



*Correction*

## Correction to: Hamiltonian and Algebraic Theories of Gapped Boundaries in Topological Phases of Matter

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There were two errors in the original publication. First, the term  $B^K$  in Eq. (2.20) was not well-defined in the case of non-normal subgroups  $K$ ; however, we found out that both the vertex terms  $A^K$  and the plaquette terms  $B^K$  are in fact redundant in Eq. (2.23) given the edge terms. The text from Eqs. (2.19–2.23) should read:

Let us now define some new projector terms, as in Ref. [10]:

$$L^K(e) := \frac{1}{|K|} \sum_{k \in K} \left( L_+^k(e) + L_-^k(e) \right), \quad (0.1)$$

$$T^K(e) := \sum_{k \in K} T_+^k(e) \quad (0.2)$$

The definitions of  $L^k$  and  $T^k$  for Eqs. (0.1–0.2) are based on Eqs. 2.1–2.4. Following Ref. [10], we can now define the following Hamiltonian:

$$H_{(G,1)}^{(K,1)} = \sum_e \left( (1 - T^K(e)) + (1 - L^K(e)) \right) \quad (0.3)$$

With this definition, it is no longer necessary to emphasize whether vertices/plaquettes/edges along the borders of gapped boundaries are contained in the hole; for simplicity, one may assume that the hole consists of all edges along and within the border.

Second, there is an error in Theorem 2.12. The theorem should read:

**Theorem.** Let  $(T, R)$  and  $(C, \pi)$  be given elementary excitations in the boundary and bulk, respectively. The term  $Y_\tau^{(T,R);(\mathbf{u}_2, \mathbf{v}_2)}$  has a nonzero coefficient in the decomposition of  $F_\tau^{(C,\pi);(\mathbf{u}_1, \mathbf{v}_1)}$  (for some quadruple  $(\mathbf{u}_1, \mathbf{v}_1, \mathbf{u}_2, \mathbf{v}_2)$ ) if and only if the following two conditions hold:

- (1) The intersection  $C \cap T$  is nonempty. When this condition holds, it is always possible to choose a double coset representative  $r_T$  that is also in  $C$ . We assume that such a choice is made, and this assumption is important because Eq. (0.7) will give different results otherwise.
- (2) There exists an  $x \in G$  such that the following is true: Let  $x \triangleright \pi$  denote the representation of  $x E(C)x^{-1}$  obtained from  $\pi$  where  $y$  acts as  $x^{-1}yx$ . Let  $\rho_{x \triangleright \pi}$  be the (possibly reducible) representation of the subgroup  $(x E(C)x^{-1}) \cap K^{rT}$  resulting from the restriction of  $x \triangleright \pi$  to  $(x E(C)x^{-1}) \cap K^{rT}$ ; let  $\rho_R$  be the representation of the same subgroup formed by restricting  $R$ . Decompose  $\rho_{x \triangleright \pi}, \rho_R$  into irreducible representations of  $(x E(C)x^{-1}) \cap K^{rT}$ :

$$\rho_{x \triangleright \pi} = \bigoplus_\sigma n_\sigma^{x \triangleright \pi} \sigma \tag{0.4}$$

$$\rho_R = \bigoplus_\sigma n_\sigma^R \sigma \tag{0.5}$$

There must exist some irreducible representation  $\sigma$  of  $(x E(C)x^{-1}) \cap K^{rT}$  such that  $n_\sigma^{x \triangleright \pi} \neq 0$  and  $n_\sigma^R \neq 0$ .

In particular, let  $X(C)$  be a set of representatives of the double cosets  $K \backslash G / E(C)$ . For given  $(C, \pi)$  let us write the decomposition after condensation as

$$(C, \pi) = \bigoplus n_{(T,R)}^{(C,\pi)} (T, R). \tag{0.6}$$

Then, we have

$$n_{(T,R)}^{(C,\pi)} = \sum_{\substack{x \in X(C) \text{ s.t. } xr_c x^{-1} \in T \\ \sigma \in ((x E(C)x^{-1}) \cap K^{rT})_{ir}}} n_\sigma^R n_\sigma^{x \triangleright \pi} \tag{0.7}$$

Furthermore, these coefficients imply that the two sides of Eq. (0.6) will always have the same quantum dimensions.