TWO PROBLEMS IN QUANTIZED ALGEBRAS OF FUNCTIONS

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1. Let $C(K)_q$ be the algebra of functions which are continuous on compact quantum group K (see [1] for definition). It is well known from [1] that there is an imbedding of $C(K)_q$ into the algebra of continuous operator-functions on the maximal torus $T \subset K$. Describe the image. The answer is known for K = SU(2) (see [2]). There is such a description for odd-dimensional quantum spheres (see [3]).

2. Let g be a finite dimensional complex Lie algebra, $C[g^*]$ be an algebra of polynomial functions on dual space g^* . Let us equip $C[g^*]$ with Poisson brackets by using the Lie-Kirillov formulas. Quantization of this Hopf-Poisson algebra is known: it is the universal enveloping algebra U(g). Therefore the usual method of orbit (Konstant-Kirillov) gives rise to the relation between the representation theory of the algebra of functions on the quantum group g^* and symplectic leaves in the Poisson-Lie group g^* (these are coadjoint orbits in our case).

Problem. How to generalize this to the case of more general quantum groups?

I mean the generalization of the method of orbits. The correspondence between representations and leaves was investigated in [1,2] for compact quantum groups.

References

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- [3] L.Vaksman, Ya.Soibelman, Algebra of functions on quantum group SU(n+1) and odd-dimensional quantum spheres, Algebra Anal. 2 no. 5 (1990), 101-120. (in Russian)