

# Resource Requirement Analysis for a Predictive-Hashing Based Multicast Authentication Protocol\*

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**Abstract.** A new multicast authentication scheme for real-time streaming applications was proposed [28] that is resistant to denial-of-service attacks with less resource usages (CPU and buffer) at receivers compared to previously proposed schemes. This scheme utilizes prediction hashing (PH) and one-way key chain (OKC) techniques based on erasure codes and distillation codes. Detailed protocol description is presented at the sender and receiver sides, and a worst-case resource (memory and CPU) requirement at the receiver-side is obtained with an assumption of security condition.

**Keywords:** denial-of-service, multicast, authentication, protocol, resource requirement, cryptographic hashing.

## 1 Introduction and Related Works

We developed an efficient multicast authentication scheme [28] for real-time streaming applications that is resistant to denial-of-service attacks while consuming less resources (CPU and buffer) at receivers compared to previously proposed schemes. This scheme utilizes *prediction hashing* (PH) and *one-way key chain* (OKC) techniques based on erasure codes [12, 13, 22, 23, 24] and distillation codes [10]. PH and OKC techniques enable the receiver to significantly reduce the CPU overhead and buffer requirements compared to other block-based solution approaches [8, 10, 15, 16, 17, 18]. Our scheme is based on block-based approach where the real-time data stream is divided into blocks of packets and each block includes predictive authentication information for the next block as well as original stream data from the current block. Preliminary analysis conducted in the middle of this paper indicates that this new scheme consumes much less CPU and buffer space than one of the recently proposed denial-of-service (DoS) resistant multicast authentication schemes, pollution resistant authenticated block streams (PRABS) [10], by a factor of more than 5 for buffer requirement and 3 for CPU requirement as will be shown at the end of Section 3.

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Several solution approaches were proposed for multicast authentication [8, 10, 12, 13, 14, 15, 17, 18, 19, 20, 22, 23, 24, 27]. However, all of the approaches are vulnerable to *denial-of service (DoS)* attacks [10]. Hash graph protocols and the Wong-Lam scheme are vulnerable to signature flooding attacks. An adversary flooding the stream with invalid signatures will overwhelm the computational resources of receivers attempting to verify the signatures. Additionally, in hash graph protocols, adversarial loss patterns can cause denial of service. For example, if an adversary causes the loss of all signature packets, nothing is verifiable. Also, erasure codes based approaches have limitations: erasure codes are designed to handle only a specific threat model: packet loss. Erasure codes assume that symbols are sometimes lost but not corrupted in transit; this is the erasure channel model. Unfortunately, the assumptions that underlie erasure codes are unrealistic in hostile environments. Adversaries can pollute the message stream by injecting invalid symbols. If erasure codes use an invalid symbol as input to its decoding algorithm, it will reconstruct invalid data. We have to assume more realistic attack model: malicious end hosts and routers can observe, inject, modify, delay, and drop messages in an erasure encoded multicast stream [10].

Recently, distillation codes [10] were developed to address DoS attack issues in erasure codes based authentication approach. The new block based authentication protocol, named as *pollution resistant authenticated block streams (PRABS)*, was designed and presented in [10] to cope with pollution attacks. However, in PRABS, receivers still need to use significant amount of buffer space, and the CPU overhead at receiver is proportional to the number of attack partitions that may be launched simultaneously.

We developed a new mechanism, which is based on *Prediction Hashing (PH)* and *One-way Key Chain (OKC)*, to overcome those limitations. The basic idea of prediction hashing is that each block of packets convey authentication information that will be used to authenticate (or predict) the next block packets instead of sending the authentication information within the same block as in previous approaches [8, 10, 15, 16, 17, 18]. PH technique allows the receivers to save significant amount of buffer space since only the authentication-related portions from each packet needs to be saved for future packet authentication, while the message portions of arrived packets are processed (or authenticated) immediately after each of them is retrieved from the packet buffer. However, in our scheme, the sender side needs to keep the message portions from two consecutive blocks in the buffer to calculate PH.

Explanation on the proposed protocol is given in Section 2 along with attack types considered and the feasibility condition of such attacks. In Section 3, resource requirement analysis is conducted on CPU and memory requirements at the receivers in the worst case scenario. Conclusion is given in Section 4.

## 2 Predictive Hashing with One-Way Key Chain

We developed a new mechanism, which is based on *Prediction Hashing (PH)* and *One-way Key Chain (OKC)*, to significantly reduce resource requirements by the receiver even in the presence of DoS attack packets flowing in. The basic idea of prediction hashing is that each block of packets convey authentication information

that will be used to authenticate (or predict) the next block packets instead of sending the authentication information within the same block as in previous approaches [8, 10, 15, 16, 17, 18]. PH technique allows the receivers to save significant amount of buffer space since only the authentication-related portions from each packet needs to be saved for future packet authentication, while the message portions of arrived packets are processed (or authenticated) immediately after each of them is retrieved from the packet buffer. However, in our scheme, the sender side needs to keep the message portions from two consecutive blocks in the buffer to calculate PH.

One-way key chain technique is already used in other contexts such as in one-time password [11], TESLA [19, 20], etc. In our approach, the sender will obtain a hash chain by applying hash operations recursively to some seed value, and the obtained key values will be assigned to the blocks in backward order of their generation times. The sender will use the assigned key to calculate Message Authentication Codes (MAC) images of the prediction hashes/signature information for the next block, and attach them (along with other authentication related information) to the current block packets. Also, each block packet reveals the key used in the previous block to let the receivers use it in authenticating the previous block packets (or partitions) without applying erasure decoding and signature verifications in most of the cases. These mechanisms are combined with erasure codes and distillation codes to develop a multicast authentication protocol which is very resistant to Denial-of-Service attacks and resource-efficient. Figure 1 shows the overview of our approach at sender side. The receiver side operation is the reverse of the process shown in Figure 1.

At the sender side, erasure codes are applied to the hashes/signature obtained from next block ( $B_{i+1}$ ) to cope with packet losses during transmission. These erasure encoded symbols are, then, divided into  $n$  pieces denoted as  $E_1, E_2, \dots, E_n$ . Message authentication codes (MAC) are applied to these  $E_1$  through  $E_n$  with a key  $K_i$  to prevent a most sophisticated DoS attack which is named as *strong relay-attack*<sup>1</sup> in this paper. Note that the key used in this process will not be revealed until the next block packet is sent out. The output from these MAC codes are denoted as  $\Gamma_1, \Gamma_2, \dots, \Gamma_n$ . These  $\langle E_j, \Gamma_j \rangle$  pairs attached to the packet are protected by attaching  $D_j$  obtained from the distillation codes. These  $D_j$ s will allow the receiver to formulate candidate partitions by applying one-way accumulators based on Merkel hash trees. When a certain *security condition* (which will be introduced later) is met, the receiver doesn't have to apply erasure decoding and signature verification operations, which are the most expensive operations in terms of CPU overhead, for each *invalid* partition. Applying only some hash operations will allow the receiver to filter out invalid partitions – due to prediction hashes and one-way key chain techniques. The sender side may choose a proper value of block period,  $p$ , to satisfy the security condition. It will be shown that this condition is general enough in most of the cases as long as the real-time constraints are not very tight. Even when the security condition may not be satisfied for every case and receiver, it will be much more difficult to launch effective DoS attacks in our scheme due to the restrictions imposed by PH and OKC techniques on adversaries.

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<sup>1</sup> This will be formally defined later in this section.

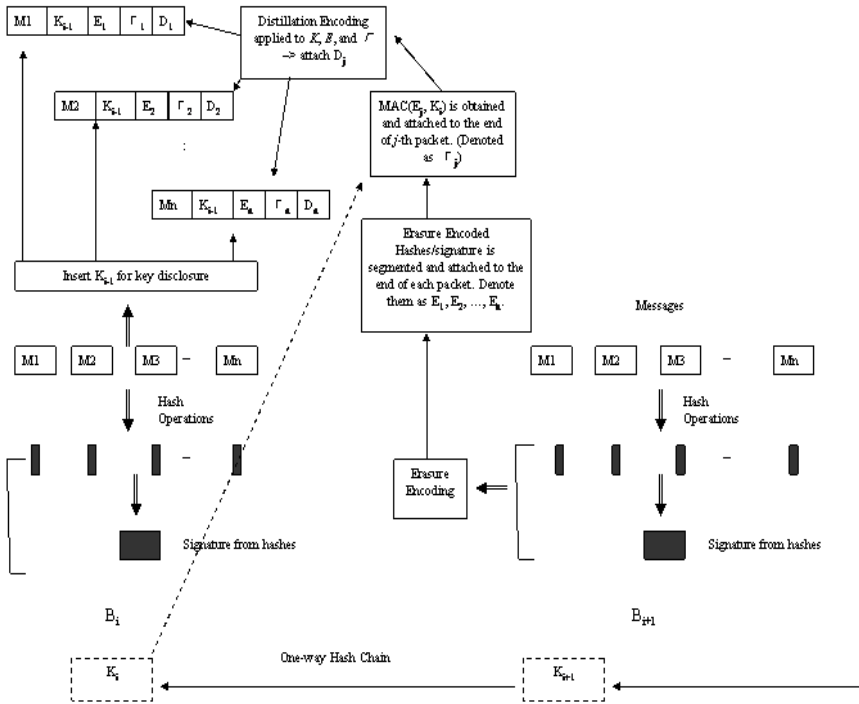


Fig. 1. Overview of our scheme with PH and OKC at the sender

For the purpose of analysis, the following attack types are introduced and used in this paper.

**Relay-Attack:** An adversary may eavesdrop authentic packets and spoof (and send) packets with invalid authentication-related attachments (while preserving the authentic message portions in each packet) in such a way that the receiver will receive at least  $n-t$  spoofed packets earlier than  $n-t$  authentic packets in the same block.

**Strong Relay-Attack:** If an adversary has the following capabilities, he/she can launch strong relay-attacks:

- o Adversary can eavesdrop at least  $n-t$  authentic packets in  $B_i$  and at least one authentic packet in  $B_{i+1}$ .
- o Adversary copies authentic message portions from  $B_i$  packets into (at least)  $n-t$  spoofed packets, and uses a disclosed key  $K_i$  (from  $B_{i+1}$  packet) to come up with modified  $E_j$  and  $\Gamma_j$  in each spoofed packet.
- o Adversary sends all these at least  $n-t$  spoofed packets in such a way that at least  $n-t$  of them will be received before a receiver receives  $n-t$  authentic packets in  $B_i$ .

### 2.1 Feasibility of Strong Relay Attacks

Security condition can be obtained under which the adversaries cannot launch strong relay-attacks. Once the system parameters such as block period ( $p$ ), block size ( $n$ ), redundancy level (related to  $t$ ), etc., are chosen to satisfy this condition, then such

attacks may not be launched by any adversary, thus maximizing the efficiency of our scheme in terms of buffer and CPU usages. Figure 2 shows a diagram for obtaining such condition. If we set the period,  $p$ , to be larger than  $\delta = d + (n-t-1)(p/n)$  where  $d$  represents the maximum delay from the sender to the receiver, then it would not be possible for any attacker to launch strong relay-attacks.

$$p > d - n/(t+1) \tag{1}$$

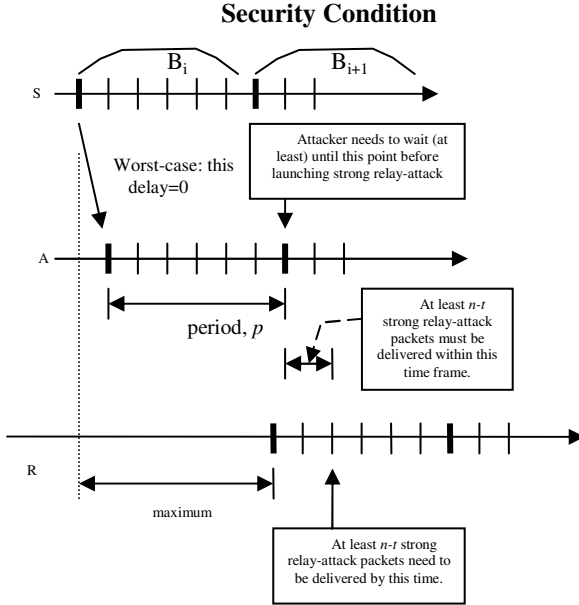


Fig. 2. Security Condition

### 3 Resource Requirement Analysis

#### 3.1 CPU Overhead

We will estimate the CPU overhead in terms of how many erasure decoding, signature verification, and hash operations are needed in each block for our extended scheme. If we assume that a safe period value is chosen from formula (2) in such a way that no strong relay-attacks may be launched, then the CPU overhead may be specified as follows:

- Number of erasure decoding and signature verification operations: Only one erasure decoding and one signature verification operations are needed for each block. This is because, in our algorithm (Figure 3) – step (4), only those partitions in SymbolBuffer which have  $\Gamma_j$  matching to  $E_j$  in a chosen member will be decoded/verified in steps (4-1) and (4-2). If any attacker can't launch strong relay-attacks, any invalid partition stored in SymbolBuffer will not have  $\Gamma_j$  matching to  $E_j$  in all its members.

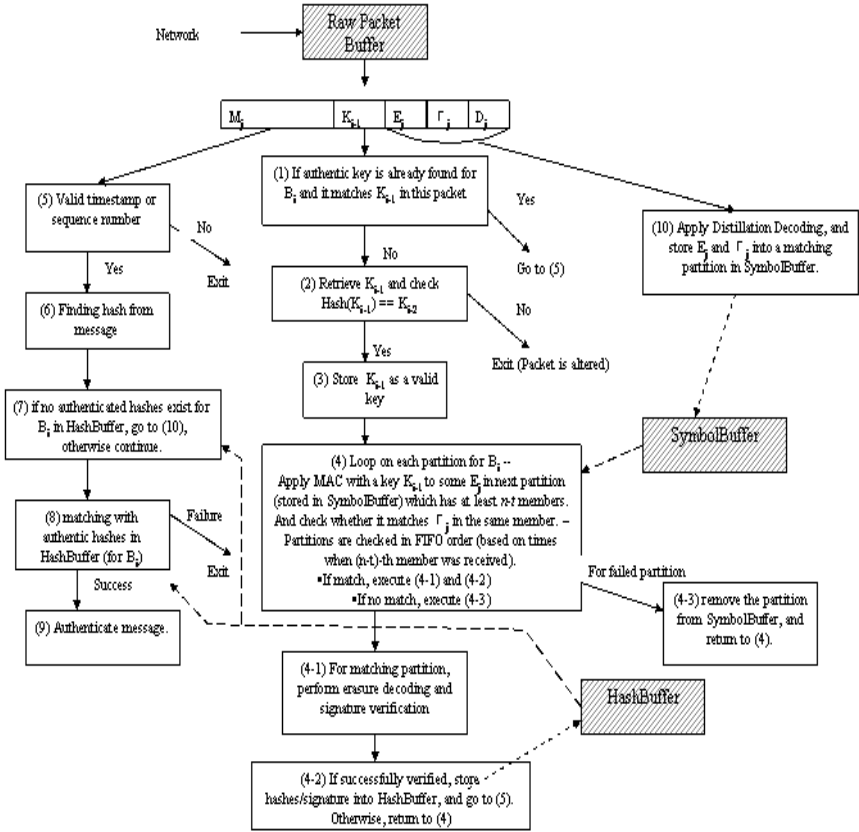


Fig. 3. Detailed Algorithm at a Receiver

o One case we need to consider is when the receiver couldn't obtain any authentic packet in  $B_i$ , and, as a result, no hashes/signature information will be stored in SymbolBuffer. And, when the authentic packets in  $B_{i+1}$  arrive later, the receiver can't authenticate message portions, however, the hashes/signature information contained in  $B_{i+1}$  packets will be stored in SymbolBuffer for  $B_{i+2}$  message authentication. Also, it needs to check  $Hash(Hash(K_i)) == K_{i-2}$  since the receiver will not have the authentic key  $K_{i-1}$ . Even when this happens, the receiver still needs to carry out only one erasure decoding and one signature verification operation when the first authentic packet in  $B_{i+2}$  is received.

- Number of cryptographic hash operations: Hash operations are applied in steps, (2), (4), (6), and (10).

o At step (2), the worst case occurs when all the attack packets have different keys included except for authentic packets. Note that these hash operations are applied even before Distillation Decoding is applied. In this worst case, the number of hash operations needed in one block is  $I$ (for authentic partition)+ $fn$  (for attack packets) =  $I + fn$ . Another extreme case is when all the attack partitions are of size

$n-t$  packets – this case triggers the highest CPU overhead in PRABS. In this case the number of hash operations is equal to the number of partitions with at least  $n-t$  members, which is  $\text{floor}(fn/(n-t))$ . In other cases, the number of hash operations is in between these two extremes.

- At step (4), the maximum number of hash operations needed in one block is equal to  $1+\text{floor}(fn/(n-t))$  since only one hash operation is required for each attack partition which has at least  $n-t$  members arrived.
- At step (6), the number of hash operations needed in one block is  $(f+1)n$  in the worst case when all the attack packets are launched from relay-attacks and have valid key included in them (but, with invalid  $E_j$  and  $\Gamma_j$ ). Also, message portions form authentic packets need to be hashed, too.
- At step (10), the number of hash operations needed in one block is  $(f+1)n \cdot \log n$  in the worst case when attack partitions have  $n-t$  members each and all the attack packets are launched from relay-attacks and have valid message portions and valid keys included in them (but, with invalid  $E_j$  and  $\Gamma_j$ ). Also, distillation decoding needs to be performed for authentic packets, too.
- Hence, the total number of hash operations in the worst case is:

$$1+fn+1+\text{floor}(fn/(n-t)) + (f+1)n + (f+1)n \cdot \log n = 2+(2f+1)n + \text{floor}(fn/(n-t)) + (f+1)n \cdot \log n \tag{2}$$

From this formula, if we subtract the number of hash operations in Prediction Hash based approach (or PRABS), then we get  $2+fn+\text{floor}(fn/(n-t)) \approx O(fn)$ .

- The total CPU processing time may be represented as follows:

$$[2+(2f+1)n + \text{floor}(fn/(n-t)) + (f+1)n \cdot \log n] \cdot C_H + C_E + C_S. \tag{3}$$

### 3.2 Buffer Requirement

There are three different buffer spaces maintained by the receiver, Raw Packet Buffer, SymbolBuffer, and HashBuffer. Again, for the purpose of simplicity, it is assumed that strong relay-attacks cannot be launched by any attacker. Under this simplified assumption, let’s find out the amount of buffer spaces needed:

- Raw Packet Buffer: The worst case scenario occurs when the receiver receives the first authentic packet in each block. In this case, all the steps in the algorithm will be executed from step (1) to (10), including one erasure decoding, one signature verification, and  $1+\log n$  hash operations (for steps (7) and (10)). The other cases which require the second longest processing times are when the steps (5) though (10) are executed with steps (2) through (4) are skipped. In this case, at most  $1+\log n$  hash operations are needed for processing each packet (steps (7) and (10)). Hence, the total buffer space needed for storing raw packets is:

$$M[(f+1)R \times (C_E + C_S + C_D + (1+\log n)C_H) - 1] \tag{4}$$

- SymbolBuffer: The maximum space is needed when the receiver receives the first authentic packet in the current block with the smallest delivery delay from the sender, and the last authentic packet in the next block at its latest time instant with the largest delivery delay. This is because even when only one authentic packet (e.g., last one) in the next block arrives, the hashes/signature may have to be

extracted and verified from the SymbolBuffer to verify the authenticity of the received packet.

$$r_2 \cdot (2p + d)(f+1) \tag{5}$$

Here,  $d$  is the maximum delay that can be experienced by the receiver. And,  $r_2$  is the byte arrival rate (bytes/sec) for  $E_j$  and  $F_j$  that need to be stored in SymbolBuffer.

- **HashBuffer:** This buffer is needed for storing authentic hashes/signature once they are authenticated at step (4-2). One set of authentic hashes/signature will no longer be required when the possibility of packet arrivals for the next block is none. Also, while the hashes/signature in HashBuffer are being used for verifying the next block packets, their attached portions (in the next block packets) may be erasure decoded and verified. Hence, double buffering type of technique needs to be used for storing hashes/signature for two consecutive blocks at any time. Thus, the buffer requirement is:

$$2r_2 \cdot p(n-t)/n \tag{6}$$

- **Total Buffer space needed is:**

$$M[(f+1)R \times (C_E + C_S + (1 + \log n)C_H) - 1] + r_2 \cdot (2p + d)(f+1) + 2r_2 \cdot p(n-t)/n \tag{7}$$

**Table 1.** Buffer and Per-Block CPU requirements for Prediction Hash based approach (including Prediction Hash with One-way Key Chain) and PRABS

	Buffer Requirement	(Average) CPU requirement
PRABS	$(r_1 + r_2 + r_3)(p+d)(f+1) + M[(f+1)R \times (f+1) (C_E + C_S + C_D) - (f+1)]$	$(n + n \times \log n)(f+1)C_H + (1 + fn(n-t))(C_E + C_S)$
Predictive Hash	$r_2 \cdot (2p + d)(f+1) + 2r_2 \cdot p(n-t)/n + M[(f+1)R \times (C_E + C_S + (1 + \log n)C_H) - 1]$	$[2 + (2f+1)n + \text{floor}(fn/(n-t))] + (f+1)n \cdot \log n \cdot C_H + C_E + C_S$

Example figures are obtained from the following realistic numbers [12, 29] and the results are shown in Table 2.

$p = 0.3, d = 0.1, f = 10, n = 8, t = 4, M = 500, r_1 = 3120 \text{ bytes/sec}, r_2 = 400 \text{ bytes/sec}, r_3 = 480 \text{ bytes/sec}, C_E = 0.005, C_S = 0.005, C_H = 0.000125.$

One hash is assumed to occupy 20 bytes. It is shown that our scheme with PH and OKC improves the performance of the previous scheme with just PH technique, and our scheme outperforms PRABS with significant improvements.

**Table 2.** Buffer and Per-Block CPU requirements for an example system

	Worst-case Buffer Requirement	(Worst-case) Per-block CPU time
PRABS	69905 bytes	0.254 seconds
Prediction Hash with One-way Key Chain	11706 bytes	0.067 seconds



## 4 Conclusion

We developed a new authentication scheme based on PH and OKC techniques on top of erasure codes and distillation codes to provide enhanced resistance to DoS attacks while consuming much less resources compared to other block-based multicast stream authentication schemes. We also analyzed the worst-case resource requirements under the assumption that the security condition is satisfied, and found out that much less resources are needed compared to other protocols such as PRABS.

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