

Object Flow Definition for Refined Activity Diagrams

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Abstract. Activity diagrams are a well-known means to model the control flow of system behavior. Their expressiveness can be enhanced by using their object flow notation. In addition, we refine activities by pairs of pre- and post-conditions formulated by interrelated object diagrams. To define a clear semantics for refined activity diagrams with object flow, we use a graph transformation approach. Control flow is formalized by sets of transformation rule sequences, while object flow is described by partial dependencies between transformation rules. This approach is illustrated by a simple service-based on-line university calendar.

1 Introduction

UML2 activity diagrams are a well-known means to model the control flow of system behavior. Their expressiveness can be enhanced by using their object flow notation. Currently, it is an open problem how to formalize coherent object flow for activity diagrams. In this paper we aim at providing a precise semantics for refined activity diagrams with coherent object flow. We use graph transformation as semantic domain, since it supports the integration of structural and behavioral aspects and provides different analysis facilities.

In [1], sufficient criteria for the consistency of *refined* activity diagrams were provided, where interrelated object diagrams are used to specify pre- and post conditions of single activities. All conditions refer to a domain class model. This refinement serves as a basis for consistency analysis. The refinement of activities by pre- and post-conditions was first introduced in [2] to analyze inconsistencies between individual activities refining use cases. Pre- and post conditions are formalized as graph transformation rules. Mehner et.al. extend the consistency analysis in [3] where also the control flow is taken into account. In [4], a similar approach for consistent integration of life sequence charts (LSCs) with graph transformation, applied to service composition modeling, was developed. The formalization based on graph transformation is used to analyze rule sequences. In addition, data flow is modeled textually by name equality for input and output variables.

In this paper, we extend refined activity diagrams by object flow. We introduce partial rule dependencies to formalize the semantics of object flow. Based on the consistency

notion of refined activity diagrams in [1], we define consistency-related properties of refined activity diagrams with object flow.

We illustrate our approach with an example from model-driven development of a service-based web university calendar. In particular the behavior modeling of individual services still lacks advanced support for precise modeling and subsequent consistency analysis. Activity diagrams are an adequate means for modeling individual services, and the use of object flow and pre-/post-conditions can define service behavior more precisely.

This paper is organized as follows. Section 2 introduces the syntax and semantics of refined activity diagrams with object flow informally. Section 3 introduces algebraic graph transformations and the new notion of partial rule dependency. Section 4 presents the semantics and consistency notion of refined activity diagrams and extends it for object flow. Sections 5 and 6 contain related work and concluding remarks.

2 Introduction to Refined Activity Diagrams with Object Flow

This section introduces refined activity diagrams with object flow and illustrates this modeling approach by a small example for a service-based web university calendar. In this example, we model services by activity diagrams with object flow where each activity is refined by pre- and post-conditions, and guards are refined by patterns.

2.1 Domain Model

Our example application manages course parts that are lectures, laboratories, and exercises where a lecture may offer a laboratory and an exercise. Each course part is held by a lecturer and can be located in a room. An appropriate class diagram is presented in Fig. 1. From an abstract class *Object*¹, three classes are derived: *Room*, *Lecturer* and *CoursePart*. The latter is abstract and is specialized by three further classes: *Laboratory*, *Exercise* and *Lecture*. Day and time information for course parts are realized by enumerations *Day* and *Time*.

2.2 Activity Diagrams with Object Flow

We use UML2 activity diagrams with object flow [5] to model services of the university calendar. Three services, *AddLecture*, *AddExercise*, and *AddLaboratory*, are shown exemplarily in Fig. 2.

Web applications usually contain a number of services. A service provides a clearly defined logical unit of functionality based on data entities. While a basic service might be realized by one activity only, more complex services might contain a number of different activities. Defining services by the means of hierarchical activity diagrams opens up the possibility to call services from other ones. The usage of other services is depicted by placing a complex activity as representation of the used service into the control flow. The invocation of a complex activity is indicated by placing a rake-style symbol within the activity node. Our example service *AddLecture* uses two other

¹ Italic class names in diagrams indicate abstract classes.

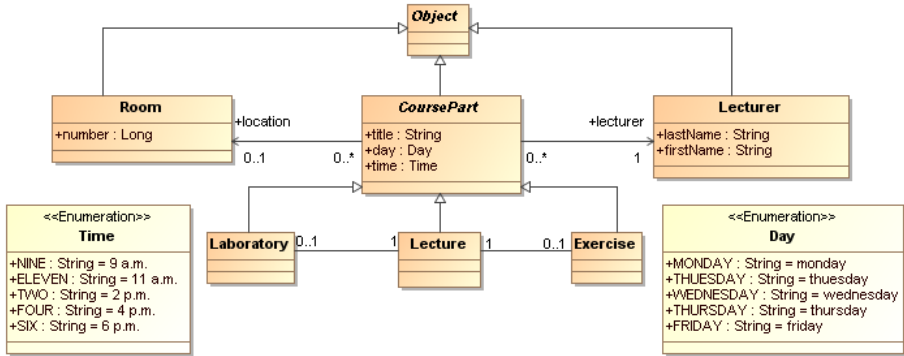


Fig. 1. Domain Class Diagram

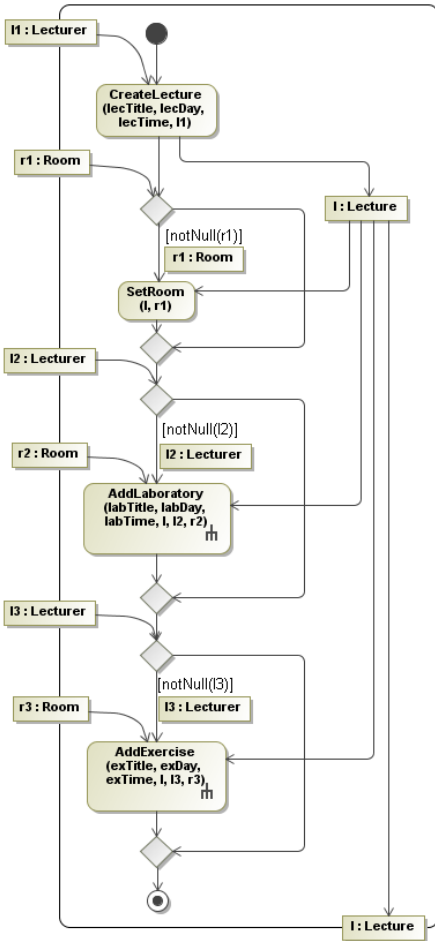
services. Accordingly, the complex activities modeling used services *AddLaboratory* and *AddExercise* are refined by corresponding activity diagrams (cf. Section 4).

UML2 provides several object flow notations. The preference for a notation depends on different aspects, e.g. the amount of information, potential ambiguities, and the equality of control and object flow. For example, if object and control flow overlap, related objects may be depicted next to transitions as shown above activity *SetRoom* in Fig. 2. Otherwise an object node with separate object flow edges has to be used as shown for lecture *l*. However, it is desirable to keep the object flow description as simple as possible without leaving out important information. Each object may be named and its identity is expressed by equal names within an activity diagram. E.g. in activity diagram *AddLecture* both lecturer nodes named *l2* depict the same object. Please note that in our approach, an object may flow along multiple outgoing edges i.e. object flows, whereas in UML2 one object serves one object flow exclusively.

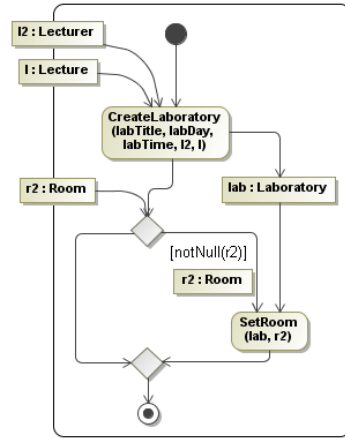
Objects passed from outside to an activity diagram can be drawn on the diagram boundary in order to show parameters flowing into certain activities. Objects passed out of the diagram itself, may be depicted as boundary objects as well. Consider Fig. 2: Objects of types *Lecturer* and *Room* are passed to the activity diagram *AddLecture*, while a newly created object of type *Lecture* is passed out of this diagram.

In Fig. 2, service *AddLecture* uses two other services *AddLaboratory* and *AddExercise*. Once a lecture has been created and its attributes have been set, a related laboratory or exercise might be created additionally. At first, a new lecture is created in activity *CreateLecture*, its attributes are set and it is linked to lecturer *l1*. If, moreover, room *r1* is not null, activity *SetRoom* is used to link this room *r1* to the lecture newly created. If a lecturer is given for a laboratory, the complex activity *AddLaboratory* is used to add a laboratory to the lecture. Therefore, *AddLecture* has to pass the newly created lecture *l*, lecturer *l2*, and room *r2* to the activity. In diagram *AddLaboratory* a new laboratory is created by the first activity *CreateLaboratory*. In the same step, this laboratory is linked to lecture *l* and to lecturer *l2*. Furthermore, the laboratory's attributes are set. In the next activity, the laboratory's location is set to room *r2*, provided that *r2* is given. If a lecturer for a related exercise is given, *AddExercise* is used by *AddLecture* analogously.

AddLecture(in String lecTitle, in Day lecDay, in Time lecTime, in String labTitle, in Day labDay, in Time labTime, in String exTitle, in Day exDay, in Time exTime, in Lecturer I1, in Room r1, in Lecturer I2, in Room r2, in Lecturer I3, in Room r3, out Lecture I)



AddLaboratory(in String labTitle, in Day labDay, in Time labTime, in Lecture I, in Lecturer I2, in Room r2)



AddExercise(in String exTitle, in Day exDay, in Time exTime, in Lecture I, in Lecturer I3, in Room r3)

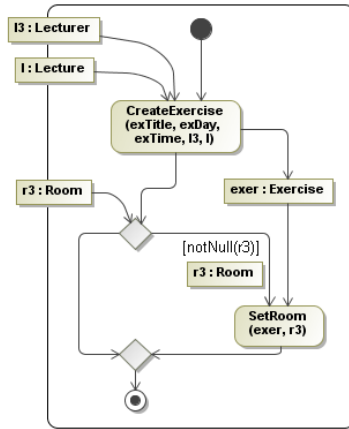


Fig. 2. Activity Diagrams of Services *AddLecture* and *AddLaboratory*

Since our activity diagrams model services, we equip each of them with a name and a comma-separated list of *parameters*. The semantics follow the programming concept of parameter passing between operations, i.e. an activity diagram models an operation consisting of a signature and a body. The signature of an activity diagram consists of its name and a list of attribute and object parameters. While object parameters have a type occurring in the domain model, attribute parameters have primitive types in most cases. This signature is an extension of UML2 made by our approach. Please note that all attributes and boundary objects used within the activity diagram are arguments which correspond to the signature. In addition, each parameter declaration has to be enriched with keyword *in*, *out*, or *inout*. This qualification defines the object flow direction. E.g.

lecturer *l1* has to be passed to diagram *AddLecture* and is therefore marked *in*. Vice versa, the newly created lecture *l* is passed out of the diagram and is therefore marked by *out*. Parameter objects marked by *inout* are both input and output objects.

2.3 Refined Activities

Activities are used to model specific changes of the current system snapshot i.e. object structure. We propose to refine activities by pre- and post-conditions specifying snapshots before and after the activity respectively. We refine activities separately by pairs of object diagrams which are typed over the domain model. Figure 3 shows object diagrams refining activities of our example (cf. Fig. 2) where pre-conditions are depicted on the left and post-conditions on the right. Objects and links with equal names on both sides express identity and preservation. Objects and links occurring on the left-hand side only will be deleted, while objects and links occurring in the right-hand side only will be created. Conditions on non-existence of patterns are depicted in red dashed outline.

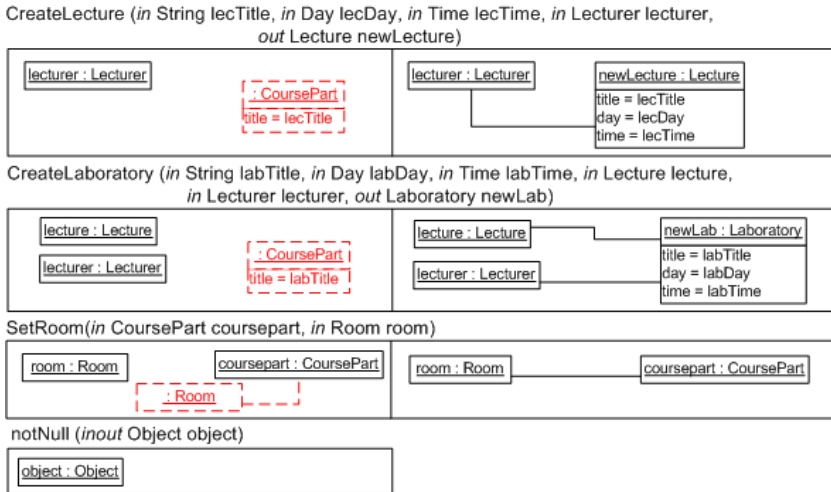


Fig. 3. Refined Activities by Pre- and Post-Conditions

Each pair of conditions exhibits a signature according to the inscription of its refined activity, i.e. it consists of a name (the activity name) and a list of typed parameters qualified with keyword *in*, *out* or *inout*. Parameters can be distinguished into object and attribute parameters, analogously to their usage in activity diagrams. While the former ones are matched to objects, the latter ones are used as attribute values. Keyword *in* requires the occurrence of the related object (if object parameter) on the left-hand side. The object may be used in a read, edit, or delete operation. Keyword *out* declares a returned object and requires its presence on the right-hand side. It may be used for a create or select operation. *Inout* declares an object to be given and returned as well, thus requires the given object on both sides which explicitly guarantees its non-deletion. Attribute parameters must be input parameters. If occurring in pre-conditions, attribute

parameter values restrict the matching of objects, occurring in post-conditions they are used to assign attribute values. Object parameter types must be respected by condition checking, i.e. by pattern matchings. Parameters may be matched, if they are matched with equally typed or sub-typed values only. Analogously, this must hold for attribute types. Note that arrays and collection-like types are not supported by our approach yet.

The first pair of conditions in Fig. 3 refines activity *CreateLecture*. The pre-condition requires the existence of a lecturer in the current system snapshot, otherwise the activity cannot be applied. Also, it requires the non-existence of a *CoursePart* instance (which could be of concrete type *Lecture*, *Exercise*, or *Laboratory*) with a *title* equal to given attribute parameter *lecTitle*. If both conditions hold, the activity is applicable and creates a *Lecture* instance associated with the given *Lecturer* instance and the lecture is returned. The refinement of activity *CreateLaboratory* shown as second pair in Fig. 3 is quite similarly, but it requires two given objects to exist and the creation of an object of type *Laboratory*. Since the conditions of *CreateExercise* are analogous to those of *CreateLaboratory*, they are left out. The refinement of activity *SetRoom* is shown as third pair. It requires two object parameters, one instance of type *Room* and one of type *CoursePart*, and it forbids the *CoursePart* instance to have a room already. No object but a link between the given course part and the new room is created here. Please note, that *CoursePart* is an abstract type. Thus instances of its concrete sub-classes can be used here only. The last condition in Fig. 3 refines guard *notNull*. Since guards do not perform model-changing transformations but rather check for existence in the system snapshot, we just define a guard pattern here. Note that we disallow non-existence conditions in guard patterns. Else-guards are predefined by negated guard patterns i.e. it is checked for non-existence of the corresponding guard pattern.

3 Formalization by Graph Transformation

The UML variant presented in the previous section can be equipped with a graph transformation semantics. We start with presenting the theory of graph transformation as in [6] and extend it by new concepts. While class diagrams are formalized by type graphs, activities with pre- and post-conditions are mapped to graph rules. The object flow is formalized by a new concept called *partial rule dependencies*. This semantics definition serves as a basis for validating the consistency of refined activity diagrams with object flow.

3.1 Graphs and Graph Transformation

Graphs are often used as abstract representation of visual models, e.g. UML models. When formalizing object-oriented models, graphs occur at two levels: the type level (defined by a meta-model) and the instance level. This idea is described by the concept of *typed attributed graphs*, where a fixed *type graph* TG serves as an abstract representation of the meta-model (without constraints). Node types can be structured by an inheritance hierarchy and may be abstract in the sense that they cannot be instantiated. Multiplicities and other annotations have to be expressed by additional graph constraints. Attribute types are formally described by data type algebras. Instances of

the type graph are *object graphs* equipped with a structure-preserving mapping to the type graph. Attribute values are given by a concrete data algebra.

Graph transformation is the rule-based modification of graphs. A *rule* is defined by $p = (L \xleftarrow{l} K \xrightarrow{r} R, I, O, NACs)$ where L is the left-hand side (LHS) of the rule representing the pre-condition and R is the right-hand side (RHS) describing the post-condition. l and r are two injective graph morphisms, i.e. functions on nodes and edges which are structure and type-preserving. They specify a partial mapping $r \circ l^{-1}$ from L to R . $L \setminus l(K)$ defines the graph part that is to be deleted, and $R \setminus r(K)$ defines the graph part to be created. The types of newly created nodes have to be non-abstract. Elements in K are mapped in a type preserving way. All graphs of a rule are attributed by the same algebra being a term algebra with variables. Some of these variables are considered to be rule parameters. Input parameters can be nodes or variables, thus $I = I_N \cup I_V$, whereas output parameters can be nodes only, i.e. $O = O_N$ with $I \subseteq L$ and $O \subseteq R$.

NACs is a set of negative application conditions, each defined by an injective graph morphism $n : L \rightarrow N$ where $N \setminus n(L)$ defines a forbidden graph part. n allows to refine node types, i.e. a node of a more abstract type is allowed to be mapped to a node with a finer type according to the inheritance hierarchy.

Example 1 (Example rules). Figure 3 shows example graph rules. Each pre-condition forms an LHS with one negative application condition and each post-condition describes an RHS. Identifiers given by names indicate the mapping between left- and right-hand sides. The solid parts of a pre-condition indicate the LHS L , while the dashed ones prohibit a certain graph part and represent $N \setminus n(L)$ of the NAC. Input and output parameters are listed on top of each pair of conditions, formally in the head of each rule.

A *graph transformation step* $G \xrightarrow{p,m} H$ between two instance graphs G and H is defined by first finding a match $m : L \rightarrow G$ of the left-hand side L of rule p into the current instance graph G such that m is an injective type-refining graph morphism. Match m has to fulfill the *dangling condition*, i.e. nodes may be deleted only, if all adjacent edges are mentioned in the LHS. Moreover, each NAC has to be fulfilled, i.e. m satisfies a *NAC*, if for each $n \in NACs$ there does not exist an injective type-refining morphism $o : N \rightarrow G$ such that $o \circ n = m$. Input parameters are instantiated by concrete values being nodes of the instance graph and data type values. Thus, parameter instantiation provides a partial match.

In the second step, graph H is constructed by a double-pushout construction (see [6]). Roughly spoken, the construction is performed in two passes: (1) build a graph D which contains all those elements of G not deleted; (2) construct H as a union of D and all elements of R to be created. To focus on the preserved part of a graph transformation step, we define a partial graph morphism *track* : $G \rightarrow H$ by $track = g^{-1} \circ h$. Graph $dom(track)$ is the subgraph of G where *track* is defined, i.e. the domain of *track*. (See also [7] for a first definition of track morphism.) Morphisms $g : D \rightarrow G$ and $h : D \rightarrow H$ are constructed by a double-pushout as shown below. Morphism g^{-1} is always well-defined, since l is injective and the pushout construction preserves injectivity, thus g is also injective. Furthermore, a so-called co-match $m' : R \rightarrow H$ is defined by the double-pushout construction. Output parameters point to a certain part

of this co-match. Output parameters are useful for pointing to specific nodes which can be used in further transformation steps then.

$$\begin{array}{ccccc}
 I & \xrightarrow{\subseteq} & L & \xleftarrow{l} & K & \xrightarrow{r} & R & \xleftarrow{\subseteq} & O \\
 & & \downarrow m & & \downarrow & & \downarrow m' & & \\
 & & G & \xrightleftharpoons[g]{h} & D & \xrightarrow{h} & H & & \\
 & & & & \text{track} & & & &
 \end{array}$$

A *graph transformation (sequence)* $t = G_0 \xrightarrow{p_1, m_1} G_1 \dots G_{n-1} \xrightarrow{p_n, m_n} G_n$ consists of zero or more graph transformation steps. Track morphism $track_{0,n}$ of sequence t is simply the composition of track morphisms $track_{n-1,n} \circ \dots \circ track_{0,1}$ of its steps. For $n = 0$, $track_{0,0} = id_{G_0}$. A set of graph rules P , together with a type graph TG , is called a *graph transformation system (GTS)* $GTS = (TG, P)$. A GTS may show two kinds of non-determinism: Given a graph, (1) several rules can be applicable, and (2) for each rule several matches can exist. There are techniques to restrict both kinds of choices. The choice of rules can be restricted by the definition of control flow while the choice of matches can be restricted by passing partial matches The tool AGG (Attributed Graph Grammar System) [8] can be used to specify and analyze graph transformation systems.

3.2 Partial Rule Dependencies

To restrict the choice of matches for rules, we introduce the concept of *partial rule dependencies* which may relate output parameter nodes of one rule to input parameter nodes of a (not necessarily direct) subsequent rule in a given rule sequence². We say that rule sequences are dependency-compatible, if the transitive closure of all dependencies between each two rules is well-defined.

Definition 1 (partial and joint rule dependencies). Given a GTS (T, P) and a rule sequence $s : p_1, \dots, p_n$ with $p_1, \dots, p_n \in P$. A partial rule dependency between rules p_i and p_j with $1 \leq i < j \leq n$ is defined by an injective partial morphism $d_{ij} : O_{iN} \rightarrow I_{jN}$ from output parameter nodes of p_i to input parameter nodes of p_j . If d_{ij} is the empty morphism, no rule dependency is defined. For each pair of rules p_i and p_j in s , its closure $closure_{ij}$ is defined as follows: (1) d_{ij} belongs to $closure_{ij}$ and (2) for all d_{ik}, d_{kj} , and rules p_k with $i < k < j$ add $d_{kj} \circ r_k \circ l_{k|I_k}^{-1} \circ d_{ik}$ to $closure_{ij}$.

$$\begin{array}{ccccc}
 O_{iN} & \xrightarrow{d_{ik}} & I_{kN} & & O_{kN} & \xrightarrow{d_{kj}} & I_{jN} \\
 \downarrow \subseteq & & \downarrow \subseteq & & \downarrow \subseteq & & \downarrow \subseteq \\
 R_i & & L_k & \xleftarrow{l_k} & K_k & \xrightarrow{r_k} & R_k & & L_j
 \end{array}$$

Rule sequence s is dependency-compatible, if for all closures $closure_{ij}$ the following holds: (1) For all $d \in closure_{ij}$: $type(x)$ has to be finer or coarser than $type(d(x))$

² Note that rule sequences differ from transformation sequences in not providing graphs to which rules are applied.

for all $x \in O_{i_N}$ wrt. the type inheritance relation defined by type graph T . (2) Each two dependencies d and d' in $\text{closure}_{e_{ij}}$ are weakly commutative, i.e. $d(x) = d'(x)$ for all $x \in \text{dom}(d) \cap \text{dom}(d')$.

If rule sequence s is dependency-compatible, we can define a joint dependency of a closure. Given $\text{closure}_{e_{ij}}$ we define the joint dependency $\text{dep}_{ij} : O_{i_N} \rightarrow I_{j_N}$ as follows: (1) $\text{dom}(\text{dep}_{ij}) = \bigcup_{d \in \text{closure}_{e_{ij}}} \text{dom}(d)$ and (2) $\text{dep}_{ij}(y) = d(y)$ if $y \in \text{dom}(d)$ for $d \in \text{closure}_{e_{ij}}$

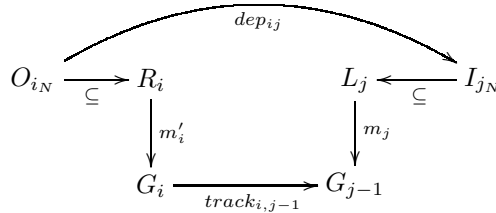
Example 2 (partial rule dependencies). Considering the rules in Fig. 3, we compose rule sequence $s = \text{CreateLecture}, \text{SetRoom}, \text{CreateLaboratory}, \text{SetRoom}$. As first step, we define partial rule dependencies taking input and output parameters into account:

$d_{12}(\text{newLecture}) = \text{coursepart}, d_{23} = d_{34} = d_{24} = d_{14} = \emptyset, d_{13}(\text{newLecture}) = \text{lecture}$. All dependencies are type-compatible, since either the types of mapped nodes are equal or in hierarchy, e.g. $\text{type}(\text{newLecture}) = \text{Lecture}$ is finer than $\text{type}(d_{12}(\text{newLecture})) = \text{type}(\text{coursepart}) = \text{Coursepart}$ (see Fig. 1). None of the closures contains more than one non-empty partial dependency. Thus, partial rule dependencies are not really composed from each other in this example, e.g. $\text{dep}_{13} = d_{13}$.

If coursepart were an *inout* parameter of rule SetRoom , $\text{closure}_{e_{13}}$ could look more interesting: With $d_{23}(\text{coursepart}) = \text{lecture}$ we would have $\text{closure}_{e_{13}} = \{d_{13}, d_{23} \circ r_2 \circ l_2^{-1} \circ d_{12}\}$ with $\text{dep}_{13}(\text{newLecture}) = \text{lecture}$.

If we enlarged the rule sequence by rule CreateLaboratory and defined $d_{34}(\text{newLab}) = \text{coursepart}$ as well as $d_{45}(\text{coursepart}) = \text{lecture}$, then dep_{35} would have to map newLab to lecture which would not be type-compatible.

Definition 2 (application of dependency-compatible rule sequences). A dependency-compatible rule sequence $s : p_1, \dots, p_n$ is applicable to some graph G_0 , if there is a graph transformation sequence $G_0 \xrightarrow{p_1, m_1} G_1 \dots G_{n-1} \xrightarrow{p_n, m_n} G_n$ such that $m_j \circ \text{dep}_{ij}$ and $\text{track}_{i,j-1} \circ m'_i(O_{i_N})$ are weakly commutative, with $\text{track}_{i,j-1}$ being the track morphism from G_i to G_{j-1} and m'_i being the co-match of rule p_i for $1 \leq i < j \leq n$.



Partial rule dependencies are defined independently of causal dependencies. Causal dependencies between rules can be analyzed by the critical pair analysis (CPA) [6]. The only kind of causal dependencies we are interested in here are *produce/use*-dependencies where the application of one rule produces an element needed by the match of a second rule. If two rules are not causally dependent on each other, the corresponding joint dependency which is defined explicitly must not introduce any produce/use-dependency. If some partial dependency is defined, it has to correspond with at least one produce/use dependency.

4 Object Flow: Semantics Definition and Properties

In this section, we first specify well-structured refined activity diagrams, refine their activities by graph rules and their guards by graph patterns, and define their semantics and consistency based on graph transformation. Thereafter, this approach is extended to refined activity diagrams with object flow.

From now on, we assume that an activity diagram does not contain any complex activities and that each complex activity has been flattened before, i.e. it has been replaced by its refining activity diagram. During this potentially recursive process, each object which goes in to or comes out from a complex activity is glued with the corresponding boundary object of the refining activity diagram, i.e. the boundary and boundary objects disappear.

4.1 Refined Activity Diagrams

As in [9,1], we restrict our considerations to well-structured activity diagrams. The building blocks are simple activities, sequences, fork-joins, decision-merge structures, and loops only.

Definition 3 (well-structured activity diagram). *A well-structured activity diagram A consists of a start activity s , an activity block B , and an end activity e such that there is a transition between s and B and another one between B and e . An activity block is defined as follows:*

- Empty: *An empty activity block is not depicted.*
- Simple: *A simple activity is an activity block.*
- Sequence: *A sequence of two activity blocks A and B connected by a transition from A to B form an activity block.*
- Decision/Merge: *A decision activity which is followed by two guarded transitions leading to one activity block each and where each block is followed by a transition both heading to a common merge activity form an activity block. One transition is explicitly guarded, called the if-guard, while the other transition carries a predefined guard "else" which equals the negated if-guard.*
- Loop: *A decision activity is followed by a guarded transition. This guard is called loop-guard. The transition leads to an activity block with an outgoing transition to the same decision activity as above. Considering this decision activity again, its incoming transition from outside becomes the incoming transition of the new block. Its outgoing transition to outside becomes the outgoing transition of the new block. This transition is guarded by "else". The whole construct forms an activity block.*
- Fork/Join: *A fork activity followed by two branches with one activity block each followed by a join activity form an activity block.*

To be able to define object flow to be coherent with control flow we define a control flow relation as prerequisite. Because of potential loops it is not a partial order.

Definition 4 (control flow relation). *The control flow relation CFR_A of an activity diagram A contains pairs (x,y) where x, y are activities such that the following holds:*

- Pair $(x, y) \in CFR_A$, if x is directly connected via a transition with y .
- If $(a, b) \in CFR_A$ and $(b, c) \in CFR_A$, then also $(a, c) \in CFR_A$.

An if- or loop-guard is equipped with a graph pattern which describes an existence condition on graphs. A guard pattern can be interpreted as identical rule (i.e. a rule where the left and the right-hand sides are equal). Guard pattern g is fulfilled by a graph G , if its corresponding rule p_g is applicable to G . After rule p_g has been performed, the guarded alternative is executed. Otherwise, rule \bar{p}_g which formalizes "else" for given guard g , is applicable to G and the second alternative is performed.

Definition 5 (guard pattern, guard rule and negated guard rule). A guard pattern g is defined by a typed graph being attributed over a term algebra with variables. Its guard rule p_g is defined by $(g \xleftarrow{id_g} g \xrightarrow{id_g} g, I, O, \emptyset)$. Its negated guard rule \bar{p}_g is defined by $(\emptyset \xleftarrow{\emptyset} \emptyset \xrightarrow{\emptyset} \emptyset, \emptyset, \emptyset, \{n : \emptyset \rightarrow g\})$.

Lemma 1. Given a guard pattern g and a graph G . Rule p_g is applicable to G , iff rule \bar{p}_g is non-applicable to G .

Proof. See [10].

Definition 6 (refined activity diagram). A refined activity diagram RA is a well-structured activity diagram such that each simple activity occurring in RA is equipped with a graph transformation rule. Each if- or loop-guard occurring in RA is equipped with a guard pattern. We also say that an activity is refined by a transformation rule where decision activities are refined by guard rules deduced from guard patterns which refine guards.

Definition 7 (semantics of refined activity diagrams). Given an activity block B of a refined activity diagram RA , its corresponding set of rule sequences S_B is defined as follows.

- If B is empty, $S_B = \emptyset$.
- If B consists of a simple activity a refined by rule p_a , $S_B = \{p_a\}$.
- If B is a sequence of X and Y , $S_B := S_X \text{ seq } S_Y = \{s_x s_y \mid s_x \in S_X \wedge s_y \in S_Y\}$
- If B is a decision block on X and Y with guard pattern g refining its if-guard, $S_B = (\{p_g\} \text{ seq } S_X) \cup (\{\bar{p}_g\} \text{ seq } S_Y)$
- If B is a loop block on X with guard pattern g refining its loop-guard, $S_B := \text{loop}(g, S_X) = \bigcup_{i \in I} S_X^i$ where $S_X^0 = \{\bar{p}_g\}$, $S_X^1 = \{p_g\} \text{ seq } S_X \text{ seq } \{\bar{p}_g\}$, $S_X^2 = \{p_g\} \text{ seq } S_X \text{ seq } S_X^1$ and $S_X^i = \{p_g\} \text{ seq } S_X \text{ seq } S_X^{i-1}$ for $i > 2$. $S_B(n) = S_X^n$ denotes the semantics of loop block B with exactly n loop executions.
- If B is a fork block on X and Y , $S_B := S_X \parallel S_Y = \bigcup s_x \parallel s_y$ with $s_x \in S_X \wedge s_y \in S_Y$ where $s_x \parallel \lambda = \{s_x\}$, $\lambda \parallel s_y = \{s_y\}$, and $p_x s'_x \parallel p_y s'_y = \{p_x\} \text{ seq } (s'_x \parallel p_y s'_y) \cup \{p_y\} \text{ seq } (p_x s'_x \parallel s'_y)$.

The semantics $Sem(RA)$ of a refined activity diagram RA consisting of a start activity s , an activity block B , and an end activity e is defined as the set of rule sequences S_B generated by the main activity block B . If RA contains k guarded loops, $Sem_{n_1, \dots, n_k}(RA) \subseteq Sem(RA)$ denotes a restricted semantics where the semantics of each guarded loop $B_j \in A$ for $1 \leq j \leq k$ is $S_{B_j}(n_j)$.

Now, we are ready to check the control flow consistency of activity diagrams. To do so, we consider snapshots of the system, i.e. object models which are formalized as graphs by mapping objects to graph nodes and object links to graph edges. In the following definitions for consistency-related properties, we directly use graphs as abstract syntax representation of object models.

Activity diagrams are *consistent*, if there is a set \mathcal{S} of model graphs such that each rule sequence in the diagram semantics is applicable to some of these graphs. If the diagram contains guarded loops, we use the restricted semantics for diagrams (as defined above) which checks for each guarded loop, if a predefined number of loop executions is feasible. \mathcal{S} is *without junk*, if each of its model graphs represents a potential snapshot of the system to which an activity sequence in A can be applied.

Definition 8 (completeness). *A set \mathcal{S} of graphs is complete wrt. to a refined activity diagram RA , if for all rule sequences s in $Sem(RA)$ there is a graph G in \mathcal{S} such that s is applicable to G . If RA contains k guarded loops, a set \mathcal{S} of graphs is quasi-complete wrt. to RA , if for all rule sequences s in $Sem_{n_1, \dots, n_k}(RA)$ there is a graph G in \mathcal{S} such that s is applicable to G . Set \mathcal{S} is without junk, if for each graph in \mathcal{S} at least one applicable rule sequence in $Sem(RA)$ (resp. $Sem_{n_1, \dots, n_k}(RA)$) exists.*

Definition 9 (consistent activity diagram (without object flow)). *A refined activity diagram RA is consistent, if there is a set \mathcal{S} of graphs which is complete wrt. RA . If RA contains k guarded loops, RA is quasi-consistent, if there is a set \mathcal{S} of graphs which is quasi-complete wrt. RA .*

4.2 Refined Activity Diagrams with Object Flow

In the following, we define refined activity diagrams by partial rule dependencies which formalize object flows and enrich its semantics.

Definition 10 (well-structured activity diagram with coherent object flow). *A well-structured activity diagram $A_{OF} = (A, Obj, OFR, I, O)$ with coherent object flow is a well-structured activity diagram A (as given in Def. 3) equipped with a set of object nodes Obj , an object flow relation OFR for A and Obj , input parameter set I , and output parameter set O , defined as follows:*

- *Input parameters can be object nodes or values, i.e. $I = I_N \cup I_V$ with $I_N \subseteq Obj$. Output parameters may only be object nodes only, i.e. $O = O_N$ with $O \subseteq Obj$.*
- *Object flow relation OFR contains triples (x, o, y) where x and y are simple or decision activities and $o \in Obj$. In addition, there is a special tag `null` not used as activity name which is used to define object flow from and to parameter objects, i.e. triples $(null, o, y)$ and $(x, o, null)$ can also be in OFR where $o \in I_N$ or $o \in O_N$, resp. For each object o in I_N (resp. in O_N), there is a triple $(null, o, y)$ (resp. $(x, o, null)$) in OFR . For each other object $o \in Obj$, there has to be a triple $(x, o, y) \in OFR$.*
- *OFR is coherent with control flow relation CFR_A of A (see Def. 4), i.e. for all $(x, o, y) \in OFR$ with $x, y \neq null$ there is $(x, y) \in CFR_A$.*

Please note that OFR contains a triple for each pair of object flows sharing an object and Obj is not allowed to contain objects not involved in object flow.

Definition 11 (refined activity diagram with object flow). A refined activity diagram RA_{OF} with object flow is a well-structured activity diagram $A_{OF} = (A, Obj, OFR, I, O)$ with coherent object flow such that each simple activity x occurring in A_{OF} is refined by a graph transformation rule p_x . Each decision activity $x \in A_{OF}$ has an if- or loop-guard which is equipped with a guard pattern g . Its guard rule p_g is also denoted by p_x . Let O_{p_x} be the output parameter set of p_x and I_{p_y} the input parameter set of p_y . OFR has to be coherent with refining rules which is defined as follows:

- For all $(x, o, y) \in OFR$ where $x \neq null$, an output object parameter exists in O_{p_x} which is called $src(x, o, y)$. If $y \neq null$, an input object parameter exists in I_{p_y} , called $tgt(x, o, y)$.
- For all triples $(x, o, y), (x, o, y')$ (resp. $(x, o, y), (x', o, y)$) in OFR we have $src(x, o, y) = src(x, o, y')$ (resp. $tgt(x, o, y) = tgt(x', o, y)$).
- For each two activities x and y and the set of all $(x, o, y) \in OFR$, the set of all pairs $(src(x, o, y), tgt(x, o, y))$ defines an injective mapping.
- For all triples $(x, o, null), (x, o', null)$ (resp. $(null, o, y), (null, o', y)$) in OFR with $o \neq o'$ we have $src(x, o, null) \neq src(x, o', null)$ (resp. $tgt(null, o, y) \neq tgt(null, o', y)$).

Definition 12 (semantics of refined activity diagrams with object flow). The semantics $Sem(RA_{OF})$ of an activity diagram RA_{OF} with object flow being a refined activity diagram of $A_{OF} = (A, Obj, OFR, I, O)$ is equal to $Sem(RA)$, the semantics of refined activity diagram RA without object flow, where in addition partial rule dependencies (see Def. 1) are defined as follows:

For each pair of rules (p_i, p_j) in a rule sequence $s : p_1, \dots, p_n$ of $Sem(RA)$ with $1 \leq i < j \leq n$, partial rule dependency d_{ij} is defined as follows: Let x (resp. y) be the activity that is refined by rule p_i (resp. p_j) in sequence s , then the partial rule dependency d_{ij} between p_i and p_j consists of all pairs $(src(x, o, y), tgt(x, o, y))$ such that $(x, o, y) \in OFR$ where src and tgt are given by Def. 11.

RA_{OF} is called dependency-compatible, if all rule sequences in $Sem(RA_{OF})$ are dependency-compatible, as defined in Def. 2.

Definition 13 (completeness of refined activity diagrams with object flow). A set \mathcal{S} of graphs is complete wrt. a dependency-compatible refined activity diagram RA_{OF} , if for all dependency-compatible rule sequences s in RA_{OF} there is a graph G in \mathcal{S} such that s is applicable to G in the sense of Def. 2.

Properties quasi-completeness and consistency of refined activity diagrams without object flow can be extended to those with object flow accordingly.

Example 3 (Semantics of activity diagrams). The semantics of the flattened activity diagram *AddLecture* in Figure 2 consists of a number of rule sequences. For listing some of them, we use the following acronyms: NN=NotNull, CLec=CreateLecture, CLab=CreateLaboratory, CEx=CreateExercise, and SR=SetRoom: $Sem(RA_{OF}) \supseteq \{(CLec, \overline{NN}, \overline{NN}, \overline{NN}), (CLec, NN, SR, \overline{NN}, \overline{NN}), (CLec, \overline{NN}, NN, CLab, \overline{NN}, \overline{NN})\}$,

$(CLec, \overline{NN}, NN, CLab, NN, SR, \overline{NN}), (CLec, NN, SR, NN, CLab, \overline{NN}, \overline{NN}),$
 $(CLec, \overline{NN}, NN, CLab, NN, SR, NN, CEx, NN, SR),$
 $(CLec, NN, SR, NN, CLab, NN, SR, NN, CEx, NN, SR)\}$

As partly shown in Example 2, the object flow in our example can be formalized by partial rule dependencies. All rule sequences given above are dependency-compatible.

5 Related Work

This paper is rooted in formal semantics and analysis of activity diagrams as well as graph transformation approaches. While a lot of research has been done on semantics and validation of activity diagrams (see e.g. [11,12,9]), few works exist on the analysis of object flow in activity diagrams such as [13] and [14]. For example, [14] adds data flow semantics to activity diagrams by means of colored petri nets. Objects which are passed between activities have attribute value checks and method calls. Colored Petri nets provide validation like reachability of certain states and quantitative analyses as matching of time bounds. In contrast, we define a semantics for activity diagrams with object flow where activities may be refined by interrelated object diagrams which has not been done before (to the best of our knowledge).

Fujaba [15], VMTS [16], and GReAT [17] are graph transformation tools for specifying and applying object rules along a control flow specified by activity diagrams. Fujaba's story diagrams integrate activity diagrams with object rules. Compared to our approach, object flow is not depicted separately, but represented by equal names in activities. Furthermore, rules are not separated from activities. Rules used at different places have to be specified several times. We define object rules independently of activities and can apply them more than once with different arguments. VMTS and GReAT support controlled rule application with explicit control flow in a similar way and some kind of object flow. All three approaches are implemented, but do not provide a formal semantics comprising activity refinement and object flow.

6 Conclusion

In this paper, we have defined refined activity diagrams with object flow where each activity is refined by a set of interrelated object diagrams in addition, describing the pre- and post-conditions of an activity. Pre-conditions can also include non-existence conditions on object patterns. We have formalized the semantics of well-structured refined activity diagrams with coherent object flow using algebraic graph transformation where activity-refining object diagrams are defined by transformation rules. In addition, we have introduced the notion of partial dependencies between rules formalizing object flow between refined activities. To prepare a notion of consistency we define the applicability of rule sequences with partial rule dependencies.

In this paper, we have applied the approach to service modeling. Our example demonstrates how service behavior can be modeled precisely and how the coherence of its object flow can be checked. We expect that domains such as work flow design and aspect-oriented modeling can benefit from the application of our concepts as well. In future, we want to use the formal semantics given by graph transformation to prove the

consistency of refined activity diagrams with object flow along sufficient criteria easy to check. We expect that the graph transformation environment AGG can do a good job to support automatic checks.

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