our parallelization scheme is depicted in Fig. 3. Initially for as many threads as there are, available network instances are created, which share weight parameters, whereas to support concurrent processing of images some variables are private to each thread. After the initialization of CNNs and images is done, the process of training starts. The major steps of an epoch include: *Training*, *Validation* and *Testing*. The first step, *Training*, proceeds with each worker picking an image, forward propagates it through the network, calculates the error, and back-propagates the partial derivatives, adjusting the weight parameters. Since each worker picks a new image from the set, other workers do not have to wait for significantly slow workers. After *Training*, each worker participates in *Validation* and *Testing* evaluating the prediction accuracy of the network by predicting images in the validation and test set accordingly. Adoption of data parallelism was inspired by Krizhevsky [24], promoting data parallelism for convolutional layers as they are computationally intensive.
- *Controlled HogWild* During the back-propagation, the shared weights are updated after each layer's computations (a technique inspired by [27]), whereas the local weight parameters are updated instantly (a technique inspired by [41]), which means that the gradients are calculated locally first then shared with other workers. However, the update to the global gradients can be performed at any time, which means that there is no need to wait for other workers to finish their updates.

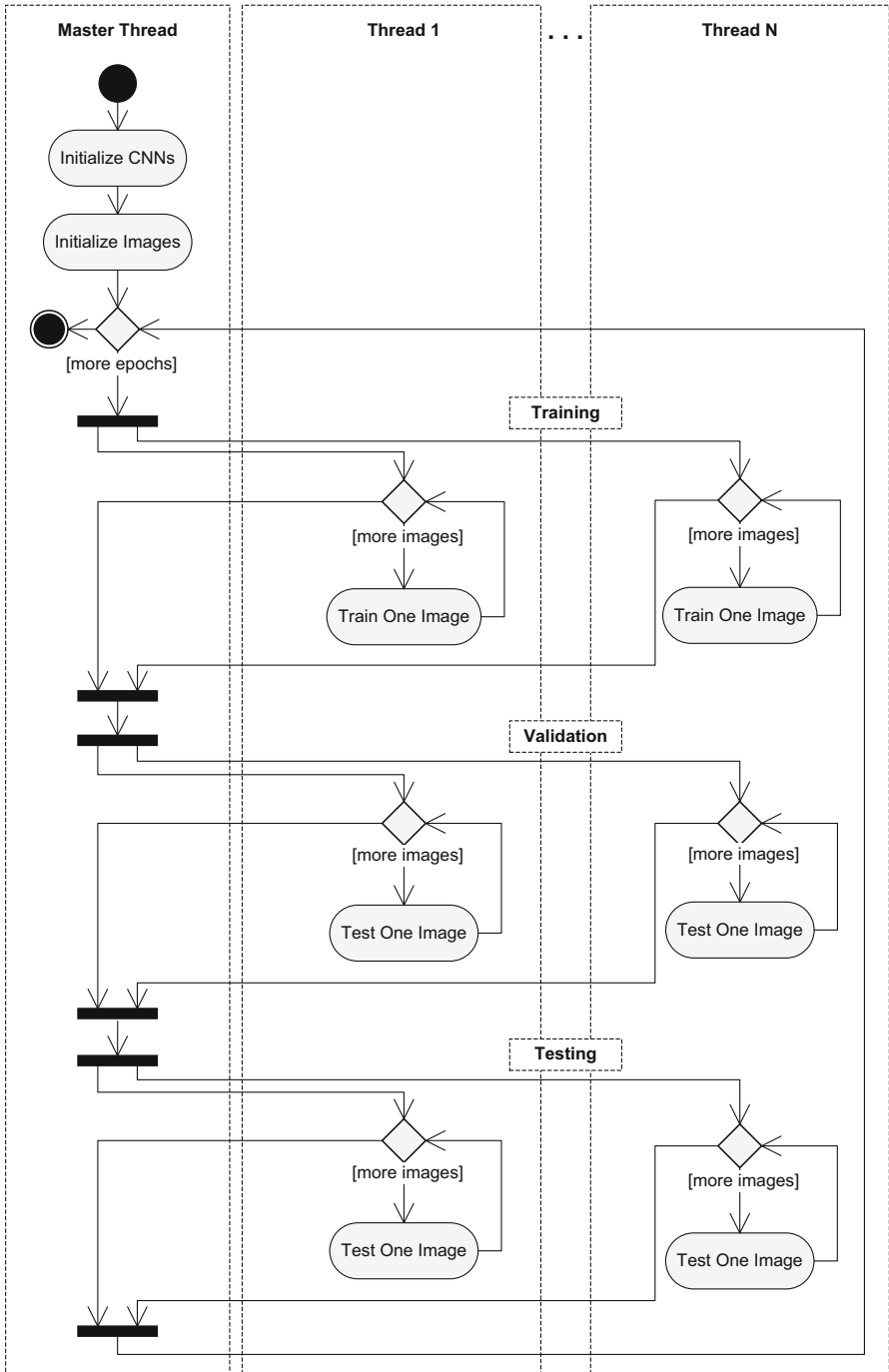


Fig. 3 Major activities of CHAOS parallelization scheme

This technique, which we refer to as non-instant updates of weight parameters without significant delay, allows us to avoid unnecessary cache line invalidation and memory writes.

- *Arbitrary order of synchronization* There is no need for explicit synchronization, because all workers share weight parameter. However, an implicit synchronization is performed in an arbitrary order because writes are controlled by a first-come-first schedule and reads are performed on demand.

The main goal of CHAOS is to minimize the time spent in the convolutional layers, which can be done through data parallelism, adapting the knowledge presented in strategy A. In strategy B, the synchronization is performed because of averaging worker's gradient calculations. Since work is distributed, computations are performed on stale parameters. The strategy can be applied in distributed and non-distributed settings. The division of work over several distributed workers was adapted in CHAOS. In strategy C, the updates are postponed using a round robin fashion where each thread gets to update when it is its turn. The difference compared to strategy B is that instances train on the same set of weights and no averaging is performed. The advantage is that all instances train on the same weights. The disadvantage of this approach is the delayed updates of the weight parameters as they are performed on stale data. Training on shared weights and delaying the updates are adopted in CHAOS. Strategy D presents a lock-free approach of updating the weight parameters; updates are performed instantly without any locks. Our updates are not instant; however, after computing the gradients there is nothing prohibiting a worker contributing to the shared weights, the notion of instant inspired CHAOS.

## 4.2 Implementation aspects

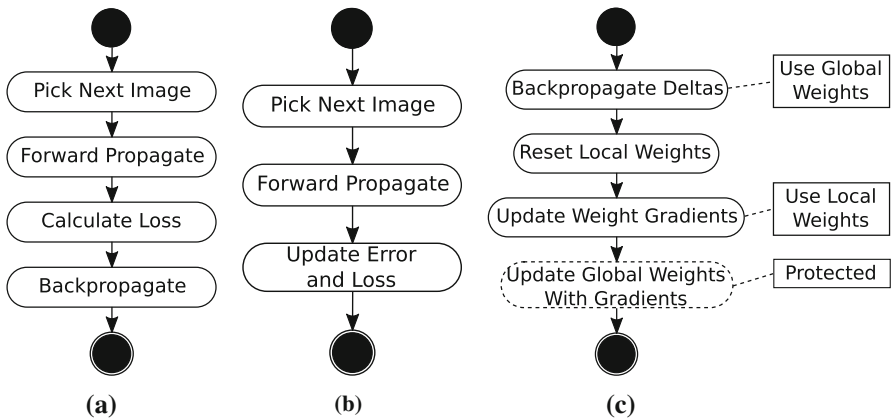
The main goal is to utilize the many cores of the Intel Xeon Phi coprocessor efficiently to lower the training time (execution time) of the selected CNN algorithm, at the same time maintaining low deviation in error rates, especially on the test set. Moreover, the quality of the implementation is verified using errors and error rates on the validation and test set.

In the sequential version, only minor modifications of the original version were performed. Mainly, we added a *Reporter* class to serialize execution results. The instrumentation should not add any time penalties in practice. However, if these penalties occur in the sequential version they are likely to imply corresponding penalties in the parallel version; therefore, it should not impact the results.

The main goal of the parallel version is to lower the execution time of the sequential implementation and to scale well with the number of processing units on the coprocessor. To facilitate this, it is essential to fully consider the characteristics of the underlying hardware. From results derived in the sequential execution, we found the hot spots of the application to be predominantly the convolutional layers. The time spent in both forward- and back-propagation is about 94% of the total time of all layers (up to 99% for the larger network), which is depicted in Table 1.

**Table 1** Execution times at each layer for the sequential version on the Xeon E5 using the small CNN architecture

Layer type	Forward propagation (s)	Back-propagation (s)	% of total
Fully connected	40.9	30.9	1.4
Convolutional	3241	1,438	93.7
Max pooling	188.3	8.2	3.9

**Fig. 4** Detailed phase of training, testing and back-propagation of one image. **a** Training. **b** Testing. **c** Back-propagation

In our proposed strategy, a set of  $N$  network instances are created and assigned to  $T$  threads. We assume  $T = N$ , i.e., one thread per network instance.  $T$  threads are spawned, each responsible for its own instance.

The overview of the algorithm is shown in Fig. 3. In Fig. 4, the training, testing and back-propagation phase are shown in details. Training (see Fig. 4a) picks an image, forward propagates it, determines the loss and back-propagates the partial derivatives (deltas) in the network—this process is done simultaneously by all workers, each worker processing one image. Each worker participating in testing (see Fig. 4b) picks an image, forward propagates it and then collects errors and error rates. The results are cumulated for all threads. Perhaps the most interesting part is the back-propagation (see Fig. 4c). The shared weights are used when propagating the deltas; however, before updating the weight gradients, the pointers are set to the local weights. Thereafter, the algorithm proceeds by updating the local weights first. When a worker has contributions to the global weights, it can update in a controlled manner, avoiding data races. Updates immediately affect other workers in their training process. Hence, the update is delayed slightly, to decrease the invalidation of cache lines, yet almost instant and workers do not have to wait for a longer period before contributing with their knowledge.

To see why delays are important, consider the following scenario: If training several network instances concurrently, they share the same weight vectors, and other variables

are thread private. The major consideration lies in the weight updates. Let  $W_l^j$  be the  $j$ -th weight on the  $l$ -th layer. In accordance with the current implementation, a weight is updated several times since neurons in a map (on the same layer) share the same weights, and the kernel is shifted over the neurons. Further, assume that several threads work on the same weight  $W_l^j$  at some point in time. Even if other threads only read the weights, their local data, as saved in the Level 2 cache, will be invalidated and a re-fetch is required to assert their integrity. This happens because cache lines are shared between cores. The approach of slightly delaying the updates and forcing one thread to update in atomicity leads to fewer invalidations. Still a major disadvantages is that the shared weights does not infer any data locality (data cannot retain completely in Level 2 cache for a longer period).

Listing 1: An extract from the vectorization report for the partial derivative updates in the convolutional layer.

```
remark #15475: --- begin vector loop cost summary ---
remark #15476: scalar loop cost: 30
remark #15477: vector loop cost: 7.500
remark #15478: estimated potential speedup: 3.980
remark #15479: lightweight vector operations: 6
remark #15480: medium-overhead vector operations: 1
remark #15481: heavy-overhead vector operations: 1
remark #15488: --- end vector loop cost summary ---
```

To further decrease the time spent in convolutional layers, loops were vectorized to facilitate the vector processing unit of the coprocessor. Data were allocated using `_mm_malloc()` with 64 byte alignment increasing the accuracy of memory requests. The vectorization was achieved by adding `#pragma omp simd` instructions and explicitly informing the compiler of the memory alignment using `__assume_aligned()`. Some unnecessary overhead is added through the lack of data alignment of the deltas and weights. The computations of partial derivatives and weight gradients in the convolutional layers are performed in a SIMD way, which allows efficient utilization of the 512 bit wide vector processing units of the Intel Xeon Phi. An extract from the vectorization report (see Listing 1), for the updates of partial derivatives in the convolutional layer, shows an estimated potential speedup of  $3.98\times$  compared to the scalar loop.

Further algorithmic optimizations were performed. For example: (1) The images are loaded into a pre-allocated memory instead of allocating new memory when requesting an image. (2) Hardware pre-fetching was applied to mitigate the shortcomings of the in-order-execution scheme. Pre-fetching loads data to L2 cache to make it available for future computations. (3) Letting workers pick images instead of assigning images to workers allows for a smaller overhead at the end of a work-sharing construct. (4) The number of locks is minimized as far as possible. (5) We made most of the variables thread private to achieve data locality.

The training phase was distributed through thread parallelism, dividing the input space over available workers. CHAOS uses the vector processing units to improve performance and tries to retain local variables in local cache as far as possible. The delayed updates decrease the invalidation of cache lines. Since weight parameters are

shared among threads, there is a possibility that data can be fetched from another core's cache instead of main memory, reducing the wait times. Also, the memory was aligned to 64 bytes and unnecessary system calls were removed from the parallel work.

## 5 Evaluation

In this section, we first describe the experimentation environment used for evaluation of our CHAOS parallelization scheme. Thereafter, we describe the development of a performance model for CHAOS. Finally, we discuss the obtained results with respect to scalability, speedup, and prediction accuracy.

### 5.1 Experimental setup

In this study, OpenMP was selected to facilitate the utilization of thread and SIMD parallelism available in the Intel Xeon Phi coprocessor. C++ programming language is used for algorithm implementation. The Intel Compiler 15.0.0 was used for native compilation of the application for the coprocessor, whereas the *O3* level was used for optimization.

*System Configuration* To evaluate our approach, we use an Intel Xeon Phi accelerator that comprises 61 cores that run at 1.2 GHz. For evaluation, 1, 15, 30, 60, 120, 180, 240, and 244 threads of the coprocessor were used. Each thread was responsible for one network instance. For comparison, we use two general purpose CPUs, including the Intel Xeon E5-s695v2 that runs at 2.4 GHz clock frequency, and the Intel Core i5 661 that runs at 3.33GHz clock frequency.

*Data Set* To evaluate our approach, the MNIST [30] dataset of handwritten digits is used. In total the MNIST dataset comprises 70,000 images, 60,000 of which are used for training/validation and the rest for testing.

*CNN Architectures*—Three different CNN architectures were used for evaluation, *small*, *medium* and *large*. The small and medium architecture were trained for 70 epochs, and the large one for 15 epochs, using a starting decay ( $\eta$ ) of 0.001 and factor of 0.9. The small and medium network consist of seven layers in total (one input layer, two convolutional layers, two max-pooling layers, one fully connected layer and the output layer). The difference between these two networks is in the number of feature maps per layer and the number of neurons per map. For example, the first convolutional layer of the small network has five feature maps and 3380 neurons, whereas the first convolutional layer of the medium network has 20 feature maps and 13520 neurons. The large network differs from the small and the medium network in the number of layers as well. In total, there are nine layers, one input layer, three convolutional layers, three max-pooling layers, one fully connected layer and the output layer. Detailed information (including the number and the size of feature maps, neurons, the size of the kernels and the weights) about the considered architectures is listed in Table 2.

To address the variability in performance measurements, we have repeated the execution of each parallel configuration for three times.

**Table 2** CNN architectures for experimental evaluation of CHAOS

	Layer type	Maps	Map size	Neurons	Kernel size	Weights
Large	Input	–	$29 \times 29$	841	–	–
	Convolutional	20	$26 \times 26$	13520	$4 \times 4$	340
	Max-pooling	20	$26 \times 26$	13520	$1 \times 1$	–
	Convolutional	60	$22 \times 22$	29040	$5 \times 5$	30060
	Max-pooling	60	$11 \times 11$	7260	$2 \times 2$	–
	Convolutional	100	$6 \times 6$	3600	$6 \times 6$	216100
	Max-pooling	100	$2 \times 2$	900	$3 \times 3$	–
	Fully connected	–	150	150	–	135150
	Output	–	10	10	–	1510
Medium	Input	–	$29 \times 29$	841	–	–
	Convolutional	20	$26 \times 26$	13520	$4 \times 4$	340
	Max-pooling	20	$13 \times 13$	3380	$2 \times 2$	–
	Convolutional	40	$9 \times 9$	3240	$5 \times 5$	20040
	Max-pooling	40	$3 \times 3$	360	$3 \times 3$	–
	Fully connected	–	150	150	–	54150
	Output	–	10	10	–	1510
	Small	Input	–	$29 \times 29$	841	–
Convolutional	5	$26 \times 26$	3380	$4 \times 4$	85	
Max-pooling	5	$13 \times 13$	845	$2 \times 2$	–	
Convolutional	10	$9 \times 9$	810	$5 \times 5$	1260	
Max-pooling	10	$3 \times 3$	90	$3 \times 3$	–	
Fully connected	–	50	50	–	4550	
Output	–	10	10	–	510	

## 5.2 Performance model

A performance model [40] enables us to reason about the behavior of an implementation in future execution contexts. Our performance model for CHAOS implementation can predict the performance for numbers of threads that go beyond the number of hardware threads supported in the Intel Xeon Phi model that we used for evaluation. Additionally, it can predict the performance of different CNN architectures with various number of images and epochs.

The goal is to construct a parametrized model with the following parameters  $ep$ ,  $i$ ,  $it$  and  $p$ , where  $ep$  stands for the number of epochs,  $i$  indicates the number of images in the training/validation set,  $it$  stands for the number of images in the test set, and  $p$  is the number of processing units. Table 3 lists the full set of variables used in our performance model, some of which are hardware dependent and some others are independent of the underlying hardware. Each variable is either measured, calculated, constant, or parameter in the model. Listing 2 shows the formula used for our performance prediction model.



Listing 2: The formula for our performance prediction model.

$$\begin{aligned}
 T(i, it, ep, p, s) &= T_{comp}(i, it, ep, p, s) + T_{mem}(ep, i, p) \\
 &= \left( \frac{Prep + 4 * i + 2 * it + 10 * ep}{s} \right. && \text{(sequential work)} \\
 &+ \left( \left( \frac{FProp + BProp}{s} \right) * \frac{i}{p_i} * ep \right) && \text{(training)} \\
 &+ \left( \left( \frac{FProp}{s} \right) * \frac{i}{p_i} * ep \right) && \text{(validation)} \\
 &+ \left( \left( \frac{FProp}{s} \right) * \frac{it}{p_{it}} * ep \right) && \text{(testing)} \\
 & * CPI \Big) * OperationFactor + T_{mem}(ep, i, p)
 \end{aligned}$$

The total execution time ( $T$ ) is the sum of computations time ( $T_{comp}$ ) and memory operations ( $T_{mem}$ ).  $T$  depends on several factors including: speed, number of processing units, communication costs (such as network latency), and memory contention. The  $T_{comp}$  is sum of sequential work, training, validation, and testing. Most interesting is contentions causing wait times, including memory latencies and synchronization overhead.  $T_{mem}$  adds memory and synchronization overheads. The contention is measured through an experimental approach by executing a small script on the coprocessor for different thread counts, weights, and layers.

We define  $T_{mem}(ep, i, p) = \frac{MemoryContention * ep * i}{p}$  where  $MemoryContention$  is the measured memory contention when  $p$  threads are fighting for the I/O weights concurrently. Table 4 depicts the measured and predicted memory contentions for the Intel Xeon Phi.

Our performance prediction model is not concerned with any practical measurements except for  $T_{mem}$ . Along with the  $CPI$  and  $OperationFactor$ , it is possible to derive the number of instructions (theoretically) per cycle that each thread can perform.

We use  $Prep$  to be different for each CNN architecture ( $10^9, 10^{10}$  and  $10^{11}$  for small, medium, and large architecture respectively). The  $OperationFactor$  is adjusted to closely match the measured value for 15 threads, and mitigate the approximations done for instructions in the first place, at the same time account for vectorization.

When one hardware thread is present per core, one instruction per cycle can be assumed. For 4 threads per core, only 0.5 instructions per cycle can be assumed, which means that each thread gets to execute two instructions every fourth cycle ( $CPI$  of 2) and hence we use the  $CPI$  factor to control the best theoretical amount of instructions a thread can retire. The speed  $s$  is defined in Table 3.  $FProp$  and  $BProp$  are placeholders for the actual number of operations.

**Table 3** Variables used in the performance model

Variable	Values	Explanation
Parameters		
$p$	1-3,840	Number of processing units/threads
$i$	60,000	Number of training/validation images
$it$	10,000	Number of test images
$ep$	70 (small, medium), 15 (large)	Number of epochs
Constants—hardware dependent		
$CPI$	1-2 threads:1 3 threads:1.5 4 threads:	Best theoretical CPI/thread
$s$	1.238 GHz	Speed of processing unit
OperationFactor	15	Operation factor
Measured—hardware dependent		
MemoryContention	see Table 4	Memory contention
$T_{Fprop}^+$	Small: 1.45 Medium: 12.55 Large: 148.88	Forward propagation / image (ms)
$T_{Bprop}^+$	Small: 5.3 Medium: 69.73 Large: 859.19	Back-propagation / image (ms)
$T_{Prep}^+$	Small: 12.56 Medium: 12.7 Large: 13.5	Time for preparations (s)
Calculated—hardware independent		
FProp*	Small: 58,000 Medium: 559,000* Large: 5,349,000	# FProp Operations / image
BProp*	Small: 524,000 Medium: 6,119,000 Large: 73,178,000	# BProp Operations / image
Prep*	Small: $10^9$ Medium: $10^{10}$ Large: $10^{11}$	# Operations carried out for preparations

\* The parameter is only used in prediction a)

+ The parameter is only used in prediction b)

### 5.3 Results

In this section, we analyze the collected data with regards to the execution time and speedup for varying number of threads and CNN architectures. The errors and error

**Table 4** Measured and predicted memory contention for the Intel Xeon Phi

# Threads	Small	Medium	Large
1	$7.10 \times 10^{-6}$	$1.56 \times 10^{-4}$	$8.83 \times 10^{-4}$
15	$6.40 \times 10^{-4}$	$2.00 \times 10^{-3}$	$8.75 \times 10^{-3}$
30	$1.36 \times 10^{-3}$	$3.97 \times 10^{-3}$	$1.67 \times 10^{-2}$
60	$3.07 \times 10^{-3}$	$8.03 \times 10^{-3}$	$3.22 \times 10^{-2}$
120	$6.76 \times 10^{-3}$	$1.65 \times 10^{-2}$	$6.74 \times 10^{-2}$
180	$9.95 \times 10^{-3}$	$2.50 \times 10^{-2}$	$1.00 \times 10^{-1}$
240	$1.40 \times 10^{-2}$	$3.83 \times 10^{-2}$	$1.38 \times 10^{-1}$
480*	$2.78 \times 10^{-2}$	$7.31 \times 10^{-2}$	$2.73 \times 10^{-1}$
960*	$5.60 \times 10^{-2}$	$1.47 \times 10^{-1}$	$5.46 \times 10^{-1}$
1920*	$1.12 \times 10^{-1}$	$2.95 \times 10^{-1}$	1.09
3840*	$2.25 \times 10^{-1}$	$5.91 \times 10^{-1}$	2.19

\* Predicted values

rates (incorrect predictions) are used to validate our implementation. Furthermore, we discuss the deviation in number of incorrectly predicted images.

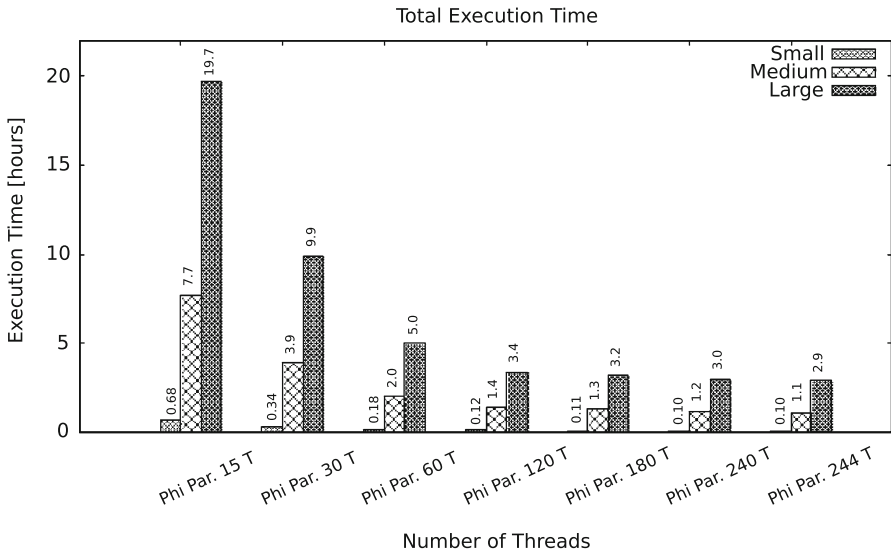
The execution time is the total time the algorithm executes, excluding the time required to initialize the network instances and images (for both the sequential and parallel version). The speedup is measured as the relativeness between two execution times, with the sequential execution times of Intel Xeon E5, Intel Core i5, and Xeon Phi as the base. The error rate is the fraction of images the network was unable to predict and the error the cumulated loss from the loss function.

In the figures and tables in this section, we use the following notations: *Par* refers to the parallel version, *Seq* is the sequential version, and *T* denotes threads, e.g., *Phi Par. 1 T* is the parallel version and one thread on the Xeon Phi.

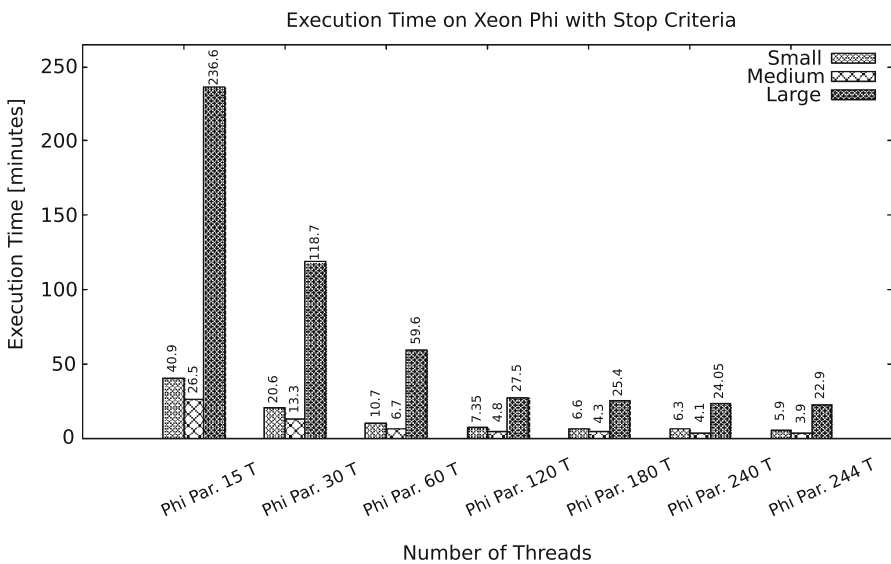
**Result 1** *The CHAOS parallelization scheme scales gracefully to large numbers of threads.*

Figure 5 depicts the total execution time of the parallel version of the implementation running on the Xeon Phi and the sequential version running on the Xeon E5 CPU. We vary the number of threads on the Xeon Phi between 1, 15, 30, 60, 120, 180, 240, and 244, and the CNN architectures between *small*, *medium* and *large*. We elide the results of *Xeon E5 Seq.* and *Phi Par. 1 T* for simplicity and clarity. The large CNN architecture requires 31.1 hours to be completed sequentially on the Xeon E5 CPU, whereas using one thread on the Xeon Phi requires 295.5 hours. By increasing the number of threads to 15, 30, and 60, the execution time decreases to 19.7, 9.9, and 5.0 hours, respectively. Using the total number of threads (that is 244) on the Xeon Phi, the training may be completed in only 2.9 hours. We may observe a promising scalability while increasing the number of threads. Similar results may be observed for the small and medium architecture.

It should be considered that the selected CNN architectures were trained for different number of epochs and that larger networks tend to produce better predictions (lower error rates). A fairer comparison would be to compare the execution times until reaching a specific error rate on the test set. In Fig. 6, the total execution times for the



**Fig. 5** Total execution time for the parallel version executed on the Intel Xeon Phi and the sequential version executed on the Intel Xeon E5



**Fig. 6** Total execution time for the parallel version executed on the Intel Xeon Phi by setting a stop criteria as the error rate is  $\leq 1.54\%$

different CNN architectures and threads on the Xeon Phi is shown. We have set the stop criteria as the *error rate*  $\leq 1.54\%$ , which is the ending error rate of the test set for the small architecture. The large network executes for a longer period even if it converges in fewer epochs and that the medium network needs less time to reach an equal (or better) ending error rate than the small and large network. Note that several

**Table 5** Average time spent on each layer for the large CNN architecture

	BPF <sup>a</sup>		BPC <sup>b</sup>		FPC <sup>c</sup>		FPF <sup>d</sup>	
	Sec	%	Sec	%	Sec	%	Sec	%
<i>Phi Par. 244 T</i>	7.8	1.36	506.2	88.48	54.7	9.56	0.23	0.04
<i>Phi Par. 240 T</i>	8.1	1.34	532.2	88.45	87.8	9.61	0.24	0.04
<i>Phi Par. 180 T</i>	9.0	1.41	557.9	87.78	64.8	10.20	0.26	0.04
<i>Phi Par. 120 T</i>	11.3	1.63	598.4	86.82	75.4	10.94	0.28	0.04
<i>Phi Par. 60 T</i>	19.5	1.91	877.7	86.19	114.4	11.23	0.47	0.05
<i>Phi Par. 30 T</i>	34.7	1.71	1,749	86.36	228.3	11.27	0.94	0.05
<i>Phi Par. 15 T</i>	60.8	1.50	3,495	86.52	456.9	11.31	1.90	0.05
<i>Phi Par. 1 T</i>	836.7	1.38	52,387	86.60	6,859	11.34	29.75	0.05
<i>Xeon E5 Seq.</i>	30.2	0.19	7,097	44.51	8714	54.66	17.04	0.11

<sup>a</sup> Back-propagation in fully connected layers

<sup>b</sup> Back-propagation of convolutional layers

<sup>c</sup> Forward propagation of convolutional layers

<sup>d</sup> Forward propagation in fully connected layers

other factors impact training, including the starting decay, the factor which the decay is decreased, dataset, loss function, preparation of images, initial weight values. Therefore, several combinations of parameters need to be tested before finding a balance. In this study, we focus on the number of epochs as the stop criteria and draw conclusions from this, considering the deviation of the error and error rates.

**Result 2** *The total execution time is strongly influenced by the forward propagation and back-propagation in the network. The convolutional layers are the most computationally expensive.*

Table 5 depicts the time spent per layer for the large CNN architecture. The results were gathered as the total time spent for all network instances on all layers together. Dividing the total time by the number of network instances and later the number of epochs yields the number of seconds spent on each layer per network instance and epoch. A lower time spent on each layer per epoch and instance indicates on a speedup. We may observe that the large architecture spends almost all the time in the convolutional layers and almost no time in the other layers. For *Phi Par. 240 T* about 88% is spent in the back-propagation of convolutional layers and about 10% in forward propagation. We have observed similar results for small and medium CNN architecture; however, we elide these results for space.

We have observed that the more threads involved in training the more percentage of the total time each thread spends in the back-propagation of the convolutional layer, and less time in the others. Overall, the time spent at each layer is decreased per thread when increasing the number of threads. Therefore, there is an interesting relationship between the layer times and the speedup of the algorithm.

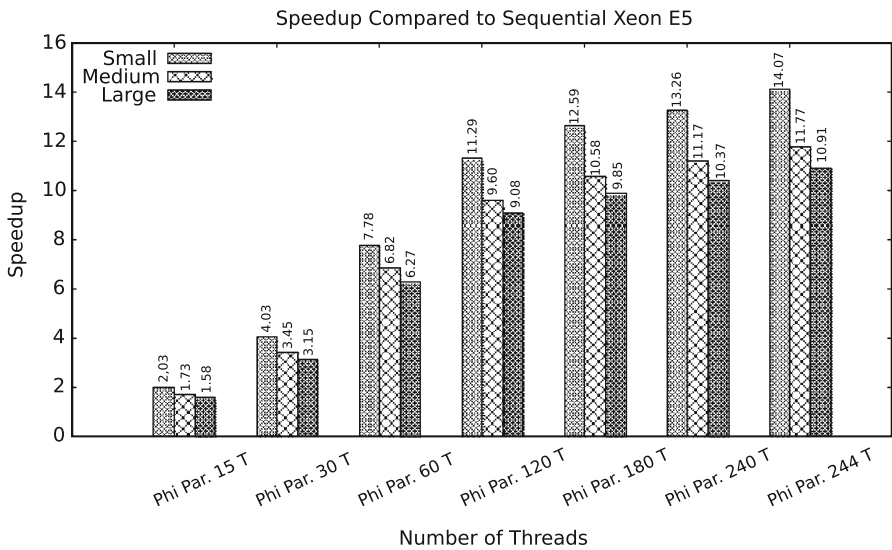
Table 6 presents the speedup relative to the *Phi Par. 1 T* for the different architectures on the convolutional layer. The times are collected by each network instance (through

**Table 6** Averaged layer speedup compared to the *Phi Par. 1 T*

	BPC-S <sup>a</sup>	BPC-M <sup>a</sup>	BPC-L <sup>a</sup>	FPC-S <sup>b</sup>	FPC-M <sup>b</sup>	FPC-L <sup>b</sup>
<i>Phi Par. 244 T</i>	102.0	99.3	103.5	122.3	124.2	125.4
<i>Phi Par. 240 T</i>	96.5	94.1	98.4	114.3	117.3	118.7
<i>Phi Par. 180 T</i>	91.8	89.5	93.9	106.3	107.0	105.8
<i>Phi Par. 240 T</i>	82.7	82.4	87.5	91.0	91.0	91.0
<i>Phi Par. 60 T</i>	56.9	58.9	59.7	58.6	60.1	60.0
<i>Phi Par. 30 T</i>	29.2	29.6	29.9	29.8	30.2	30.1
<i>Phi Par. 15 T</i>	14.7	14.8	15.0	14.9	15.1	15.0

<sup>a</sup> Back-propagation of convolutional layers—small, medium, large CNN

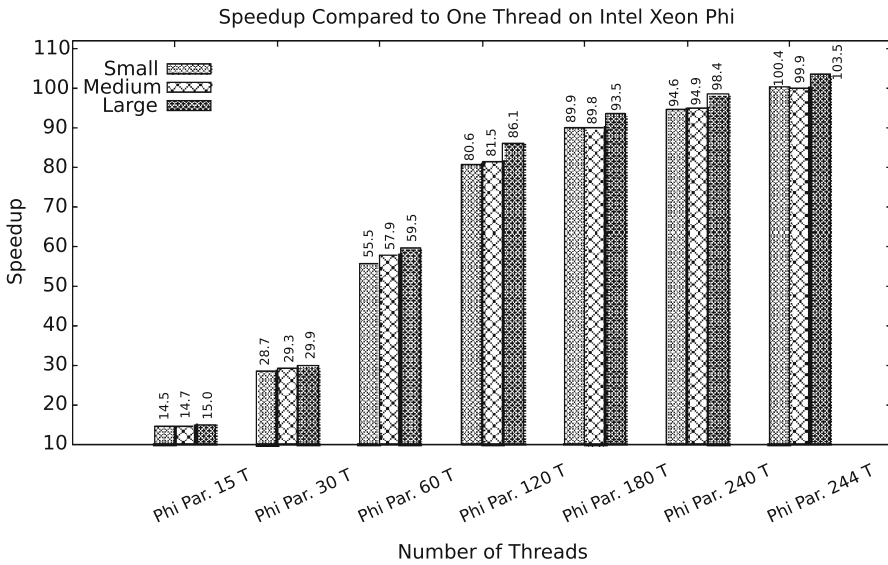
<sup>b</sup> Forward propagation of Convolutional layers—small, medium, large CNN



**Fig. 7** Speedup of the three CNN architectures by varying the number of threads compared to the sequential execution on Intel Xeon E5

instrumentation of the forward- and back-propagate function) and averaged over the number of network instances and epochs. As can be seen, in almost all cases there is an increase in speedup when increasing the network size, and more importantly, the speedup does not decrease. Maybe the most interesting phenomena is that the speedup per layer have an almost direct relationship to the speedup of the algorithm, especially if compared to the back-propagation part. This emphasizes the importance of reducing the time spent in the convolutional layers.

**Result 3** Using CHAOS parallel implementation for training of CNNs on Intel Xeon Phi, we achieved speedups of up to 103 $\times$ , 14 $\times$ , and 58 $\times$  compared to the single-thread performance on Intel Xeon Phi, Intel Xeon E5 CPU, and Intel Core i5, respectively.

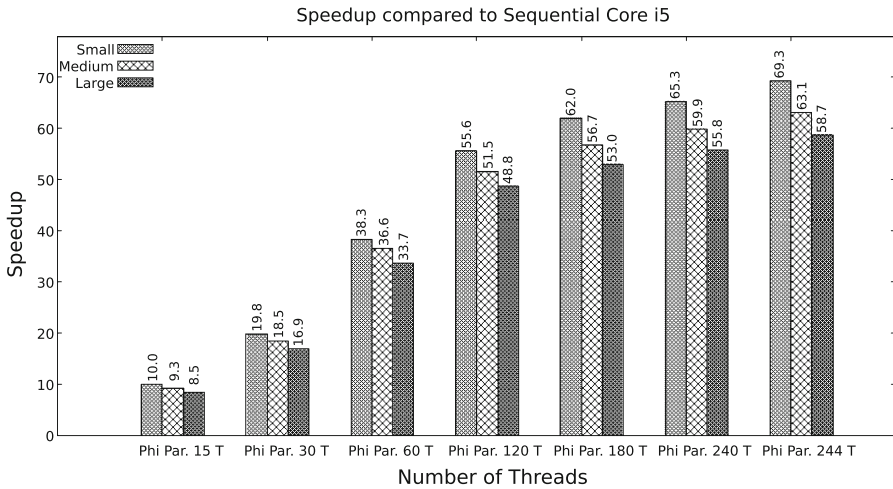


**Fig. 8** Speedup of the three CNN architectures by varying the number of threads compared to one thread on Intel Xeon Phi

Figures 7 and 8 emphasize the facts shown in Fig. 5 in terms of speedup. Figure 7 depicts the speedup compared to the sequential execution on Xeon E5 (*Xeon E5 Seq.*) for various number of threads and CNN architectures. As can be seen, adding more threads results in speedup increase in all cases. Using 240 threads on the Xeon Phi infer a  $13.26\times$  speedup for the small CNN architecture. Utilizing the last core of the Xeon Phi, which is used by the OS, shows even higher speedup ( $14.07\times$ ). We may observe that doubling the number of threads from 15, to 30, and from 30 to 60 almost doubles the speedup (2.03, 4.03, and 7.78). Increasing the number of threads further results with significant speedup, but the double speedup trend breaks.

Figure 8 shows the speedup compared to the execution running in one thread of the Xeon Phi (*Phi Par. 1 T*) while varying the number of threads and the CNN architectures. We may observe that the speedup is close to linear for up to 60 threads for all CNN architectures. Increasing the number of threads further results with significant speedup. Moreover, it can be seen that when keeping the number of threads fixed and increasing the architecture size, the speedup increases with a small factor as well, except for 244 threads. It seems like larger architectures are beneficial. However, it could also be the case that *Phi Par. 1 T* executes relatively slower than *Xeon E5 Seq.* for larger architectures than for smaller ones.

Figure 9 shows the speedup compared to the sequential version executed in Intel Core i5 (*Core i5 Seq.*) while varying the number of threads and the CNN architectures. We may observe that using 15 threads we gain  $10\times$  speedup. Doubling the number of threads to 30, and then to 60 results with close to double speedup increase ( $19.8$  and  $38.3$ ). By using 120 threads (that is two threads per core), the trend of double speedup increase breaks ( $55.6\times$ ). Increasing the number of threads per core to three and four results with modest speedup increase ( $62\times$  and  $65.3\times$ ).



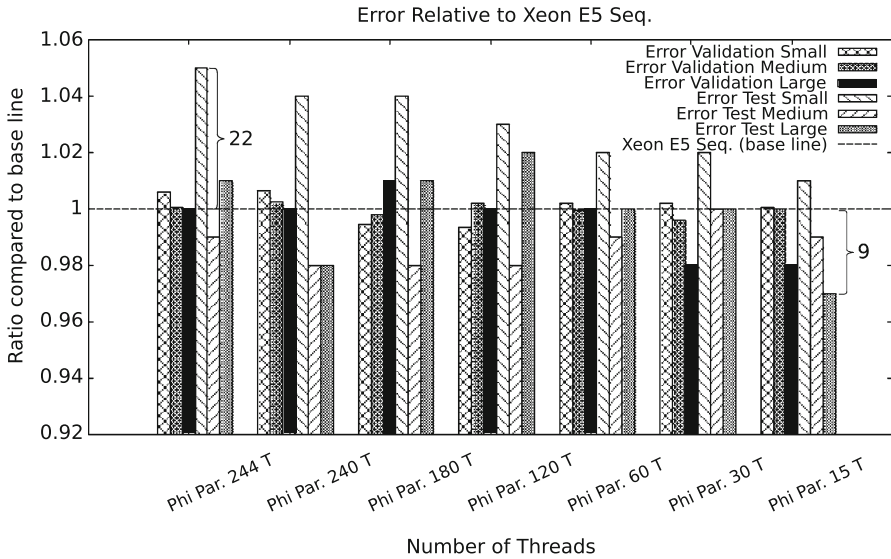
**Fig. 9** Speedup of the three CNN architectures by varying the number of threads compared to one thread on Intel Core i5

**Result 4** *The image classification accuracy of parallel implementation using CHAOS is comparable to the one running sequentially. The deviation error and the number of incorrectly predicted images is not abundant.*

We validate the implementation by comparing the error and error rates for each epoch and configuration. Figure 10 depicts the ending errors for the three considered CNN architectures for both validation and test set. The black dashed line delineates the base line (that is a ratio of 1). Values below the line are considered better, whereas those above the line are worse than for *Xeon E5 Seq.* As a base line, we use the *Xeon E5*; however, identical results are derived executing the sequential version on any platform. As can be seen in Fig. 10, the largest difference is encountered by *Phi Par. 244 T*, about 22 units (0.05%) worse than the base line. On the contrary, *Phi Par. 15 T* has 9 units lower error compared to the base line for the large test set. The validation sets are rather stable, whereas the test set fluctuates more heavily. Although one should consider the deviation in error respectfully, they are not abundant in this case. Please note that the diagram has a high zoom factor and hence the differences are magnified.

Table 7 lists the number of incorrectly classified images for each CNN architecture. For each architecture, the total (*Tot*) number of images and the difference (*Diff*) compared to the optimal numbers of *Xeon E5 Seq.* are shown. Negative values indicate that the ending error rate was better than optimal (less images were incorrectly predicted), whereas positive values indicate that more images than *Xeon E5 Seq.* were incorrectly predicted. For each column in the table, *best* and *worst* values are annotated with *underline* and *bold* fonts, respectively. No obvious pattern can be found; however, increasing the number of threads does not lead to worse prediction in general. *Phi Par. 180 T* stands out as it was 17 images better than *Xeon E5 Seq.* for small architecture on validation set. *Phi Par. 15 T* also performs worst on the small architecture on the validation set. The overall worst performance is achieved by *Phi par. 120 T* on the test set for small CNN architecture. Please note that the total number of images in the





**Fig. 10** Relative cumulative error (loss) for the three considered CNN architectures (small, medium, and large) for both validation and test set

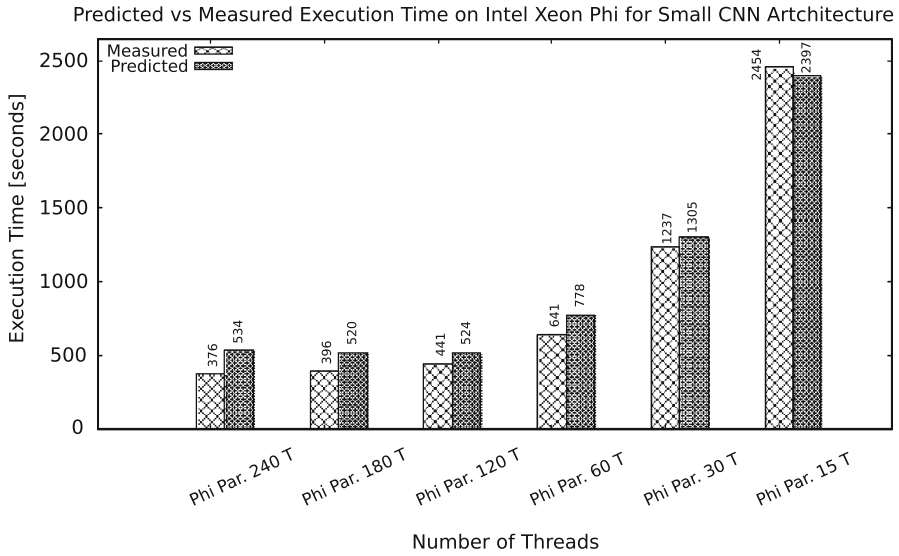
**Table 7** Number of incorrectly classified images for different CNN architectures

# of Phi threads	Validation						Test					
	Small		Medium		Large		Small		Medium		Large	
	Tot	Diff	Tot	Diff	Tot	Diff	Tot	Diff	Tot	Diff	Tot	Diff
244	616	4	85	1	12	2	155	2	98	3	<b>95</b>	<b>1</b>
240	610	-2	86	2	11	1	154	1	<u>95</u>	<u>0</u>	91	-3
180	<u>595</u>	<u>-17</u>	<b>87</b>	<b>3</b>	<b>12</b>	<b>2</b>	158	5	98	3	95	1
120	607	-5	83	-1	11	1	<b>159</b>	<b>6</b>	95	0	94	0
60	615	3	<u>81</u>	<u>-3</u>	11	1	156	3	98	3	91	-3
30	612	0	83	-1	<u>10</u>	<u>0</u>	156	3	98	3	90	-5
15	<b>617</b>	<b>5</b>	84	0	<u>10</u>	<u>0</u>	<u>153</u>	<u>0</u>	<b>100</b>	<b>5</b>	<u>84</u>	<u>-10</u>

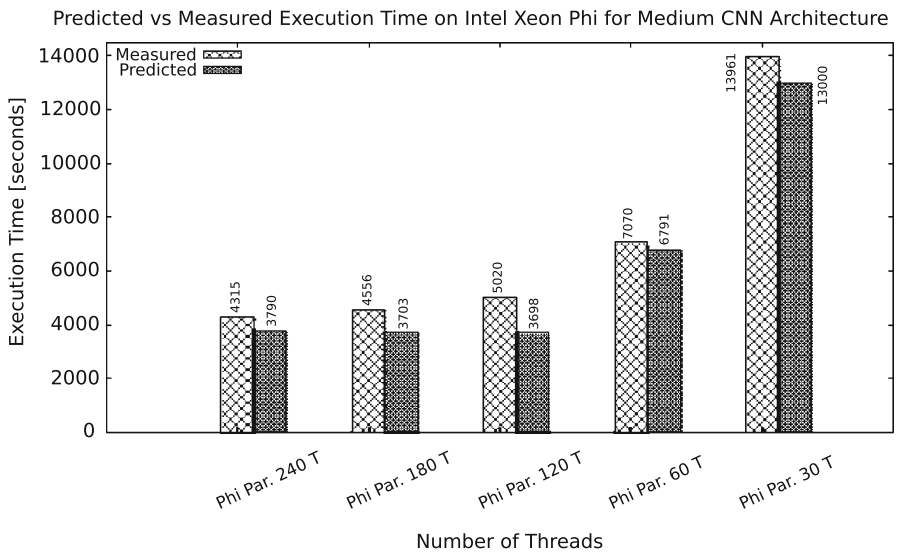
validation set is 60, 000 and 10, 000 for the test set. Overall, the number of incorrectly predicted images and the deviation from the base line is not abundant.

**Result 5** *The predicted execution times obtained from the performance model match well the measured execution times.*

Figures 11, 12, and 13 depict the predicted and measured execution times for small, medium, and large CNN architecture. For the small network (see Fig. 11), the predictions are close to the measured values with a slight deviation at the end. The prediction model seems to overestimate the execution time with a small factor.



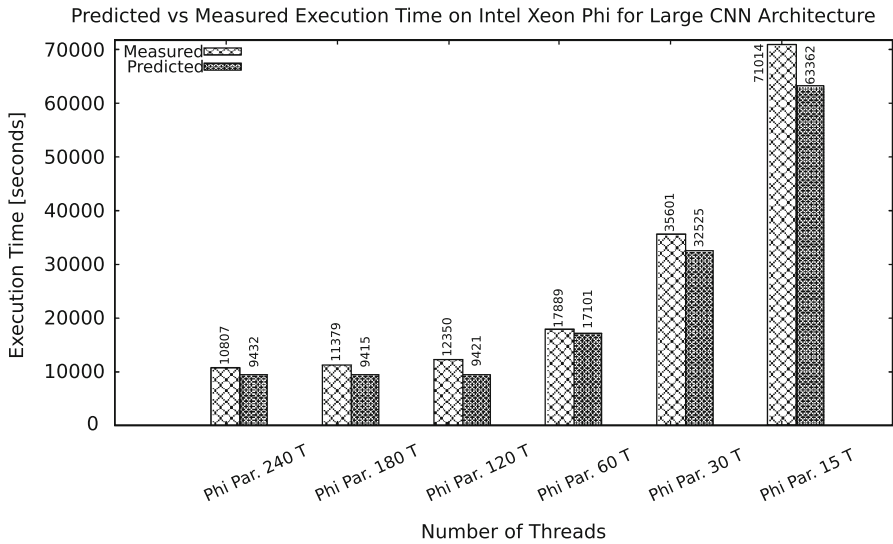
**Fig. 11** Comparison between the predicted execution time and the measured execution time on Intel Xeon Phi for the small CNN architecture



**Fig. 12** Comparison between the predicted execution time and the measured execution time on Intel Xeon Phi for the medium CNN architecture

For the medium architecture (see Fig. 12), the prediction follow the measured values closely, although it underestimates the execution time slightly. At 120 threads, the measured and predicted values starts to deviate, which are recovered at 240 threads.

The large architecture yields similar results as the medium. As can be seen, the measured values are slightly higher than the predictions; however, the predictions



**Fig. 13** Comparison between the predicted execution time and the measured execution time on Intel Xeon Phi for the large CNN architecture

follow the measured values. As can be seen for 120 threads, there is a deviation which is recovered for 240 threads. Also, the predictions increase between 120 and 180, and 180 and 240 threads for both predictions, whereas the actual execution time is lowered. This is most probably due to the CPI factor that is added when 3 or more threads are present on the same core. We use the expression  $x = \frac{|m - p|}{p}$  to calculate the deviation in predictions for our prediction model and all considered architectures, where  $m$  is the measured and  $p$  is the predicted value. The average deviations over all measured thread counts are as follows: 14.57% for the small CNN, 14.76% for medium, and 15.36% for large CNN.

**Result 6** *Prediction of execution time for number of threads that go beyond the 240 hardware threads of the model of Intel Xeon Phi used in this paper show that CHAOS scales well up to several thousands of threads.*

We used the prediction model to predict the execution times for 480, 960, 1920, and 3840 threads for different CNN architectures, using the same parameters. The results in Table 8 show that if 3,840 threads were available, the small network should take about 4.6 minutes to train, the medium 14.5 minutes, and the large 36.8 minutes. The predictions for the large CNN architecture are not as well aligned when increasing to larger thread counts as for small and medium.

Additionally, we evaluated the execution time for varying image counts, and epochs, for 240 and 480 threads for the small CNN architecture. As can be seen in Table 9, doubling the number of images or epochs, approximately doubles the execution time. However, doubling the number of threads does not reduce the execution time in half.

**Table 8** Predicted execution times (min) for 480, 960, 1,920, and 3,840 threads using the performance models

# Threads	480	960	1920	3,840
Small CNN	6.6	5.4	4.9	4.6
Medium CNN	36.8	23.9	17.4	14.2
Large CNN	92.9	60.8	44.8	36.8

**Table 9** Execution times in minutes when scaling epochs and images for 240 and 480 threads using the performance model on the small CNN architecture

240 threads						480 threads			
Images		Epochs				Epochs			
$i^a$	$it^b$	70	140	280	560	70	140	280	560
60k	10k	8.9	17.6	35.0	69.7	6.6	12.9	25.6	51.1
120k	20k	17.6	35.0	69.7	139.3	12.9	25.6	51.1	101.9
240k	40k	35.0	69.7	139.3	278.3	25.6	51.1	101.9	203.6

<sup>a</sup> Number of images in the training/validation set

<sup>b</sup> Number of images in the test set

## 6 Summary and future work

Deep learning is important for many modern applications, such as voice recognition, face recognition, autonomous cars, precision medicine, or computer vision. We have presented CHAOS that is a parallelization scheme to speedup the training process of convolutional neural networks. CHAOS can exploit both thread and SIMD parallelism of Intel Xeon Phi coprocessor. Moreover, we have described our performance prediction model, which we use to evaluate our parallelization solution and infer the performance on future architectures of the Intel Xeon Phi. Major observations include,

- CHAOS parallel implementation scales well with the increase of the number of threads;
- convolutional layers are the most computationally expensive part of the CNN training effort; for instance, for 240 threads, 88% of the time is spent on the back-propagation of convolutional layers;
- using CHAOS for training CNNs on Intel Xeon Phi, we achieved up to 103 $\times$ , 14 $\times$ , and 58 $\times$  speedup compared to the single-thread performance on Intel Xeon Phi, Intel Xeon E5 CPU, and Intel Core i5, respectively;
- image classification accuracy of CHAOS parallel implementation is comparable to the one running sequentially;
- predicted execution times values obtained from our performance model match well the measured execution times;
- results of the performance model indicate that CHAOS scales well beyond the 240 hardware threads of the Intel Xeon Phi that is used in this paper for experimentation.

Future work will extend CHAOS to enable the use of all cores of host CPUs and the coprocessor(s).

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## References

1. Abadi M et al (2015) TensorFlow: large-scale machine learning on heterogeneous systems. Software <http://tensorflow.org/>
2. Ahmed K, Qiu Q, Malani P, Tamhankar M (2014) Accelerating pattern matching in neuromorphic text recognition system using intel xeon phi coprocessor. In: International Joint Conference on Neural Networks (IJCNN), 2014, IEEE, pp 4272–4279
3. Andrew N, Jiquan N, Chuan Yu F, Yifan M, Caroline S (2011) Ufldl tutorial on neural networks
4. Bahrampour S, Ramakrishnan N, Schott L, Shah M (2015) Comparative study of deep learning software frameworks. arXiv preprint [arXiv:1511.06435](https://arxiv.org/abs/1511.06435)
5. Benkner S, Pllana S, Traff J, Tsigas P, Dolinsky U, Augonnet C, Bachmayer B, Kessler C, Moloney D, Osipov V (2011) PEPPIER: efficient and productive usage of hybrid computing systems. IEEE Micro 31(5):28–41
6. Chang CC, Lin CJ (2011) Libsvm: a library for support vector machines. ACM Trans Intell Syst Technol (TIST) 2(3):27
7. Chellapilla K, Puri S, Simard P (2006) High performance convolutional neural networks for document processing. Tenth international workshop on frontiers in handwriting recognition. Suvisoft
8. Chrysos G (2012) Intel Xeon Phi coprocessor-the architecture. Intel Whitepaper. <https://software.intel.com/en-us/articles/intel-xeon-phi-coprocessor-codename-knights-corner>
9. Cireşan D (2017) Simple C/C++ code for training and testing MLPs and CNNs. <http://people.idsia.ch/~cireşan/data/net.zip>. Accessed 14 Feb 2017
10. Cireşan D, Meier U, Masci J, Schmidhuber J (2011) A committee of neural networks for traffic sign classification. In: The 2011 International Joint Conference on Neural Networks (IJCNN), IEEE, pp 1918–1921
11. Cireşan D, Meier U, Masci J, Schmidhuber J (2012) Multi-column deep neural network for traffic sign classification. Neural Netw 32:333–338
12. Cireşan DC, Meier U, Masci J, Gambardella LM, Schmidhuber J (2011) High-performance neural networks for visual object classification. arXiv preprint [arXiv:1102.0183](https://arxiv.org/abs/1102.0183)
13. De Grazia MDF, Stoianov I, Zorzi M (2012) Parallelization of deep networks. In: ESANN 2012 proceedings, 20th European symposium on artificial neural networks, Computational intelligence and machine learning. i6doc.com publication, pp 621–626
14. DeepLearning: convolutional neural networks (LeNet) - DeepLearning 0.1 documentation. <http://deeplearning.net/tutorial/lenet.html> (2016). Accessed 17 March 2016
15. Deng L, Yu D (2014) Deep learning: methods and applications. Found Trends Signal Process 7(3–4):197–387
16. Dokulil J, Bajrovic E, Benkner S, Pllana S, Sandrieser M, Bachmayer B (2013) High-level support for hybrid parallel execution of c++ applications targeting intel xeon phi coprocessors. Procedia Computer Science. 2013 International Conference on Computational Science, vol 18, pp 2508–2511. doi:[10.1016/j.procs.2013.05.430](https://doi.org/10.1016/j.procs.2013.05.430)
17. Fox GC, Jha S, Qiu J, Luckow A (2015) Towards an understanding of facets and exemplars of big data applications. In: Proceedings of the 20 years of beowulf workshop on honor of thomas sterling's 65th birthday, Beowulf '14, ACM, New York, NY, USA, pp 7–16. doi:[10.1145/2737909.2737912](https://doi.org/10.1145/2737909.2737912)
18. Gibansky A (2016) Fully connected neural network algorithms. <http://andrew.gibiansky.com/blog/machine-learning/fully-connected-neural-networks/>. Accessed 21 March 2016
19. Hadsell R, Sermanet P, Ben J, Erkan A, Scoffier M, Kavukcuoglu K, Muller U, LeCun Y (2009) Learning long-range vision for autonomous off-road driving. J Field Robot 26(2):120–144

20. Hsu CH (2014) Editorial. *Future Gener Comput Syst* 36(Complete):16–18. doi:[10.1016/j.future.2014.02.003](https://doi.org/10.1016/j.future.2014.02.003)
21. Jiang P, Winkley J, Zhao C, Munnoch R, Min G, Yang LT (2016) An intelligent information forwarder for healthcare big data systems with distributed wearable sensors. *IEEE Syst J* 10(3):1147–1159. doi:[10.1109/JSYST.2014.2308324](https://doi.org/10.1109/JSYST.2014.2308324)
22. Jin L, Wang Z, Gu R, Yuan C, Huang Y (2014) Training large scale deep neural networks on the intel xeon phi many-core coprocessor. In: *IPDPS Workshops*, IEEE Computer Society, pp 1622–1630
23. Kessler CW, Dastgeer U, Thibault S, Namyst R, Richards A, Dolinsky U, Benkner S, Trff JL, Pillana S (2012) Programmability and performance portability aspects of heterogeneous multi-/manycore systems. In: *2012 Design, Automation Test in Europe Conference Exhibition (DATE)*, IEEE, Dresden, Germany, pp 1403–1408. doi:[10.1109/DATE.2012.6176582](https://doi.org/10.1109/DATE.2012.6176582)
24. Krizhevsky A (2014) One weird trick for parallelizing convolutional neural networks. eprint [arXiv:1404.5997](https://arxiv.org/abs/1404.5997). <https://arxiv.org/abs/1404.5997>. Accessed 2 Mar 2017
25. Krizhevsky A, Hinton G (2009) Learning multiple layers of features from tiny images. Technical Report, University of Toronto. <https://www.cs.toronto.edu/~kriz/learning-features-2009-TR.pdf>. Accessed 2 Mar 2017
26. Krizhevsky A, Sutskever I, Hinton GE (2012) Imagenet classification with deep convolutional neural networks. In: *Advances in neural information processing systems*, pp 1097–1105
27. Langford J, Smola AJ, Zinkevich M (2009) Slow learners are fast. In: *NIPS'09, Proceedings of the 22nd International Conference on Neural Information Processing Systems*. Curran Associates Inc, Vancouver, British Columbia, Canada, pp 2331–2339. <http://dl.acm.org/citation.cfm?id=2984093.2984354>. Accessed 2 Mar 2017
28. LeCun Y, Bengio Y, Hinton G (2015) Deep learning. *Nature* 521(7553):436–444. doi:[10.1038/nature14539](https://doi.org/10.1038/nature14539)
29. LeCun Y, Bottou L, Bengio Y, Haffner P (1998) Gradient-based learning applied to document recognition. *Proc IEEE* 86(11):2278–2324
30. LeCun Y, Cortes C (2010) Mnist handwritten digit database. AT&T Labs [Online]. <http://yann.lecun.com/exdb/mnist>
31. LeCun Y, Huang FJ, Bottou L (2004) Learning methods for generic object recognition with invariance to pose and lighting. In: *Proceedings of the 2004 IEEE Computer Society Conference on Computer Vision and Pattern Recognition*, 2004. CVPR 2004, IEEE, vol 2, pp II–97
32. Leung KC, Eyers D, Tang X, Mills S, Huang Z (2013) Investigating large-scale feature matching using the intel xeon phi coprocessor. In: *2013 28th International Conference of, Image and Vision Computing New Zealand (IVCNZ)*, IEEE, pp 148–153
33. Lu M, Zhang L, Huynh HP, Ong Z, Liang Y, He B, Goh RSM, Huynh R (2013) Optimizing the mapreduce framework on intel xeon phi coprocessor. In: *2013 IEEE International Conference on Big Data*, IEEE, pp 125–130
34. Memeti S, Pillana S (2016) Combinatorial optimization of dna sequence analysis on heterogeneous systems. *Pract Exp Concurr Comput*. doi:[10.1002/cpe.4037](https://doi.org/10.1002/cpe.4037)
35. Memeti S, Pillana S (2016) A machine learning approach for accelerating dna sequence analysis. *The Int J High Perform Comput Appl*. doi:[10.1177/1094342016654214](https://doi.org/10.1177/1094342016654214)
36. Murphy J (2016) Deep learning frameworks: a survey of Tensorflow, Torch, Theano, Caffe, Neon, And The IBM machine learning stack. <https://www.microway.com/hpc-tech-tips/deep-learning-frameworks-survey-tensorflow-torch-theano-caffe-neon-ibm-machine-learning-stack/>. Accessed 17 Feb 2017
37. Najafabadi MM, Villanustre F, Khoshgoftaar TM, Seliya N, Wald R, Muharemagic E (2015) Deep learning applications and challenges in big data analytics. *J Big Data* 2(1):1. doi:[10.1186/s40537-014-0007-7](https://doi.org/10.1186/s40537-014-0007-7)
38. NVIDIA: WhatIsGPU-AcceleratedComputing?. <http://www.nvidia.com/object/what-is-gpu-computing.html> (2016). Accessed 14 Nov 2016
39. Pillana S, Benkner S, Mehofer E, Natvig L, Xhafa F, (2009) Towards an intelligent environment for programming multi-core computing systems. *Euro-Par, 2008 workshops—parallel processing*, vol 5415. *Lecture Notes in Computer Science*. Springer, Berlin, pp 141–151
40. Pillana S, Benkner S, Xhafa F, Barolli L (2008) Hybrid performance modeling and prediction of large-scale computing systems. In: *2008 International Conference on Complex, Intelligent and Software Intensive Systems*, pp 132–138. doi:[10.1109/CISIS.2008.20](https://doi.org/10.1109/CISIS.2008.20)

41. Recht B, Re C, Wright S, Niu F (2011) Hogwild: a lock-free approach to parallelizing stochastic gradient descent. *Advances in Neural Information Processing Systems*, pp 693–701
42. Sainath TN, Kingsbury B, Saon G, Soltan H, Mohamed Ar, Dahl G, B Ramabhadran (2015) Deep convolutional neural networks for large-scale speech tasks. *Neural Netw* 64:39–48
43. Scherer D, Schulz H, Behnke S (2010) Accelerating large-scale convolutional neural networks with parallel graphics multiprocessors. *Artificial neural networks–ICANN 2010*, Springer, pp 82–91
44. Schmidhuber J (2015) Deep learning in neural networks: an overview. *Neural Netw* 61:85–117
45. Sharma S, Tim US, Wong J, Gadia S, Sharma S (2014) A brief review on leading big data models. *Data Sci J* 13:138–157. doi:[10.2481/dsj.14-041](https://doi.org/10.2481/dsj.14-041)
46. Shi S, Wang Q, Xu P, Chu X (2016) Benchmarking state-of-the-art deep learning software tools. arXiv preprint [arXiv:1608.07249](https://arxiv.org/abs/1608.07249)
47. Song I, Kim HJ, Jeon PB (2014) Deep learning for real-time robust facial expression recognition on a smartphone. In: 2014 IEEE International Conference on Consumer Electronics (ICCE), IEEE, pp 564–567
48. Strawn G (2016) Data scientist. *IT Prof* 18(3):55–57. doi:[10.1109/MITP.2016.41](https://doi.org/10.1109/MITP.2016.41)
49. Szegedy C, Liu W, Jia Y, Sermanet P, Reed S, Anguelov D, Erhan D, Vanhoucke V, Rabinovich A (2015) Going deeper with convolutions. In: *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pp 1–9
50. Tabik S, Peralta D, Herrera AHPF (2017) A snapshot of image pre-processing for convolutional neural networks: case study of mnist. *Int J Comput Intell Syst* 10:555–568
51. Taigman Y, Yang M, Ranzato M, Wolf L (2014) Deepface: closing the gap to human-level performance in face verification. In: *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pp 1701–1708
52. Teodoro G, Kurc T, Kong J, Cooper L, Saltz J (2013) Comparative performance analysis of intel xeon phi, gpu, and cpu. arXiv preprint [arXiv:1311.0378](https://arxiv.org/abs/1311.0378)
53. Tian X, Saito H, Preis S, Garcia EN, Kozhukhov S, Masten M, Cherkasov AG, Panchenko N (2013) Practical SIMD vectorization techniques for Intel Xeon Phi coprocessors. *IPDPS workshops*, IEEE, pp. 1149–1158
54. Vrtanoski J, Stojanovski TD (2012) Pattern recognition with opencl heterogeneous platform. *Telecommunications forum (TELFOR)*, 2012 20th, IEEE, pp 701–704
55. Washburn A (2014) Siri Will Soon Understand You a Whole Lot Better | Wired. [http://www.wired.com/2014/06/siri\\_ai/](http://www.wired.com/2014/06/siri_ai/). Accessed 17 March 2016
56. Williams S, Waterman A, Patterson D (2009) Roofline: an insightful visual performance model for multicore architectures. *Commun ACM* 52(4):65–76. doi:[10.1145/1498765.1498785](https://doi.org/10.1145/1498765.1498785)
57. Wu K, Chen X, Ding M (2014) Deep learning based classification of focal liver lesions with contrast-enhanced ultrasound. *Opt Int J Light Electron Opt* 125(15):4057–4063
58. Yadan O, Adams K, Taigman Y, Ranzato M (2013) Multi-gpu training of convnets. arXiv preprint [arXiv:1312.5853](https://arxiv.org/abs/1312.5853) 9
59. You Y, Song SL, Fu H, Marquez A, Dehnavi MM, Barker K, Cameron KW, Randles AP, Yang G (2014) Mic-svm: designing a highly efficient support vector machine for advanced modern multi-core and many-core architectures. In: 2014 IEEE 28th International Parallel and Distributed Processing Symposium, IEEE, pp 809–818
60. Zhang L, Wang L, Wang X, Liu K, Abraham A (2012) Research of neural network classifier based on FCM and PSO for breast cancer classification. Springer, Berlin, pp 647–654